

[B] Final Examinations of Geometry and Measurement

Some Schools Examinations on Geometry

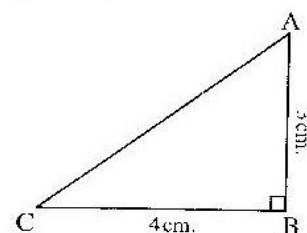
1 Cairo Governorate

Patriarchal College
Heliopolis


Answer the following questions :

1 Choose the correct answer :

- (1) The reflected image of the point A (- 3 , 2) in the origin point is the point \hat{A} (..... ,)
 (a) (3 , - 2) (b) (3 , 2) (c) (- 3 , - 2) (d) (2 , - 3)
- (2) The reflection in the X-axis maps the point B (X , y) to the point \hat{B} (..... ,)
 (a) (X , y) (b) (X , - y) (c) (- X , - y) (d) (- X , y)
- (3) * The measure of the exterior angle of the equilateral triangle at any one of its vertices equals
 (a) 60° (b) 120° (c) 150° (d) 30°
- (4) The image of the point (- 1 , 3) under the translation (4 , - 2) is the point (..... ,)
 (a) (5 , - 5) (b) (5 , 1) (c) (3 , 1) (d) (3 , - 1)
- (5) In the opposite figure :
 AC = cm.
 (a) 5 (b) 7
 (c) 8 (d) 6
- (6) * The measure of the interior angle of a regular polygon of 10 sides equals
 (a) 72° (b) 108° (c) 144° (d) 150°



2 Complete :

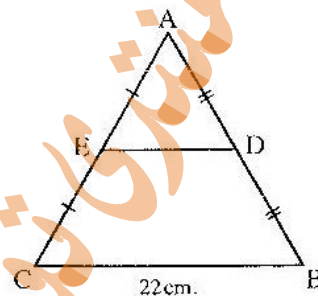
- (1) The image of the point A (4 , 3) by rotation around the origin point O and an angle whose measure is 360° is the point \hat{A} (..... ,)
- (2) If \hat{A} (- 3 , - 3) is the reflected image of the point A (X , y) in the origin point (0 , 0) , then X = and y =
- (3) The image of the point C (X , y) is the point \hat{C} (- X , - y) by rotation around the origin point O and an angle whose measure is°

- (4) * If ABCD is a parallelogram in which $m(\angle A) + m(\angle C) = 110^\circ$
 , then $m(\angle D) = \dots\dots\dots^\circ$

- (5) In the opposite figure :

If $BC = 22$ cm.

, then $ED = \dots\dots\dots$ cm.



- 3 [a] Find $\overline{A'B'}$ the translated image of \overline{AB} , where A (2 , 1) and B (2 , 4) when translated MN units in the direction of \overrightarrow{MN} , where M (-2 , 5) and N (3 , 7)

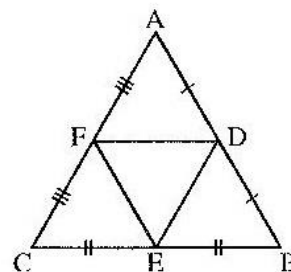
- [b] In the opposite figure :

$AB = 10$ cm. , $BC = 16$ cm. , and $AC = 14$ cm. ,

D , E and F are the midpoints of \overline{AB} , \overline{BC} , and \overline{AC} respectively.

Prove that :

The perimeter of $\triangle DEF = 20$ cm.



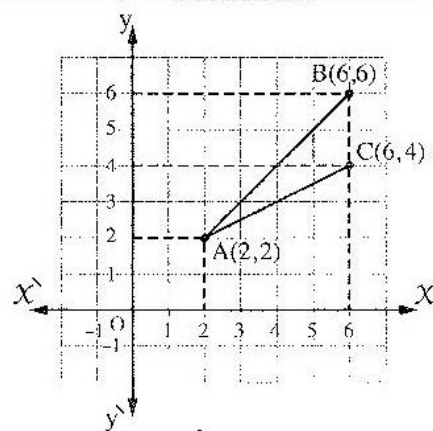
- 4 [a] In the opposite figure :

Draw the image of the $\triangle ABC$

by the reflection in the X-axis

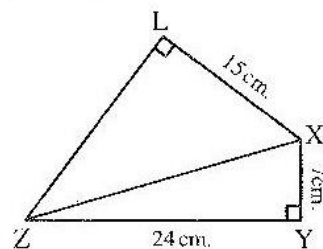
where A (2 , 2) , C (6 , 4)

and B (6 , 6)



- [b] In the opposite figure :

Find the length of \overline{LZ}

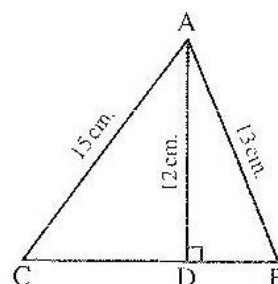


- 5 [a] In the opposite figure :

Prove that :

(1) $BC = 14$ cm.

(2) Area of $\triangle ABC = 84$ cm²



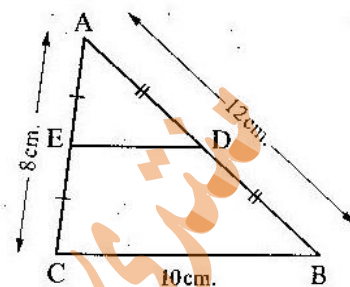
[b] In the opposite figure :

ABC is a triangle in which

$AB = 12 \text{ cm.}$, $BC = 10 \text{ cm.}$

and $AC = 8 \text{ cm.}$

Find the perimeter of the triangle ADE



2

Cairo Governorate

East Nasr City Educational Zone
Futures Language School



Answer the following questions :

1 Choose the correct answer from those given :

- ① The image of the point $(-4, 5)$ by translation $(2, -3)$ is
 (a) $(2, 2)$ (b) $(-2, 2)$ (c) $(2, -2)$ (d) $(-2, -2)$
- ② The point whose image by reflection in the origin point is itself is
 (a) $(1, 0)$ (b) $(0, 1)$ (c) $(0, 0)$ (d) $(-1, 0)$
- ③ The image of a triangle by rotation about the origin point with an angle of measure 360° is
 (a) point. (b) triangle. (c) line segment. (d) straight line.
- ④ If ABC is right-angled triangle at B , $AB = 20 \text{ cm.}$, $AC = 25 \text{ cm.}$, then the length of BC = cm.
 (a) 5 (b) 45 (c) 225 (d) 15
- ⑤ The number of axis of symmetry of a square equal
 (a) 0 (b) 1 (c) 2 (d) 4
- ⑥ * ABCD is a parallelogram in which : $m(\angle A) = 50^\circ$, then $m(\angle B) =$
 (a) 50° (b) 120° (c) 130° (d) 40°

2 Complete the following :

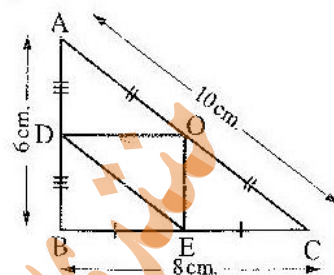
- ① Rotation in the plane reserves of angles.
- ② The line segment joining the midpoints of two sides of a triangle is the third side.
- ③ In the right-angled triangle , area of the square drawn on the hypotenuse equals of the lengths of the other two sides.
- ④ * The sum of measures of the exterior angles of the hexagon equals $^\circ$
- ⑤ The image of the point $(3, -8)$ by rotation about the origin point with an angles of measure 180° is

3 [a] In the opposite figure :

ABC is a triangle in which D , E , O are midpoints of \overline{AB} , \overline{BC} , \overline{AC} respectively , $\overline{DE} \parallel \overline{AC}$

AB = 6 cm. , BC = 8 cm. , AC = 10 cm.

Find with prove the perimeter of : $\triangle EDO$



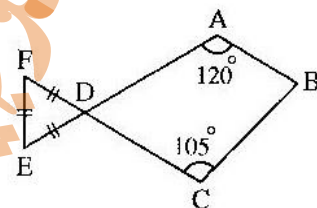
[b] * In the opposite figure :

$$\overline{AE} \cap \overline{CF} = \{D\}$$

, $\triangle DEF$ is an equilateral triangle

, $m(\angle A) = 120^\circ$ and $m(\angle C) = 105^\circ$

Find : $m(\angle B)$

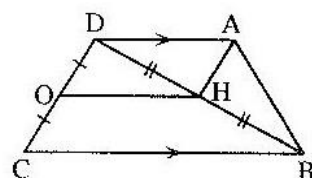


4 [a] In the opposite figure :

$$\overline{AD} \parallel \overline{BC}, AD = \frac{1}{2} BC$$

, H and O are midpoints of \overline{DB} and \overline{DC} respectively

Prove that : AHOD is a parallelogram



[b] In the opposite figure :

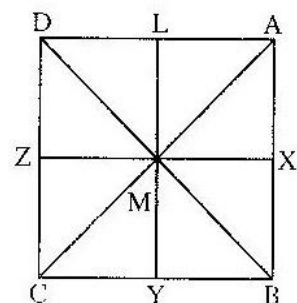
ABCD is a square X , Y , Z , L are midpoints of \overline{AB} , \overline{BC} , \overline{CD} and \overline{DA} respectively

Find :

(1) The image of $\triangle AML$ by translation with a magnitude AM in direction \overrightarrow{AM}

(2) The image of $\triangle AML$ by rotation about the point M with an angle of measure -90°

(3) The image of $\triangle AML$ by reflection in \overleftrightarrow{LY}



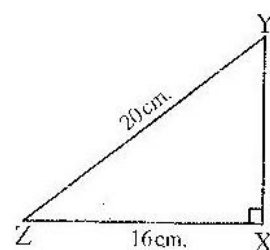
5 [a] Draw $\triangle OBC$ on a square lattice where O (0 , 0) , B (3 , 0) , C (0 , 4) , then draw its image by rotation about the origin point with an angle of measure 180°

[b] In the opposite figure :

XYZ is right-angled triangle at X

, YZ = 20 cm. , XZ = 16 cm.

Find : the length of \overline{XY}



3

Cairo Governorate

Zetoun Educational Administration
Gomhouria Language School


Answer the following questions :

1 Choose the correct answer :

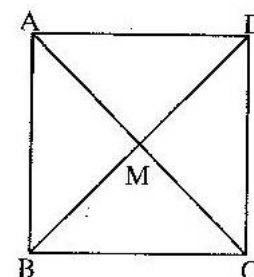
- (1) The line segment joining the midpoints of two sides of a triangle is the third side.
 (a) bisect to (b) perpendicular (c) equal to (d) parallel to
- (2) The image of a rhombus by any translation is a
 (a) rhombus. (b) rectangle. (c) square. (d) trapezium.
- (3) ABC is a triangle in which $m(\angle A) = 90^\circ$, then $(AC)^2 = (BC)^2 \dots\dots\dots (AB)^2$
 (a) + (b) - (c) \times (d) \div

(4) In the opposite figure :

ABCD is a square, $\overline{AC} \cap \overline{BD} = \{M\}$

, the image of $\triangle AMD$ by rotation $R(M, 90^\circ)$ is

- (a) $\triangle BMA$ (b) $\triangle DMA$
 (c) $\triangle DMC$ (d) $\triangle CMB$



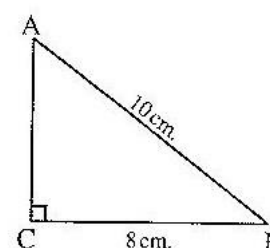
- (5) The image of the point $(-1, 3)$ by reflection in y-axis is
 (a) $(1, 3)$ (b) $(3, -1)$ (c) $(-1, -3)$ (d) $(1, -3)$
- (6) * In $\triangle ABC$: if $m(\angle A) + m(\angle B) = 110^\circ$, then $m(\angle C) = \dots\dots\dots$
 (a) 110° (b) 90° (c) 70° (d) 55°

2 Complete each of the following :

- (1) In the rectangle ABCD, $(AB)^2 + (AD)^2 = \dots\dots\dots$
- (2) * The square is a with a right angle.
- (3) The length of the line segment joining the midpoints of two sides of a triangle equals

(4) In the opposite figure :

AC = cm.

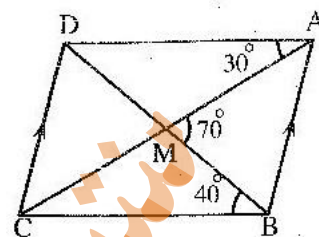


- (5) Translation in the plane reserves of angles.

3 [a] * In the opposite figure :

ABCD is a quadrilateral where : $\overline{AC} \cap \overline{BD} = \{M\}$
 $\overline{AB} \parallel \overline{DC}$, $m(\angle AMB) = 70^\circ$, $m(\angle MBC) = 40^\circ$
 and $m(\angle MAD) = 30^\circ$

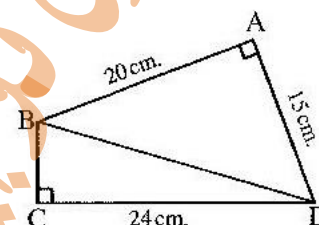
Prove that : ABCD is a parallelogram.



[b] In the opposite figure :

$m(\angle A) = m(\angle C) = 90^\circ$
 $AB = 20$ cm. , $CD = 24$ cm.
 $AD = 15$ cm.

Find : the perimeter of $\triangle BCD$



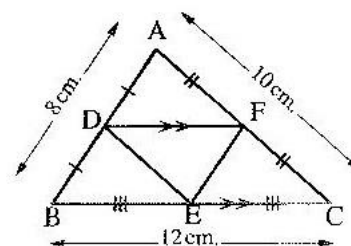
4 [a] Using the square lattice :

Draw $\triangle ABC$, where $A(-2, 3)$, $B(2, 3)$, $C(2, 6)$, then
 Find its image by translation $(X, y) \longrightarrow (X + 2, y - 1)$

[b] In the opposite figure :

D , E , F are midpoints of
 \overline{AB} , \overline{BC} , \overline{CA} respectively
 $AB = 8$ cm. , $BC = 12$ cm. , $AC = 10$ cm.

Find : the perimeter of $\triangle DEF$

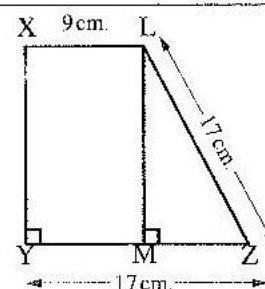


5 In the opposite figure :

XYZL is a trapezium , in which
 $\overline{XL} \parallel \overline{YZ}$, $m(\angle Y) = 90^\circ$
 $\overline{LM} \perp \overline{YZ}$, $YZ = ZL = 17$ cm. , $XL = 9$ cm.

Find : ① The length of \overline{XY}

② The image of \overline{XL} by translation of magnitude XY in the direction of \overline{XY}



4

Giza Governorate

Hafr EL-Baten Language Schools



Answer the following questions :

1 Complete :

- ① Square is a rectangle in which
- ② The image of the point $(2, 1)$ by reflection X-axis is
- ③ The image of the point $(2, 5)$ by translation $(X, y) \longrightarrow (X + 2, y - 3)$ is

(4) The measure of each interior angle of the regular pentagon is

(5) A rhombus with right-angle is called

2] Choose the correct answer :

(1) The number of diagonals of a quadrilateral is

- (a) 4 (b) 3 (c) 2 (d) 0

(2) The diagonal of square divided its vertex angle in two angles of the measure of each of them is

- (a) 30° (b) 45° (c) 60° (d) 90°

(3) The image of the point $(-3, 5)$ by rotation about the origin point and with an angle of measure 90° is

- (a) $(5, 3)$ (b) $(-5, 3)$ (c) $(3, 5)$ (d) $(-5, -3)$

(4) Any triangle has at least two interior angles.

- (a) right (b) obtuse (c) acute (d) reflex

(5) The sum of measures of the interior angles of the pentagon is

- (a) 540° (b) 720° (c) 360° (d) 180°

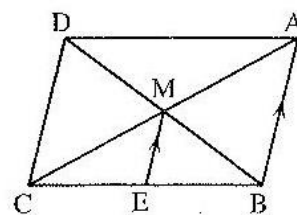
(6) * In the parallelogram XYZL, if $m(\angle X) = \frac{1}{2} m(\angle Y)$, then $m(\angle Y) = \dots\dots\dots$

- (a) 120° (b) 60° (c) 90° (d) 180°

3] [a] Prove that : the ray drawn from the midpoint of a side of a triangle parallel to another side bisects the third side.

[b] In the opposite figure :

ABCD is a parallelogram its diagonals are intersect at M
 $\overrightarrow{ME} \parallel \overrightarrow{AB}$ prove that $BE = EC$



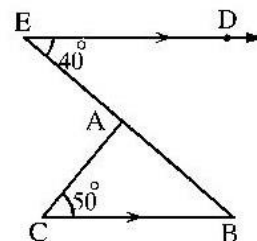
4] [a] Find the length of the diagonal of a rectangle whose area 48 cm^2 and of width 6 cm.

[b] In the opposite figure :

$\overrightarrow{ED} \parallel \overrightarrow{CB}$, $m(\angle C) = 50^\circ$

, $m(\angle E) = 40^\circ$

Prove that : $\overrightarrow{AC} \perp \overrightarrow{BE}$

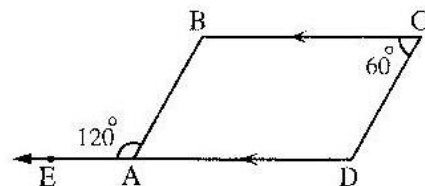


5] In the opposite figure :

$E \in \overrightarrow{DA}$, $m(\angle EAB) = 120^\circ$

, $m(\angle C) = 60^\circ$, $\overrightarrow{DA} \parallel \overrightarrow{CB}$

Prove that : ABCD is a parallelogram



5

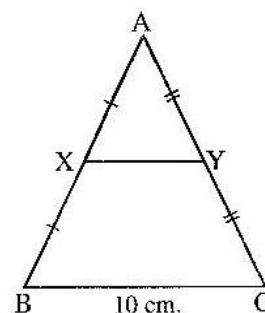
Giza Governorate

Omrania Directorate
EL-Sadat Governmental Language School


Answer the following questions :

1 Choose the correct answer from given ones :

- (1) The image of the point $(-2, 3)$ by reflection in y-axis is
 (a) $(2, 3)$ (b) $(-2, -3)$ (c) $(2, -3)$ (d) $(3, 2)$
- (2) The image of the point $(-3, 5)$ by rotation about the origin point with angle of measure 90° is
 (a) $(5, 3)$ (b) $(-5, -3)$ (c) $(3, 5)$ (d) $(-5, 3)$
- (3) In $\triangle ABC$ if $m(\angle B) = 90^\circ$, $AB = 6$ cm., $BC = 8$ cm., then $AC =$ cm.
 (a) 100 (b) 8 (c) 6 (d) 10
- (4) In the opposite figure :
 X , Y are midpoints of \overline{AB} , \overline{AC} respectively , $BC = 10$ cm., then $XY =$ cm. .
 (a) 5 (b) 20
 (c) 10 (d) 30
- (5) The image of the point $(2, -3)$ by translation $(4, 1)$ is
 (a) $(6, 2)$ (b) $(4, -2)$ (c) $(6, -2)$ (d) $(-2, 6)$
- (6) * The measure of the interior angle of a regular pentagon is
 (a) 900° (b) 108° (c) 720° (d) 540°

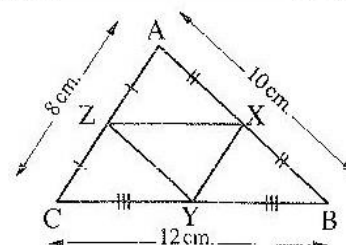


2 Complete each of the following :

- (1) The number of axis of symmetry of square is
- (2) In the parallelogram XYZL, if $m(\angle X) = \frac{1}{2} m(\angle Y)$, then $m(\angle Y) =$ °
- (3) The line segment joining between the midpoints of two sides of triangle is
- (4) The image of $(3, 7)$ by rotation $R(O, 180^\circ)$ is
- (5) If \hat{A} is the image of A by reflection in M and $MA = 6$ cm., then $A\hat{A} =$ cm.

3 [a] In the opposite figure :

ABC is a triangle in which X , Y , Z are midpoints of \overline{AB} , \overline{BC} and \overline{CA} , $AB = 10$ cm., $BC = 12$ cm., $AC = 8$ cm.

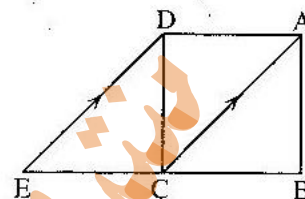
Find with proof : perimeter of $\triangle XYZ$


[b] * In the opposite figure :

ABCD is a square , $E \in \overline{BC}$, $\overline{AC} \parallel \overline{DE}$

(1) Prove that : ACED is a parallelogram.

(2) Find : $m(\angle ACE)$

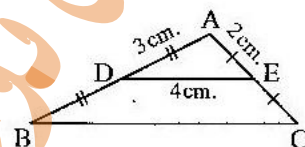


4 [a] In the opposite figure :

D , E are midpoints of \overline{AB} , \overline{AC} respectively

$AD = 3$ cm. , $AE = 2$ cm. , $DE = 4$ cm.

Find : the perimeter of $\triangle ABC$

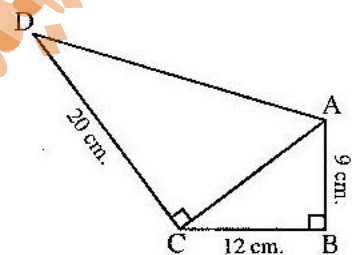


[b] In the opposite figure :

$m(\angle B) = m(\angle ACD) = 90^\circ$

$AB = 9$ cm. , $BC = 12$ cm. , $CD = 20$ cm.

Find length of : \overline{AC} and \overline{AD}



5 On the square lattice draw $\triangle ABC$ where $A(1, 1)$, $B(4, 1)$, $C(4, 4)$, then determine each of the following :

(1) The image of $\triangle ABC$ by reflex in y-axis.

(2) The image of $\triangle ABC$ by rotation about origin point with angle of measure 180°

6 Alexandria Governorate

East Educational Zone
English Language Schools



Answer the following questions :

1 Complete the following :

(1) The line segment joining the midpoints of two sides of a triangle is the third side.

(2) If $\triangle XYZ$ is a right angled triangle at X , $XY = 12$ cm. and $XZ = 9$ cm. , then $YZ =$

(3) * If ABCD is a rhombus , then \perp

(4) The image of the point $(-1, 2)$ by rotation about the origin point with angle of measure 90° is

(5) The sum of the measures of the accumulative angles about a point =

2 Choose the correct answer from those given :

(1) If X and Y are the midpoints of \overline{AB} and \overline{AC} in $\triangle ABC$ and $XY = 3$ cm. , then $BC =$ cm.

(a) 3

(b) 5

(c) 6

(d) 9

(2) The image of the point (2 , 3) by transformation $(X , y) \longrightarrow (X + 1 , y - 2)$ is the point

- (a) (3 , 4) (b) (2 , 1) (c) (- 3 , 0) (d) (3 , 1)

(3) The image of the point (5 , 1) by reflection in the origin point is

- (a) (1 , 5) (b) (- 1 , - 5) (c) (- 5 , - 1) (d) (- 1 , 5)

(4) The perpendicular to one of two parallel lines is to the other.

- (a) parallel (b) equal (c) congruent (d) perpendicular

(5) The angle with measure 70° complement angle with measure $^\circ$

- (a) 70 (b) 110 (c) 290 (d) 20

(6) * The sum of measures of the exterior angles of the triangle = $^\circ$

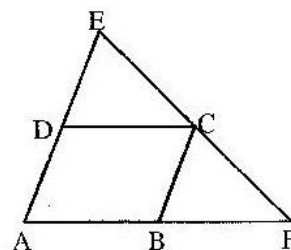
- (a) 180 (b) 90 (c) 360 (d) 270

[3] [a] In the opposite figure :

ABCD is a parallelogram

$E \in \overrightarrow{AD}$ where $AD = DE$, $\overrightarrow{EC} \cap \overrightarrow{AB} = \{F\}$

Prove that : $EC = CF$

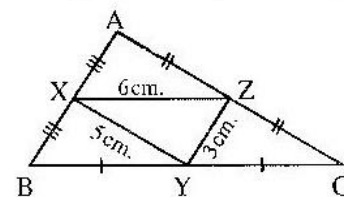


[b] In the opposite figure :

X , Y , Z are the midpoints of \overline{AB} , \overline{BC} , \overline{CA} respectively.

If $XY = 5$ cm. , $YZ = 3$ cm. and $XZ = 6$ cm.

Find with proof the perimeter of $\triangle ABC$

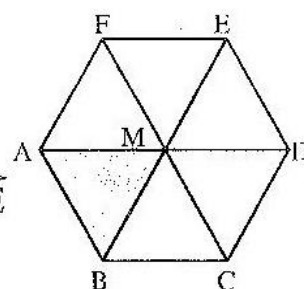


[4] In the opposite figure :

ABCDEF is a regular hexagon

Find the image of $\triangle ABM$ by :

- (1) Reflection on \overleftrightarrow{EB} (2) Translation FE in direction of \overrightarrow{FE}
 (3) Rotation (M , 120°) (4) Reflection in M
 (5) Rotation (M , 300°)



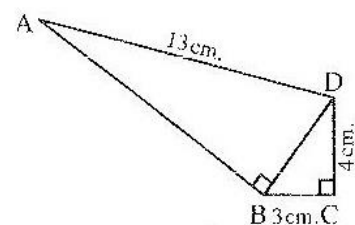
[5] [a] In the square net draw $\triangle ABC$ in which A (- 2 , 2) , B (3 , 1) , and C (2 , 5) , then find its image by reflection in the origin point.

[b] In the opposite figure :

$BC = 3$ cm. , $CD = 4$ cm. , $DA = 13$ cm.

$m(\angle ABD) = m(\angle C) = 90^\circ$

Find with proof the length of : \overline{BD} , \overline{AB}





7

Alexandria Governorate

Mid Educational Zone
Math's Supervision

Answer the following questions :

1 Complete each of the following :

- ① The measure of the right angle =°
- ② The image of the point (2 , - 1) by reflection in X-axis is
- ③ The ray drawn parallel to one side of triangle and passing through the midpoint of another side
- ④ * In $\triangle ABC$: If $m(\angle A) + m(\angle C) = m(\angle B)$, then $m(\angle B) = \dots\dots\dots$
- ⑤ The line segment joining the midpoints of two sides of a triangle is

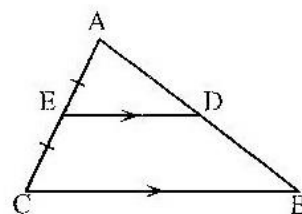
2 Choose the correct answer :

- ① The perimeter of a square with side length 6 cm. = cm.
(a) 30 (b) 36 (c) 24 (d) 216
- ② The image of the point (- 1 , 3) by translation (4 , - 2) is
(a) (3 , 1) (b) (3 , - 1) (c) (5 , 1) (d) (5 , - 5)
- ③ The edge length of a cube whose total area is 600 cm^2 . is cm.
(a) 10 (b) 100 (c) 300 (d) 90
- ④ In $\triangle ABC$, if $m(\angle B) = 90^\circ$, $AB = 3 \text{ cm}$. , $BC = 4 \text{ cm}$. , then $AC = \dots\dots\dots \text{ cm}$.
(a) 7 (b) 1 (c) 5 (d) 4

⑤ In the opposite figure :

ED : BC = :

- (a) 1 : 1 (b) 1 : 2
- (c) 1 : 3 (d) 1 : 4



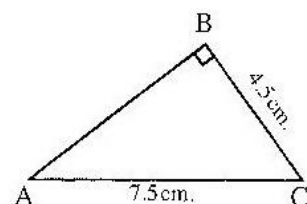
⑥ * The parallelogram whose two diagonals are equal in length and perpendicular is called

- (a) rectangle. (b) square. (c) rhombus. (d) trapezium.

3 [a] In the opposite figure :

ABC is a right-angled triangle at B

, AC = 7.5 cm. , BC = 4.5 cm.

Find : the length of \overline{AB}


[b] Draw the image of the square ABCD where A (2 , 4) , B (2 , 1) , C (5 , 1) , D (5 , 4) by reflection in the X-axis.

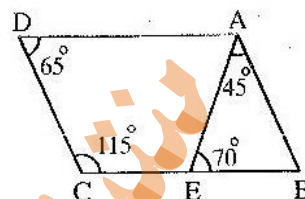
4 [a] * In the opposite figure :

$E \in \overline{BC}$, $m(\angle BAE) = 45^\circ$

, $m(\angle AEB) = 70^\circ$, $m(\angle D) = 65^\circ$

and $m(\angle C) = 115^\circ$

Prove that : ABCD is a parallelogram.



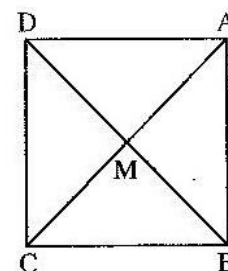
[b] If the image of the point A (1 , 1) by translation in the coordinate plane is \hat{A} (2 , 2)
 , find the images of the points O (0 , 0) , B (4 , 2) , C (− 3 , 5) by the same translation.

5 [a] In the opposite figure :

ABCD is a square

, M is the intersection point of its diagonal

, find the image of $\triangle MAB$ by rotation about M with angle 90°

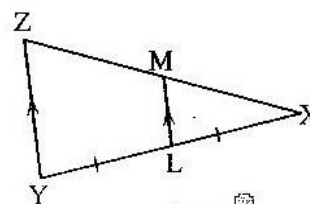


[b] In the opposite figure :

L is a midpoint of \overline{XY}

, $\overline{LM} \parallel \overline{YZ}$, $XZ = 10$ cm.

Find : the length of \overline{XM}



8

El-Kalyoubia Governorate

Directorate of Education
 Inspection of Mathematics



Answer the following questions :

1 Complete the following :

- (1) The ray drawn from the midpoint of a side of a triangle and parallel to another side
- (2) The image of the point (5 , − 3) by translation 3 units in negative direction of X-axis is
- (3) (− 3 , 2) is the image of the point (− 3 , − 2) by reflection in
- (4) ABCD is a parallelogram in which $m(\angle A) = 50^\circ$, then $m(\angle B) =$
- (5) If $\triangle XYZ$ in which $m(\angle Y) = 90^\circ$, then $(XZ)^2 =$ +

2 Choose the correct answer :

- (1) The image of the point (2 , 5) by reflection in y-axis is
 (a) (− 2 , 5) (b) (5 , 2) (c) (− 2 , − 5) (d) (2 , − 5)
- (2) The measure of each angle of a regular hexagon is
 (a) 120° (b) 136° (c) 105° (d) 90°

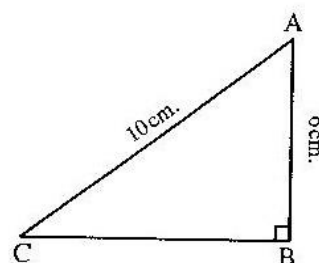
- (3) The image of the point $(3, -7)$ by reflection in the origin point is
- (a) $(-3, 7)$ (b) $(-3, -7)$ (c) $(3, -7)$ (d) $(3, 7)$
- (4) The sum of measures of interior angles of a triangle equals
- (a) 90° (b) 180° (c) 270° (d) 360°
- (5) The number of diagonals of quadrilateral is
- (a) 4 (b) 3 (c) 5 (d) 2
- (6) * If the measure of an interior angle of a regular polygon is 135° , then the number of its sides is
- (a) 6 (b) 4 (c) 7 (d) 8

3 [a] In the opposite figure :

ABC is a triangle in which

$m(\angle B) = 90^\circ$, $AB = 6$ cm. , $AC = 10$ cm.

Find with proof : the length of \overline{BC}

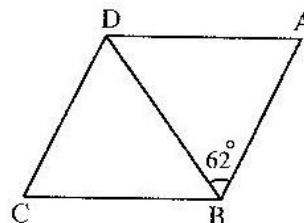


[b] * In the opposite figure :

ABCD is a rhombus , \overline{BD} is a diagonal in it

, $m(\angle ABD) = 62^\circ$

Find with proof : $m(\angle A)$



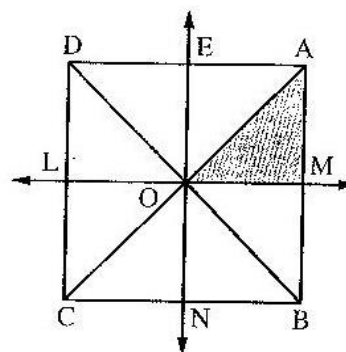
4 [a] In the opposite figure :

ABCD is a square of side length 6 cm.

and the origin point is its centre.

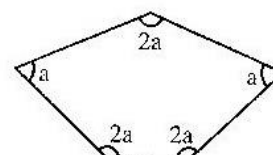
Find :

- (1) The image of $\triangle AOM$ by translation 3 cm. in the direction of \overrightarrow{AB}
- (2) The image of $\triangle AOM$ by rotation $R(O, 90^\circ)$
- (3) The image of $\triangle AOM$ by reflection in \overleftrightarrow{EN}



[b] * In the opposite figure :

Find the value of a

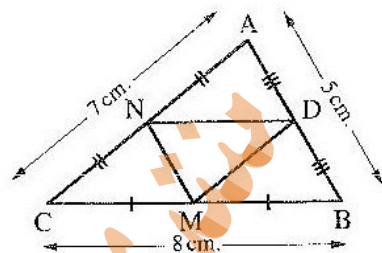


5 [a] In the opposite figure :

$AB = 5 \text{ cm.}$, $BC = 8 \text{ cm.}$

, $AC = 7 \text{ cm.}$ D , M , N are
the midpoints of \overline{AB} , \overline{BC} and \overline{AC}

respectively find with proof the perimeter of ΔDMN



[b] Draw the triangle ABC in which $AB = 3 \text{ cm.}$, $BC = 4 \text{ cm.}$, $m(\angle B) = 90^\circ$
, then draw its image by reflection in straight line \overleftrightarrow{BC}

9

El-Monofia Governorate

Maths Supervision



Answer the following questions :

1 Choose the correct answer :

- (1) The image of the point $(2, -1)$ by reflection in y-axis is
 (a) $(2, 1)$ (b) $(-2, -1)$ (c) $(-2, 1)$ (d) $(2, -1)$
- (2) ABCD is a parallelogram , $m(\angle A) = 70^\circ$, then $m(\angle C) = \dots\dots\dots^\circ$
 (a) 110 (b) 35 (c) 70 (d) 140
- (3) The diagonals are equal in length and perpendicular in
 (a) square. (b) rhombus. (c) rectangle. (d) parallelogram.
- (4) The image of the point $(5, -3)$ by translation 3 units in negative direction of X-axis is
 (a) $(-3, 5)$ (b) $(-2, -3)$ (c) $(2, -3)$ (d) $(5, 0)$
- (5) In ΔABC , if D and E are the midpoints of \overline{AB} and \overline{AC} respectively , $BC = 8 \text{ cm.}$
 , then $DE = \dots\dots\dots \text{ cm.}$
 (a) 16 (b) 8 (c) 4 (d) 2
- (6) * The triangle contains two angles at least
 (a) acute (b) obtuse (c) right (d) reflex

2 Complete each of the following :

- (1) The ray drawn from the midpoint of a side of the triangle parallel to another side
- (2) The number of axis of symmetry of isosceles triangle =
- (3) The image of the point by rotation about the origin point with an angle of measure 90° is $(-1, 4)$
- (4) The length of diagonal of a rectangle whose dimensions are 6 cm. and 8 cm. = cm.
- (5) The translation is determined by and

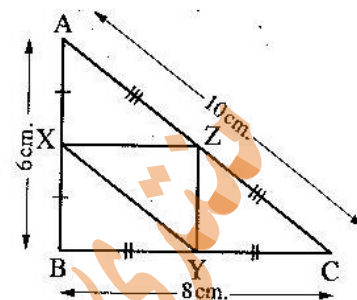
3 [a] In the opposite figure :

X, Y, Z are midpoints of \overline{AB}

, \overline{BC} and \overline{AC} , $AB = 6$ cm.

, $BC = 8$ cm. , $AC = 10$ cm.

Find : the perimeter of $\triangle XYZ$



[b] Using the square lattice , draw the triangle ABC where $A(3, -1)$, $B(5, 2)$ and $C(-2, 4)$, then draw its image by rotation $R(O, 180^\circ)$

4 [a] In the opposite figure :

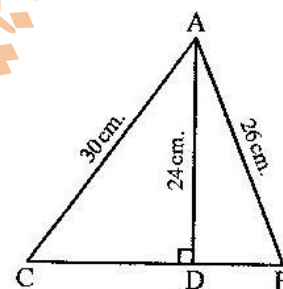
$\overline{AD} \perp \overline{BC}$, if $AD = 24$ cm.

, $AB = 26$ cm. , $AC = 30$ cm.

Find :

① The length of \overline{BC}

② The area of $\triangle ABC$



[b] In a cartesian plane draw the image of $\triangle ABC$ where $A(-2, 3)$, $B(2, 3)$, $C(2, 6)$ by translation $(x, y) \rightarrow (x + 2, y - 1)$

5 In the opposite figure :

ABCD is a parallelogram , M is the point of intersection of its diagonals

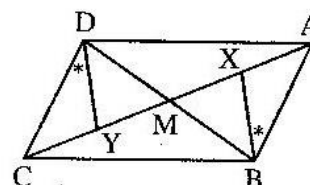
and $X \in \overline{AC}$, $Y \in \overline{AC}$, such that

$m(\angle ABX) = m(\angle CDY)$

Prove that :

① $\triangle ABX$ is the image of $\triangle CDY$ by reflection in M

② The figure $XB Y D$ is a parallelogram.



10 El-Gharbia Governorate

Central Maths supervision
Official Language Schools



Answer the following questions :

1 Choose the correct answer from those given :

① The image of the point $(-3, 5)$ by rotation about the origin point and with an angle of measure 90° is

(a) $(5, 3)$

(b) $(-5, 3)$

(c) $(3, 5)$

(d) $(-5, -3)$

- (2) The image of the point $(2, -1)$ by reflection in X-axis is
- (a) $(2, 1)$ (b) $(2, 2)$ (c) $(-2, -1)$ (d) $(-1, 2)$
- (3) In $\triangle ABC$ if : $m(\angle A) > m(\angle B) + m(\angle C)$, then the angle A is
- (a) acute. (b) right. (c) obtuse. (d) straight.
- (4) The image of the square by rotation about origin point with an angle of measure 90° is
- (a) rectangle. (b) square. (c) rhombus. (d) trapezium.
- (5) In $\triangle ABC$ if : X , Y are the midpoints of \overline{AC} and \overline{BC} respectively , then $\overline{XY} \parallel$
- (a) \overline{AB} (b) \overline{BC} (c) \overline{AC} (d) \overline{CY}
- (6) The measure of the interior angle of a regular polygon of 18 sides equals
- (a) 130° (b) 140° (c) 150° (d) 160°

2 Complete each of the following :

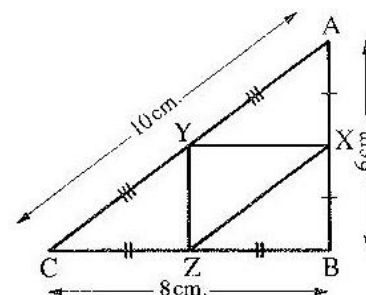
- (1) The line segment joining the midpoints of two sides of a triangle is the third side.
- (2) The image of the point $(3, -2)$ by translation on $(X - 1, y + 6)$ is
- (3) The image of the point $(3, 2)$ by rotation with an angle of measure 180° about the origin point is
- (4) The image of the point $(4, 1)$ by reflection in the origin point is
- (5) In $\triangle XYZ$, $m(\angle Y) = 90^\circ$, then $(XZ)^2 =$

3 [a] In the opposite figure :

$AB = 6 \text{ cm}$, $BC = 8 \text{ cm}$, $AC = 10 \text{ cm}$.

X , Y , Z are midpoints of \overline{AB} , \overline{AC} and \overline{BC} respectively

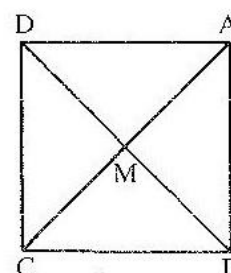
Find : the perimeter of $\triangle XYZ$



[b] In the opposite figure :

ABCD is a square , whose diagonal intersect at M , **find :**

- (1) The image of $\triangle ABC$ by reflection in \overleftrightarrow{AC}
- (2) The image of $\triangle MAB$ by reflection in point M



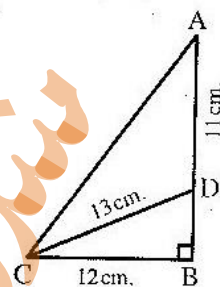
4 [a] In the opposite figure :

ΔABC in which $m(\angle B) = 90^\circ$

$D \in \overline{AB}$ such that $AD = 11$ cm.

, if $BC = 12$ cm , $DC = 13$ cm.

Find the length of each of : \overline{AB} , \overline{AC}



[b] Complete :

If the point $(1, 4)$ is the image of the point $(-1, 3)$ by a translation (X, y) , then the image of the point $(3, -2)$ by the same translation is

5 [a] Draw ΔABC where $A(1, 5)$, $B(3, 1)$ and $C(5, 3)$, then draw its image :

(1) By reflection in y-axis.

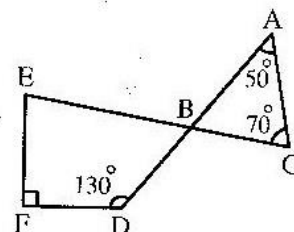
(2) By rotation about origin point with an angle of measure 180°

[b] * In the opposite figure :

$\overline{CE} \cap \overline{AD} = \{B\}$, $m(\angle A) = 50^\circ$, $m(\angle C) = 70^\circ$

, $m(\angle D) = 130^\circ$ and $m(\angle F) = 90^\circ$

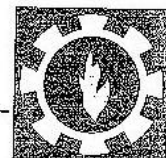
Find : $m(\angle E)$



11

Suez Governorate

Maths Inspectorate



Answer the following questions :

1 Choose the correct answer :

(1) The image of the point $(2, -5)$ by reflection in X-axis is

- (a) $(-2, 5)$ (b) $(2, 5)$ (c) $(-2, -5)$ (d) $(5, 2)$

(2) The right-angled triangle has right angle.

- (a) 1 (b) 2 (c) 0 (d) 3

(3) The image of the point $(-3, 5)$ by rotation about origin point with angle 90° is

- (a) $(-3, 5)$ (b) $(-5, 3)$ (c) $(3, 5)$ (d) $(-5, -3)$

(4) The hexagon has sides.

- (a) 5 (b) 6 (c) 7 (d) 8

(5) The image of the point $(3, -2)$ by translation $(-1, 6)$ is

- (a) $(2, 4)$ (b) $(-2, 4)$ (c) $(7, -8)$ (d) $(2, -4)$

(6) The measure of the interior angle of a regular pentagon =

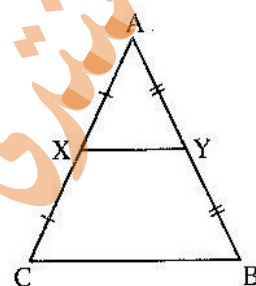
- (a) 900° (b) 180° (c) 540° (d) 108°

2 Complete :

(1) In $\triangle ABC$ if $m(\angle B) = 90^\circ$, then $(AC)^2 = \dots + \dots$

(2) In the opposite figure :

$\overline{XY} \parallel \dots$



(3) The image of $(3, -4)$ by reflection in y-axis is

(4) The ray drawn from the midpoint of a side of a triangle parallel to another side

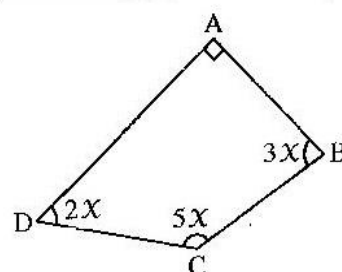
(5) The image of $(2, -1)$ by rotation about origin point with an angle of measure 180° is

3 [a] In the opposite figure :

ABCD is a quadrilateral

in which : $m(\angle A) = 90^\circ$

Find : the value of X

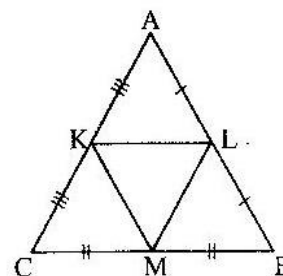


[b] In the opposite figure :

K, L, M are midpoints of \overline{AC} , \overline{AB} , \overline{BC}

$AB = 5$ cm, $BC = 8$ cm, $AC = 7$ cm.

Find the perimeter of : $\triangle KLM$

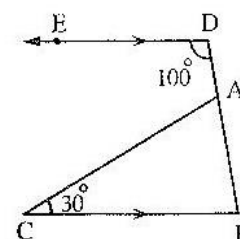


4 [a] In the opposite figure :

$\overline{DE} \parallel \overline{BC}$, $m(\angle D) = 100^\circ$

, $m(\angle C) = 30^\circ$ and $A \in \overline{DB}$

Find : $m(\angle BAC)$



[b] Draw $\triangle ABC$ where $A(1, 1)$, $B(4, 1)$, $C(4, 5)$ find its image by reflection in y-axis. By using square lattice.

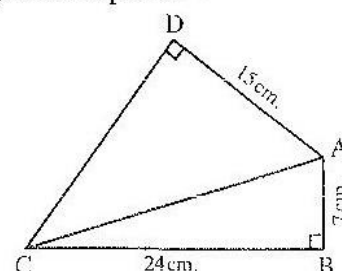
5 [a] Complete : The sum of the measures of the accumulative angles at a point =

[b] In the opposite figure :

$m(\angle B) = m(\angle D) = 90^\circ$, $AD = 15$ cm.

, $AB = 7$ cm, $BC = 24$ cm.

Find : the length of \overline{AC} , \overline{DC}



12

Damietta Governorate

Inspection Of Mathematics



Answer the following questions :

1 Choose the correct answer :

- (1) The image of the point (3 , 5) by reflection in y-axis is
 (a) (− 3 , − 5) (b) (3 , − 5) (c) (− 3 , 5) (d) (− 5 , − 3)
- (2) The length of line segment joining between two midpoints of two sides of triangle = the length of its third side.
 (a) $\frac{1}{2}$ (b) $\frac{2}{3}$ (c) $\frac{1}{4}$ (d) $\frac{1}{5}$
- (3) The measure of the right angle = °
 (a) 180 (b) 90 (c) 120 (d) 0
- (4) If ABC is a right-angled triangle at B , AB = 4 cm. , BC = 3 cm. , then AC = cm.
 (a) 7 (b) 1 (c) 4 (d) 5
- (5) The area of square of side length 3 cm is cm².
 (a) 9 (b) 6 (c) 12 (d) 3
- (6) The parallelogram whose two diagonals are is called a rectangle.
 (a) parallel (b) perpendicular (c) equal in length (d) bisect each other

2 Complete :

- (1) The image of the point (2 , 3) by rotation R (O , 90°) is
- (2) The number of axis of symmetry of the square =
- (3) Translation reserves of angles.
- (4) If ABC is right-angled triangle at B , then $(AB)^2 = (AC)^2 - \dots\dots\dots$
- (5) The line segment joining between two midpoints of two sides of triangle is parallel to

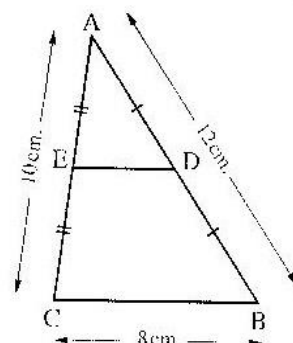
3 [a] In the opposite figure :

ABC is a triangle in which AB = 12 cm.

BC = 8 cm. , AC = 10 cm.

Find by proof :

the perimeter of triangle ADE



[b] In the opposite figure :

$$m(\angle B) = 90^\circ, \overline{DC} \perp \overline{AC}$$

$AB = 12 \text{ cm}$, $BC = 9 \text{ cm}$, and $CD = 20 \text{ cm}$.

Find by proof : the length of \overline{AC} and \overline{AD}

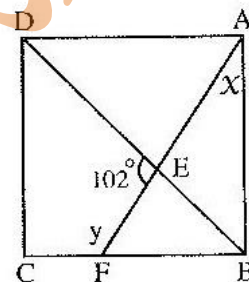


4 [a] In the opposite figure :

ABCD is a square

, find in degrees the value

of each of x and y



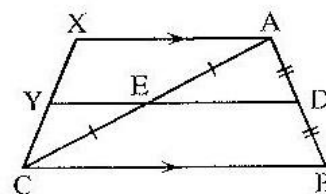
[b] Draw the image of $\triangle ABC$ in which : $AB = 6 \text{ cm}$, $BC = 4 \text{ cm}$, $AC = 5 \text{ cm}$,
by reflection in \overleftrightarrow{AC}

5 [a] In the opposite figure :

$$AD = DB, AE = EC, \overline{AX} \parallel \overline{BC}$$

$$, \overline{DE} \cap \overline{XC} = \{Y\},$$

prove that : Y is the midpoint of \overline{XC}



[b] If the point $\hat{A}(4, 5)$ is the image of the point $A(1, 7)$ by translation

$$(X, y) \longrightarrow (X + a, y + b) \text{ find :}$$

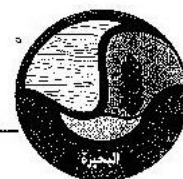
(1) The value of a and b

(2) The image of the point $B(2, -4)$ by the same translation.

13

El-Beheira Governorate

General Math Supervision



Answer the following questions :

1 Choose the correct answer :

(1) The image of the point $(2, -1)$ by reflection in X-axis is

(a) $(2, 1)$

(b) $(1, 2)$

(c) $(-2, -1)$

(d) $(-1, 2)$

(2) If the image of the point $(5, -3)$ by rotation about the origin point is itself , then the measure of rotation angle is

(a) 90°

(b) 180°

(c) 270°

(d) 360°

- (3) The image of the point $(-1, 3)$ by translation $(4, -2)$ is
 (a) $(3, 1)$ (b) $(3, -1)$ (c) $(5, 1)$ (d) $(5, -5)$
- (4) The smallest number of the acute angle in any triangle is
 (a) zero (b) 1 (c) 2 (d) 3
- (5) The image of the point $(-2, 1)$ by reflection in the origin point is
 (a) $(2, 1)$ (b) $(-2, 1)$ (c) $(2, -1)$ (d) $(-2, -1)$
- (6) * ABCD is a parallelogram in which $m(\angle A) + m(\angle C) = 100^\circ$, then $m(\angle B) =$
 (a) 50° (b) 100° (c) 130° (d) 180°

2 Complete of each of the following :

- (1) The line segment joining the midpoints of two sides of triangle is to the third side.
- (2) The image of the point $(4, 6)$ by translation : $(X, y) \longrightarrow (X, y - 7)$ is
- (3) The image of the point $(2, -4)$ by rotation about the origin point with an angle of measure 90° is
- (4) The ray drawn from the midpoint of a side of a triangle parallel to another side the third side.
- (5) In $\triangle XYZ$ if $m(\angle Y) = 90^\circ$, then $(XZ)^2 =$

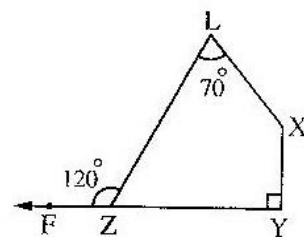
3 [a] Using the square lattice :

Draw $\triangle XYZ$ in which $X(4, 1)$, $Y(5, 0)$, $Z(-1, -2)$, then draw its image by rotation about the origin point with an angle of measure (-180°)

[b] In the opposite figure :

$F \in \overline{YZ}$, $m(\angle L) = 70^\circ$
 , $m(\angle Y) = 90^\circ$ and $m(\angle LZF) = 120^\circ$

Find : $m(\angle X)$

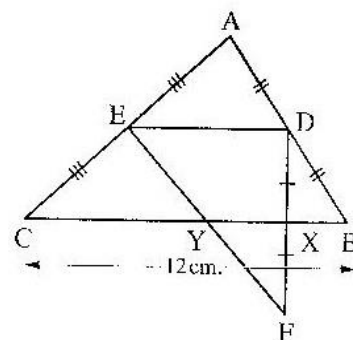


4 [a] In the opposite figure :

D is the midpoint of \overline{AB} , E is the midpoint of \overline{AC}
 , $\overline{DF} \cap \overline{BC} = \{X\}$, $DX = XF$ and $BC = 12$ cm.

Find : the length of \overline{XY}

- [b] Find the length of the diagonal of rectangle whose area 48 cm^2 , and its width 6 cm.



5 [a] In the opposite figure :

ΔABC in which $m(\angle B) = 90^\circ$, $\overline{AE} \parallel \overline{BC}$

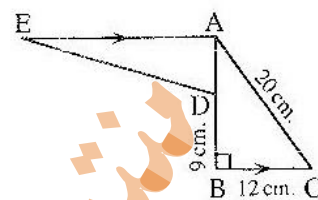
if $BC = 12$ cm. , $AC = 20$ cm. , $D \in \overline{AB}$

such that $BD = 9$ cm. , $AE = 2 BC$

Find :

(1) The length of \overline{AD}

(2) The length of \overline{ED}



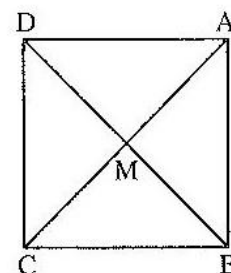
[b] In the opposite figure :

ABCD is a square , whose diagonals intersect at M

Find :

(1) The image of ΔABC by reflection in \overleftrightarrow{AC}

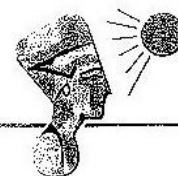
(2) The image of ΔMAB by rotation about M with angle of measure (-90°)



14

El-Menia Governorate

Governmental Language Schools



Answer the following questions :

1 Choose the correct answer :

(1) The image of point $(-1, 3)$ by translation $(4, -2)$ is

- (a) $(3, 1)$ (b) $(3, -1)$ (c) $(5, 1)$ (d) $(5, -5)$

(2) * The measure of the exterior angle of the equilateral triangle at anyone of its vertices equals

- (a) 60° (b) 120° (c) 150° (d) 30°

(3) The image of point $(3, -5)$ by reflection in y-axis is

- (a) $(3, 5)$ (b) $(-3, -5)$ (c) $(-3, 5)$ (d) $(-5, 3)$

(4) The image of point $(-3, 5)$ by rotation about the origin point with an angle of measure (-90°) is

- (a) $(5, 3)$ (b) $(-5, 3)$ (c) $(3, 5)$ (d) $(-5, -3)$

(5) The image of the square by rotation about the origin point with an angle of measure 90° is

- (a) rectangle. (b) square. (c) rhombus. (d) trapezium.

(6) The sum of measures of the exterior angles of the hexagon =

- (a) 720° (b) 120° (c) 180° (d) 360°

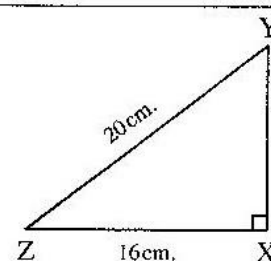
2 Complete :

- (1) The ray drawn from the midpoint of a side of a triangle parallel to another side the third side.
- (2) The line segment joining the midpoint of two sides of a triangle is the third side.
- (3) The length of the line segment joining the midpoints of two sides of a triangle is the length of the third side.
- (4) The image of the point $(2, -1)$ by rotation about the original point with an angle of measure (-180°) is
- (5) $(-3, 2)$ is the image of the point $(3, 2)$ by reflection in axis.

3 [a] In the opposite figure :

XYZ is a triangle in which $m(\angle X) = 90^\circ$,
 $YZ = 20$ cm. , $XZ = 16$ cm.

Find : the length of \overline{XY}

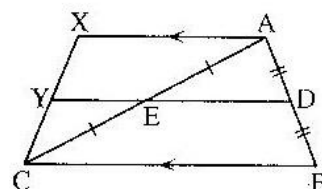


- [b]** Using the lattice , draw \overline{AB} where $A(4, 3)$, $B(-1, 1)$, then find the image of \overline{AB} by translation $(X, Y) \longrightarrow (X + 2, Y - 1)$

4 [a] In the opposite figure :

$AD = DB$, $AE = EC$, $\overline{AX} \parallel \overline{BC}$
 $\overline{DE} \cap \overline{XC} = \{Y\}$

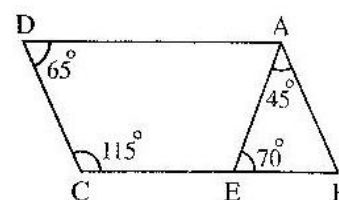
Prove that : Y is the midpoint of \overline{XC}



[b] In the opposite figure :

$E \in \overline{BC}$, $m(\angle BAE) = 45^\circ$,
 $m(\angle AEB) = 70^\circ$, $m(\angle D) = 65^\circ$
 and $m(\angle C) = 115^\circ$

Prove that : ABCD is a parallelogram.

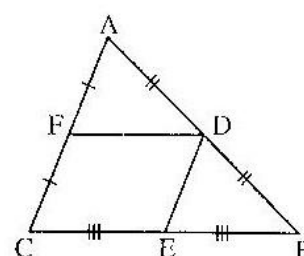


5 [a] In the opposite figure :

ABC is a triangle in which D , E and F are the midpoints of \overline{AB} , \overline{BC} and \overline{CA} respectively.

$BC = 12$ cm. , and $AC = 10$ cm.

Find : the perimeter of the quadrilateral DECF

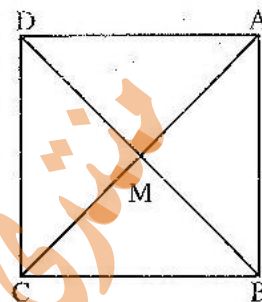


[b] In the opposite figure :

ABCD is a square , whose diagonals

inteseect at M. Find the image of $\triangle MAB$

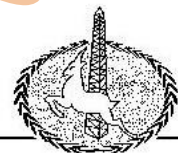
By rotation about M with angle of measure (-90°)



15

Matrouh Governorate

Maths Supervision



Answer the following questions :

1 Complete the following :

- (1) In the right-angled triangle , area of the square drawn on the hypotenuse equals
- (2) The reflection in a line reserves,
- (3) * The measure of the exterior angle of a triangle is equal to the sum of
- (4) The sum of the measures of the accumulative angles at a point is equal to
- (5) The neutral rotation maps the figure to

2 Choose the correct answer from those given :

- (1) The image of the point $(1, -4)$ by reflection in y-axis is
 (a) $(-1, -4)$ (b) $(4, 1)$ (c) $(-1, 4)$ (d) $(-4, -1)$
- (2) The length of a line segment joining the midpoints of two sides of a triangle is equal to the length of the third side.
 (a) quarter (b) half (c) third (d) double
- (3) The diagonals which are equal in the length and perpendicular in
 (a) square. (b) rhombus. (c) rectangle. (d) parallelogram.
- (4) The image of the point $(5, -3)$ by translation 3 units in negative direction of X-axis is
 (a) $(-2, -6)$ (b) $(2, -3)$ (c) $(0, -6)$ (d) $(-6, -2)$
- (5) The triangle ABC is right-angled at B , where $AB = 6$ cm. , $BC = 8$ cm. , then $AC =$
 (a) 14 cm. (b) 2 cm. (c) 10 cm. (d) 6 cm.
- (6) * If the measure of an interior angle of a regular polygon is 135° , then the number of its sides is
 (a) 6 (b) 4 (c) 7 (d) 8

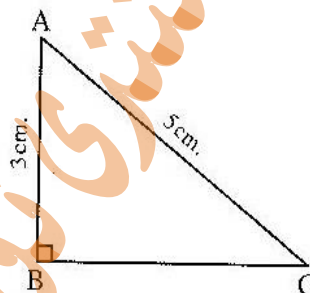
3 [a] Complete : Rotation in a plane reserve,

[b] ABC is a right-angled triangle at B

If $AB = 3$ cm.

, $AC = 5$ cm.

Find : the length of \overline{BC}



4 [a] On a square lattice , draw the image of square ABDC where :

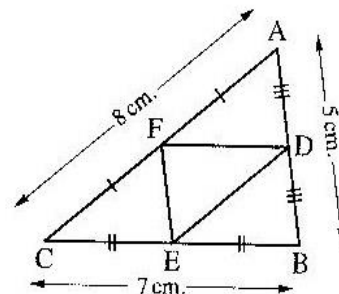
$A(1, 2)$, $B(-2, 2)$, $C(1, 5)$, $D(-2, 5)$ by reflection in the y-axis.

[b] ABC is a triangle , D , E and F are

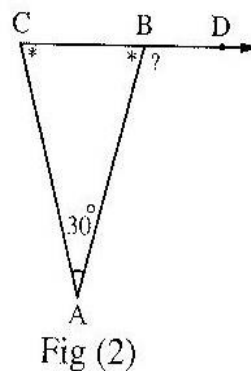
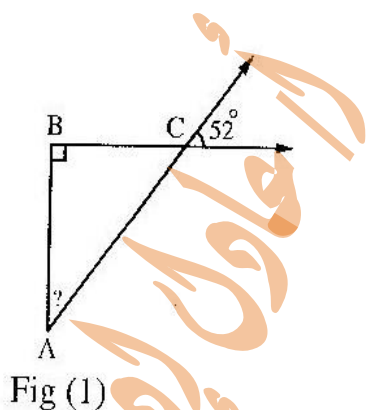
the midpoint of \overline{AB} , \overline{BC} , \overline{CA} respectively

where $AB = 5$ cm. , $BC = 7$ cm. , $CA = 8$ cm.

Calculate the perimeter of $\triangle DEF$



5 [a] In the following figures , find the measure of the angle marked by (?)



[b] On a square lattice , draw the triangle ABC where $A(4, 4)$, $B(4, 2)$, $C(1, 2)$, then find its image by rotation about the origin point with an angle of measure 180°

Model Examinations of the School Book



on Geometry and Measurement

Model 1

Answer the following questions :

1 Choose the correct answer from those given :

- 1 Circumference of a circle of radius 7 cm. = cm.

$$(\pi = \frac{22}{7})$$

- (a) 11 (b) 22 (c) 44 (d) 88

- 2 The image of the point $(-1, 3)$ by translation $(4, -2)$ is

- (a) $(3, 1)$ (b) $(3, -1)$ (c) $(5, 1)$ (d) $(5, -5)$

- 3 The measure of the exterior angle of the equilateral triangle is

- (a) 30° (b) 45° (c) 60° (d) 120°

- 4 In a parallelogram if the adjacent sides are equal in the length, then the shape is

- (a) square. (b) rhombus. (c) rectangle. (d) trapezium.

- 5 The number of the diagonals of a pentagon is

- (a) 3 (b) 5 (c) 7 (d) 9

- 6 The number of axes of symmetry of an isosceles triangle =

- (a) zero (b) 1 (c) 2 (d) 3

2 Complete the following :

- 1 The image of the point $(2, 1)$ by reflection in X-axis is

- 2 In the opposite figure :

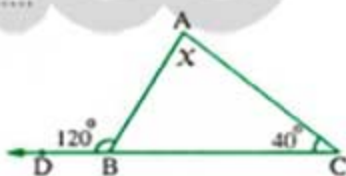
$$x = \dots\dots\dots^\circ$$

- 3 XYZ is a triangle in which $m(\angle Y) = 90^\circ$, $XY = 3$ cm.

, $XZ = 5$ cm. , then $YZ = \dots\dots\dots$ cm.

- 4 ABCD is a parallelogram in which $m(\angle A) = 100^\circ$, then $m(\angle B) + m(\angle D) = \dots\dots\dots^\circ$

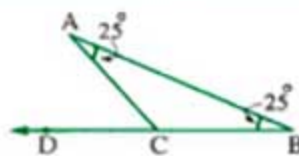
- 5 The sum of the measures of the interior angles of a triangle =



3 [a] In the opposite figure :

$$m(\angle A) = m(\angle B) = 25^\circ$$

Find : $m(\angle ACD)$



- [b] Draw a triangle ABC in which $AB = 5$ cm. , $AC = 3$ cm. and $m(\angle A) = 40^\circ$
 , then draw \hat{C} is the image of C under rotation $R(A, 40^\circ)$, \hat{B} is the image
 of B under rotation $R(A, -40^\circ)$

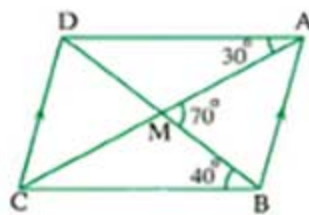
4 [a] In the opposite figure :

$$\overline{AB} \parallel \overline{DC}, \overline{AC} \cap \overline{BD} = \{M\},$$

$$m(\angle DAC) = 30^\circ, m(\angle DBC) = 40^\circ$$

$$\text{and } m(\angle AMB) = 70^\circ$$

Prove that : ABCD is a parallelogram.



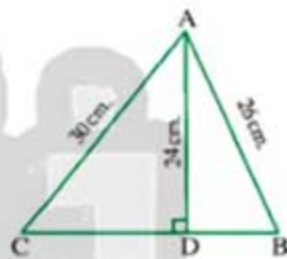
- [b] Use the translation : $(x, y) \longrightarrow (x + 2, y + 3)$
 to find the point whose image is $(2, 3)$

5 [a] In the opposite figure :

$$\overline{AD} \perp \overline{BC}, \text{ if } AD = 24 \text{ cm. , } AB = 26 \text{ cm. , } AC = 30 \text{ cm.}$$

1 Find : The length of \overline{BC}

2 Find : The area of $\triangle ABC$



[b] In the opposite figure :

$$ABCD \text{ is a square , } E \in \overline{BC}, \overline{AC} \parallel \overline{DE}$$

Prove that : ACED is a parallelogram.



Model 2

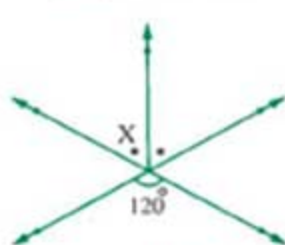
Answer the following questions :

1 Choose the correct answer from those given :

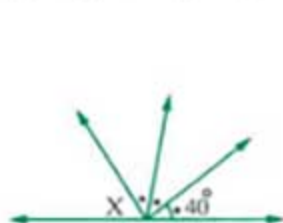
- 1 ABC is a right-angled triangle at B , $AB = 6$ cm. , $BC = 8$ cm. , then $AC = \dots\dots\dots$ cm.
 (a) 10 (b) 28 (c) 100 (d) 160
- 2 The measure of each angle of regular hexagon equals
 (a) 60° (b) 108° (c) 120° (d) 135°
- 3 The two diagonals are equal in length and not perpendicular in
 (a) parallelogram. (b) rectangle. (c) rhombus. (d) square.

Geometry and Measurement

- 4 In all the following shapes $m(\angle X) = 60^\circ$ except the shape



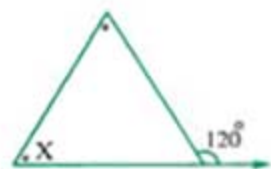
(a)



(b)



(c)



(d)

- 5 In the opposite figure :

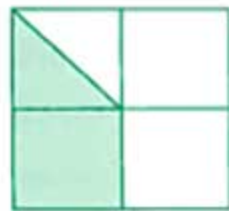
The area of the shaded part from the area of all shape equals

(a) $\frac{1}{8}$

(b) $\frac{1}{4}$

(c) $\frac{3}{8}$

(d) $\frac{3}{4}$



- 6 In the opposite figure :

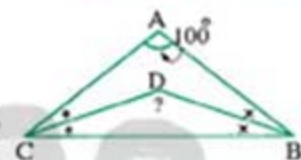
$m(\angle BDC) = \dots\dots\dots^\circ$

(a) 60

(b) 80

(c) 100

(d) 140



- 2 Complete the following :

- 1 In the opposite figure :

Semicircle of diameter 14 cm. and two semicircles the diameter of each is 7 cm.

, then the perimeter of the figure equals cm. $(\pi = \frac{22}{7})$

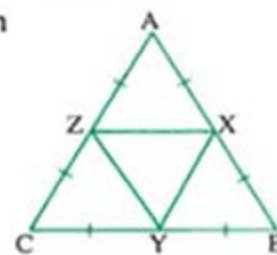


- 2 The image of the point (2, 3) by translation \overrightarrow{MN} , in direction \overrightarrow{MN} , where M (2, -1), N (5, 1) is
- 3 The volume of a cube of side length 1.2 m. = cm^3 .
- 4 The ray drawn parallel to one side of a triangle and passing through the midpoint of another side

- 5 In the opposite figure :

The image of the triangle XBY

by translation \overrightarrow{XZ} in direction \overrightarrow{XZ} is



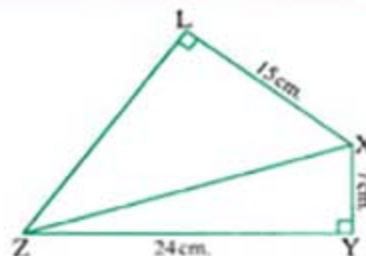
- 3 [a] In the opposite figure :

XYZL is a quadrilateral in which

$m(\angle Y) = m(\angle L) = 90^\circ$, $XY = 7$ cm. ,

$YZ = 24$ cm. , $XL = 15$ cm.

Find : The length of each of \overline{XZ} and \overline{LZ}



- [b] Using the square lattice, draw \overline{AB} where $A(4, 3)$, $B(-1, 1)$
then find the image of \overline{AB} by translation $(X, y) \rightarrow (X+2, y-1)$

- 4 [a] Draw the image of triangle ABC where $A(1, 1)$, $B(3, 4)$, $C(5, 2)$
by reflection in X-axis.

- [b] In the opposite figure :

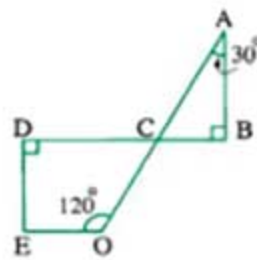
\overline{AB} and \overline{ED} are perpendicular to \overline{BD}

$$\overline{BD} \cap \overline{AO} = \{C\},$$

$$m(\angle A) = 30^\circ$$

$$m(\angle EOC) = 120^\circ,$$

Find : $m(\angle E)$

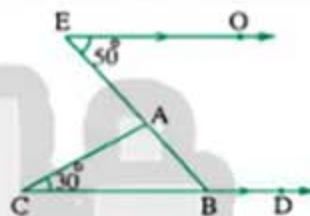


- 5 [a] In the opposite figure :

$$\overline{EO} \parallel \overline{CD}, m(\angle E) = 50^\circ$$

$$m(\angle C) = 30^\circ,$$

Find the measures of angles of $\triangle ABC$, $m(\angle ABD)$



- [b] In the opposite figure :

X is the midpoint of \overline{AB}

$$Y \in \overline{CD}, Z \in \overline{CE}$$

$$\overline{AD} \parallel \overline{XY} \parallel \overline{BC}, \overline{YZ} \parallel \overline{DE}$$

Is $CZ = ZE$? giving reason



Model examination for the merge students

Answer the following questions :

1 Choose the correct answer :

- 1 The sum of the measures of the interior angles of a triangle =°
 (a) 90 (b) 360 (c) 180 (d) 540
- 2 The image of the point (3, -2) by reflection in the y-axis is the point
 (a) (3, 2) (b) (-3, -2) (c) (-3, 2) (d) (-2, 3)
- 3 The diagonals are equal and perpendicular in
 (a) rhombus. (b) square. (c) rectangle. (d) parallelogram.

4 In the opposite figure :

AC = cm.

- (a) 5 (b) 7
 (c) 25 (d) 625

5 In the opposite figure :

 $m(\angle ACD) = \dots\dots\dots^\circ$

- (a) 40 (b) 140
 (c) 90 (d) 50

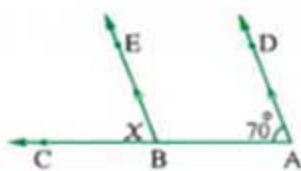


2 Complete each of the following :

- 1 The length of the line segment that joins two midpoints of two sides of a triangle equals the length of the third side.
- 2 The rectangle is a parallelogram in which one of its angles is
- 3 The length of the side of a rhombus whose perimeter is 24 cm. equals cm.
- 4 The image of the point A (-3, 2) by reflection in the origin point is the point \hat{A} (..... ,)

5 In the opposite figure :

$$x = \dots\dots\dots^\circ$$



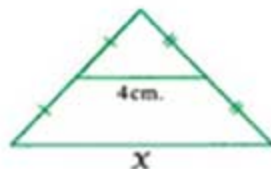
3 Put (✓) or (X) :

- 1 The image of the point (4 , 3) by reflection in the X-axis is the point (3 , - 4) ()
- 2 If ABC is a right-angled triangle at B , then $(AB)^2 = (BC)^2 + (AC)^2$ ()
- 3 The pentagon has 5 diagonals. ()
- 4 ABCD is a parallelogram , in which $m(\angle A) = 70^\circ$, then $m(\angle C) = 110^\circ$ ()
- 5 Any triangle contains at least two acute angles. ()

4 Join from the column (A) to the suitable in the column (B) :

Column (A)	Column (B)
1 The sum of the measures of the interior angles of a quadrilateral =	• 120°
2 The measure of each angle of a regular hexagon =	• 360°
3 The image of the point (3 , 2) by translation (1 , - 2) is the point	• (- 1 , - 3)
4 The image of the point (1 , 3) by rotation about the origin point , of angle of measure 180° is the point (..... ,)	• 45
5 The diagonal of the square divides the angle of the vertex into two angles , the measure of each =°	• (4 , 0)

5 Find the value of X :



$$X = \dots\dots\dots \text{ cm.}$$

Fig. (1)



$$X = \dots\dots\dots^\circ$$

Fig. (2)

Schools Examinations

on Geometry and
Measurement

1

Cairo Governorate

East Nahr City Zone
Manaret Heliopolis School

Answer the following questions :

1 Complete :

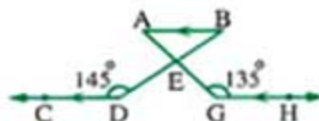
- The sum of measures of the exterior angles of the heptagon is°
- If two lines intersect , then each two vertically opposite angles are
- In $\triangle ABC$, if $m(\angle A) + m(\angle C) = m(\angle B)$, then $m(\angle B) = \dots\dots\dots^\circ$
- The image of $(2, 3)$ by translation $(X, y) \rightarrow (X + 4, y - 2)$ is
- The length of the line segment joining two midpoints of two sides of a triangle equals the length of the third side.

2 Choose the correct answer :

- ABCD is a parallelogram in which $m(\angle A) = 80^\circ$, then $m(\angle C) = \dots\dots\dots$
(a) 80° (b) 100° (c) 120° (d) 60°
- If the image of the point $(5, -3)$ by rotation about the origin point is itself , then the measure of the rotation angle is°
(a) 90 (b) 180 (c) 270 (d) 360
- The line segment joining two midpoints of two sides of a triangle is the third side.
(a) intersecting (b) parallel to (c) perpendicular to (d) congestive
- The sum of measures of the accumulative angles at a point is°
(a) 90 (b) 180 (c) 270 (d) 360
- If ABC is a right-angled triangle at B and $AB = 4$ cm. , $BC = 3$ cm. , then $AC = \dots\dots\dots$ cm.
(a) 16 (b) 25 (c) 9 (d) 5
- The sum of measures of the interior angles of a hexagon is°
(a) 360 (b) 540 (c) 720 (d) 120

3 [a] In the opposite figure :

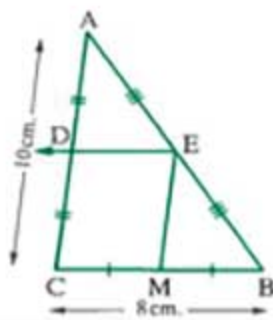
ABE is a triangle , $\overline{AB} \parallel \overline{GH} \parallel \overline{CD}$, $m(\angle CDB) = 145^\circ$
 $m(\angle AGH) = 135^\circ$
 Calculate : $m(\angle DEG)$



[b] In the opposite figure :

ABC is a triangle in which E , M and D are the midpoints of the sides \overline{AB} , \overline{BC} and \overline{CA} respectively , $BC = 8$ cm. , $AC = 10$ cm.

Prove that : DEMC is a parallelogram.

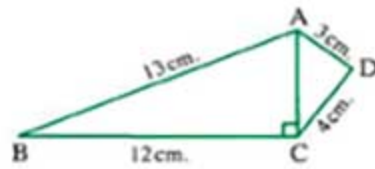


4 [a] In the opposite figure :

$m(\angle ACB) = 90^\circ$, $AB = 13$ cm. , $AD = 3$ cm. , $CD = 4$ cm. , $BC = 12$ cm.

Find : 1 The length of \overline{AC}

2 The perimeter of the figure ABCD

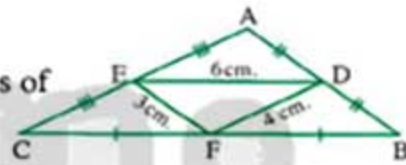


[b] In the opposite figure :

ABC is a triangle in which : D , F and E are the midpoints of \overline{AB} , \overline{BC} and \overline{CA}

respectively such that : $DF = 4$ cm. , $FE = 3$ cm. , $DE = 6$ cm.

Calculate : The perimeter of $\triangle ABC$



5 [a] Using the lattice , find the images of the points :

A (-4 , 1) , B (0 , 4) and C (-2 , 2) by reflection in X-axis.

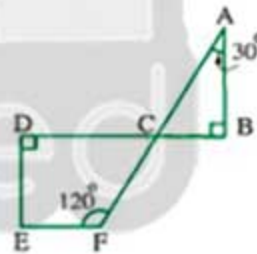
[b] In the opposite figure :

$\overline{AB} \perp \overline{BC}$, $\overline{BD} \cap \overline{AF} = \{C\}$

, $m(\angle A) = 30^\circ$, $m(\angle F) = 120^\circ$

Find with proof : 1 $m(\angle ACB)$

2 $m(\angle E)$



2

Cairo Governorate

Abdeen Directorate
Patriarchal College

Answer the following questions :

1 Choose the correct answer :

1 The sum of the measures of the interior angles of the pentagon equals°

(a) 360 (b) 540 (c) 720 (d) 108

2 The two diagonals are equal in length and perpendicular in the

(a) parallelogram (b) rectangle (c) rhombus (d) square

Geometry and Measurement

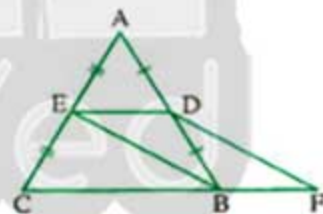
- 3 The image of the point $(4, -7)$ by reflection in X-axis is
 (a) $(4, 7)$ (b) $(-4, -7)$ (c) $(-4, 7)$ (d) $(4, -7)$
- 4 The line segment joining the midpoints of two sides of a triangle is the third side.
 (a) parallel to (b) perpendicular to (c) bisect to (d) equal to
- 5 In $\triangle ABC$, if $m(\angle B) = 90^\circ$, $AB = 6$ cm. and $BC = 8$ cm., then $AC =$ cm.
 (a) 100 (b) 8 (c) 14 (d) 10
- 6 The image of the point $(-3, 4)$ by rotation about the origin with an angle of measure 90° is
 (a) $(-4, 3)$ (b) $(3, -4)$ (c) $(-4, -3)$ (d) $(4, 3)$

2 Complete :

- 1 A quadrilateral in which only two opposite sides are parallel is called
- 2 The measure of each angle of the regular octagon equals°
- 3 The image of the point $(1, -5)$ by translation $(-4, 6)$ is
- 4 If the measure of each interior angle of a regular polygon is 140° , then the number of its sides is
- 5 ABCD is a parallelogram in which $m(\angle A) + m(\angle C) = 100^\circ$, $m(\angle B) =$ °

3 [a] In the opposite figure :

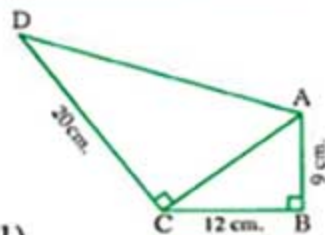
D and E are the midpoints of \overline{AB} and \overline{AC} respectively
 $F \in \overline{CB}$, where $BF = \frac{1}{2} CB$
 Prove that : DFBE is a parallelogram.



- [b] Draw the image of $\triangle XYZ$ in which $XY = 3$ cm., $YZ = 5$ cm. and $ZX = 7$ cm.
 by reflection in the straight line containing the longest side.

4 [a] In the opposite figure :

$m(\angle B) = m(\angle ACD) = 90^\circ$
 $AB = 9$ cm., $BC = 12$ cm. and $CD = 20$ cm.
 Find by proof : The length of each of \overline{AC} and \overline{AD}



- [b] In the square lattice draw $\triangle ABC$ where : $A(-4, 2)$, $B(-1, 1)$
 and $C(-2, 5)$, then draw its image by
 the translation : $(x, y) \rightarrow (x + 5, y - 3)$

5 [a] In the opposite figure :

$$\overline{DC} \cap \overline{BE} = \{O\}, m(\angle A) = 85^\circ$$

$$, m(\angle D) = 100^\circ, m(\angle E) = 35^\circ \text{ and } m(\angle C) = 50^\circ$$

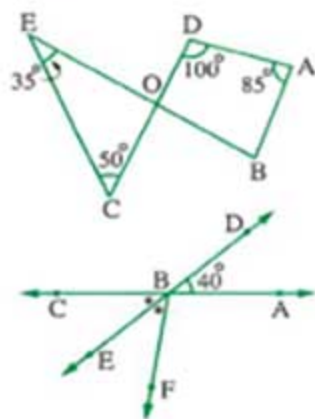
Find : $m(\angle B)$

[b] In the opposite figure :

$$\overline{AC} \cap \overline{DE} = \{B\}, m(\angle ABD) = 40^\circ$$

, \overline{BE} bisects $\angle CBF$

Find : $m(\angle ABF)$



3

Cairo Governorate

Hedayek El Koba Educational Zone



Answer the following questions : (Calculators are Permitted)

1 Choose the correct answer :

- 1 The measure of the interior angle of the regular octagon equals
 (a) 1080° (b) 180° (c) 135° (d) 108°
- 2 If ABCD is a parallelogram in which $m(\angle A) + m(\angle C) = 140^\circ$, then $m(\angle B) =$
 (a) 40° (b) 110° (c) 70° (d) 60°
- 3 In $\triangle ABC$, if $m(\angle B) = 90^\circ$, $AB = 20$ cm., $AC = 25$ cm., then $BC =$ cm.
 (a) 625 (b) 12 (c) 15 (d) 225
- 4 If the perimeter of a square is 20 cm., then its area equals cm^2
 (a) 25 (b) 100 (c) 5 (d) 16
- 5 The image of point $(-3, 5)$ by rotation about origin point with an angle of measure 90° is
 (a) $(-5, 3)$ (b) $(-5, -3)$ (c) $(5, 3)$ (d) $(3, -5)$
- 6 The image of point $(-1, 3)$ by translation $(4, -2)$ is
 (a) $(3, 1)$ (b) $(3, -1)$ (c) $(5, 1)$ (d) $(5, -5)$

2 Complete the following :

- 1 The line segment joining the midpoints of two sides of a triangle is parallel to
- 2 The image of the point $(2, -4)$ by reflection in y-axis is
- 3 The number of axis of symmetry of a rectangle is

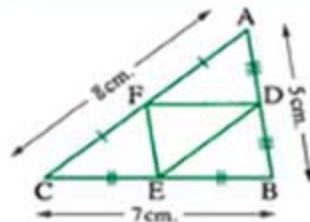
Geometry and Measurement

- 4 The measure of exterior angle of an equilateral triangle equals°
 5 The volume of a cube of side length 6 cm. is cm³.

3 [a] In the opposite figure :

ABC is a triangle , D , E and F are midpoints
 of \overline{AB} , \overline{BC} , \overline{CA} respectively
 where $AB = 5$ cm. , $BC = 7$ cm. and $CA = 8$ cm.

Calculate : The perimeter of $\triangle DEF$

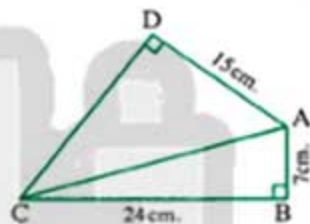


- [b] On square lattice , draw the square ABCD where A (1 , 2) , B (-2 , 2) , C (-2 , 5) and D (1 , 5) , then draw its image by reflection in X-axis.

4 [a] In the opposite figure :

$m(\angle B) = m(\angle D) = 90^\circ$
 $AD = 15$ cm. , $AB = 7$ cm. and $BC = 24$ cm.

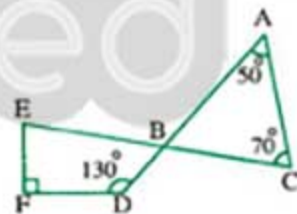
Find : The length of each of \overline{AC} , \overline{DC}



- [b] Draw $\triangle ABC$ where A (1 , 5) , B (3 , 1) and C (5 , 3) , then draw its image by rotation about the origin point with an angle of measure 180°

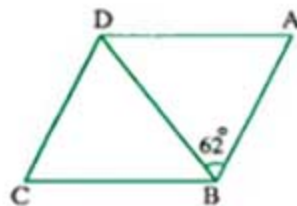
5 [a] In the opposite figure :

$\overline{CE} \cap \overline{AD} = \{B\}$
 $m(\angle A) = 50^\circ$, $m(\angle C) = 70^\circ$
 $m(\angle D) = 130^\circ$ and $m(\angle F) = 90^\circ$
 Find : $m(\angle E)$



[b] In the opposite figure :

ABCD is a rhombus
 \overline{BD} is a diagonal in it
 $m(\angle ABD) = 62^\circ$
 Find with proof : $m(\angle A)$



4

Giza Governorate

El-Haram Zone
Hefr El-Baten Language School British Academy

Answer the following questions :

1 Choose the correct answer :

- 1 The measure of each angle of the regular pentagon equals
(a) 100° (b) 120° (c) 108° (d) 110°
- 2 The sum of measures of accumulative angles at a point equals
(a) 90° (b) 100° (c) 360° (d) 180°
- 3 Any triangle has at least two angles.
(a) acute (b) obtuse (c) right (d) reflex
- 4 ABCD is a parallelogram in which $m(\angle A) = 70^\circ$, then $m(\angle B) = \dots\dots\dots^\circ$
(a) 70 (b) 110 (c) 90 (d) 180
- 5 $(-4, 5)$ is the image of $(5, 4)$ by rotation in the origin point with an angle of measure
(a) 90° (b) -90° (c) 180° (d) 360°
- 6 The image of the point $(-2, 2)$ by a translation of magnitude 3 units in the positive direction of y-axis is
(a) $(-1, 2)$ (b) $(-2, 5)$ (c) $(-1, 5)$ (d) $(1, 5)$

2 Complete the following :

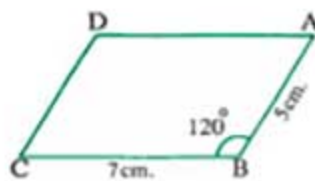
- 1 The sum of measures of the interior angles of any triangle equals
- 2 Each two opposite angles of a parallelogram are
- 3 The length of the line segment joining the midpoint of two sides of a triangle is equal to the length of the third side.
- 4 The image of the point $(3, -5)$ by rotation 360° about the origin point is
- 5 The image of $(-3, 0)$ by reflection in the y-axis is

3 [a] A regular hexagon of side length 15 cm.

Find : 1 its perimeter.

2 the measure of each angle.

[b] In the opposite figure :

ABCD is a parallelogram , $\overline{AB} = 5$ cm., $BC = 7$ cm. , $m(\angle B) = 120^\circ$ Find : $m(\angle C)$, $m(\angle D)$, the length of each of \overline{AD} and \overline{DC} 

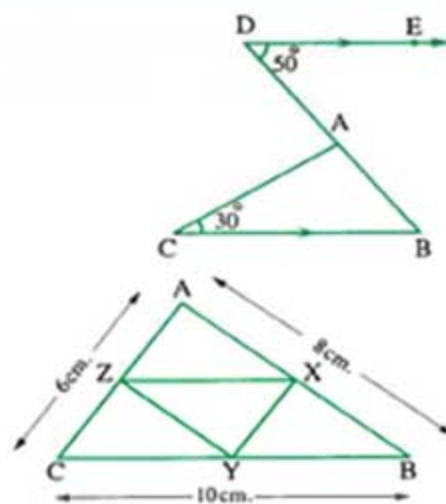
Geometry and Measurement

4 [a] In the opposite figure :

 $\overline{DE} \parallel \overline{BC}$, $m(\angle D) = 50^\circ$ $m(\angle C) = 30^\circ$ Find : $m(\angle B)$ and $m(\angle BAC)$

[b] In the opposite figure :

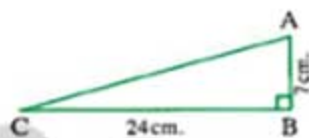
X , Y and Z

are the midpoints of \overline{AB} , \overline{BC} and \overline{AC} respectively $AB = 8 \text{ cm}$, $AC = 6 \text{ cm}$, $BC = 10 \text{ cm}$.Find : The perimeter of $\triangle XYZ$ 

5 [a] In the opposite figure :

 $m(\angle B) = 90^\circ$, $AB = 7 \text{ cm}$. $BC = 24 \text{ cm}$.Find : The length of \overline{AC}

[b] Draw ABC in which A (1 , 1) , B (5 , 1) and C (3 , 3) , then find its image by reflection in y-axis.



5

Giza Governorate

Experimental Schools
Math Inspector

Answer the following questions :

1 Complete the following :

- The image of the point (5 , -3) under rotation of angle of measure 90° about the origin point is
- The ray which is drawn from the midpoint of a side in a triangle parallel to another side the third side.
- In the rhombus the two diagonals are
- The sum of measures of the exterior angles of any convex polygon equals°
- In $\triangle ABC$, if $m(\angle A) + m(\angle B) = m(\angle C)$, then $\triangle ABC$ is

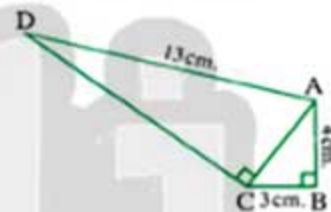
2 Choose the correct answer :

- If the measure of an interior angle of a regular polygon is 135° , then the number of its sides is
(a) 6 (b) 4 (c) 7 (d) 8

- 2 The image of the point $(-1, 4)$ by the translation $(x, y) \rightarrow (x + 3, y - 2)$ followed by reflection in the x -axis is
- (a) $(2, 2)$ (b) $(-2, 2)$ (c) $(-2, -2)$ (d) $(2, -2)$
- 3 ABCD is a parallelogram in which $m(\angle A) + m(\angle C) = 110^\circ$, then $m(\angle B) = \dots\dots\dots$
- (a) 125° (b) 80° (c) 100° (d) 110°
- 4 The concave polygon should have angle.
- (a) an acute (b) a right (c) an obtuse (d) a reflex
- 5 The image of the point is itself by reflection in y -axis.
- (a) $(0, 3)$ (b) $(3, 0)$ (c) $(3, 3)$ (d) $(-3, 3)$
- 6 The identity rotation about the origin point with an angle of measure°
- (a) 90 (b) 180 (c) 360 (d) -90

3 [a] In the opposite figure :

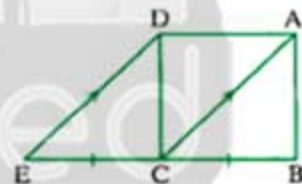
ABCD is a quadrilateral in which
 $m(\angle B) = m(\angle ACD) = 90^\circ$
 $AB = 4$ cm, $BC = 3$ cm, and $AD = 13$ cm.
 Find : AC and DC



[b] In the opposite figure :

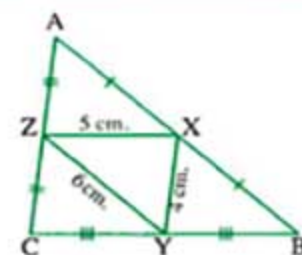
ABCD is a square, $E \in \overline{BC}$
 such that $BC = CE$

- 1 Prove that : The figure ACED is a parallelogram.
 2 Find : $m(\angle E)$



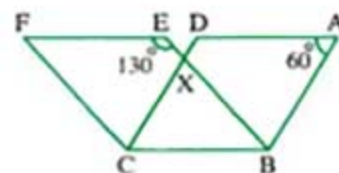
4 [a] In the opposite figure :

$\triangle ABC$ in which X, Y and Z are the midpoints of
 \overline{AB} , \overline{BC} , \overline{CA} respectively
 $XZ = 5$ cm, $XY = 4$ cm, $YZ = 6$ cm.
 Find with proof : The perimeter of $\triangle ABC$



[b] In the opposite figure :

ABCD and EBCF are two parallelograms
 $m(\angle BAD) = 60^\circ$, $m(\angle BEF) = 130^\circ$
 Find with proof : $m(\angle BXC)$



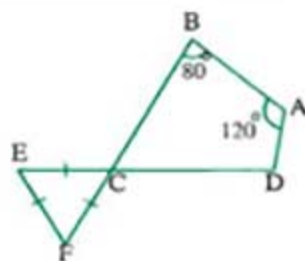
Geometry and Measurement

5 [a] In the opposite figure :

ABCD is a quadrilateral in which $m(\angle A) = 120^\circ$

, $m(\angle B) = 80^\circ$, $\triangle CEF$ is an equilateral triangle

Find : $m(\angle D)$

[b] Using the square lattice draw $\triangle ABC$ where :

A (2 , 4) , B (4 , 2) and C (3 , 1) , then map its image by the translation

$(X, y) \rightarrow (X + 2, y + 3)$

6

Alexandria Governorate

East Educational Zone
Math's Supervision (A)



Answer the following questions :

1 Complete each of the following :

- The angle whose measure is 89° is angle.
- The length of the line segment that joins two midpoints of two sides of a triangle equals
- The area of one face of a cube is 25 cm^2 then its volume equals cm^3 .
- The image of the point (2 , 1) by reflection in X-axis is
- In the parallelogram XYZL , if $m(\angle X) = \frac{1}{2} m(\angle Y)$, then $m(\angle Y) = \dots\dots\dots$

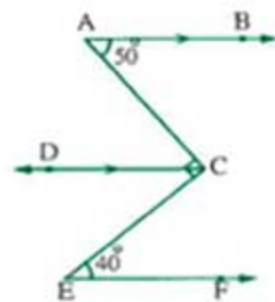
2 Choose the correct answer from those given :

- The supplementary of the angle whose measure is 30° is an angle of measure
(a) 30 (b) 60 (c) 120 (d) 150
- The number of the diagonals of a pentagon is
(a) 3 (b) 5 (c) 7 (d) 9
- The image of the point (- 1 , 3) by translation (4 , - 2) is
(a) (3 , 1) (b) (3 , - 1) (c) (5 , 1) (d) (5 , - 5)
- The sum of the measures of the interior angles of the triangle equals
(a) 90 (b) 360 (c) 180 (d) 540
- ABC is right-angled triangle at B , AB = 6 cm. , BC = 8 cm. , then AC = cm.
(a) 10 (b) 28 (c) 100 (d) 160
- The measure of the exterior angle of the equilateral triangle is
(a) 30 (b) 45 (c) 60 (d) 120

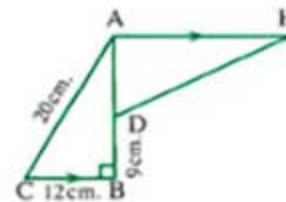
Final Examinations

- 3 [a] In the opposite figure :

$\overline{AB} \parallel \overline{CD}$, $m(\angle A) = 50^\circ$

 $\angle ACE$ is right angle and $m(\angle E) = 40^\circ$ Prove that : $\overline{AB} \parallel \overline{EF}$ 

- 4 [a] In the opposite figure :

ABC is a triangle , $m(\angle B) = 90^\circ$ $\overline{AE} \parallel \overline{BC}$, if $BC = 12$ cm. , $AC = 20$ cm. $D \in AB$ where $BD = 9$ cm. and $AE = 2 BC$ Find : The length of each of \overline{AD} , \overline{ED} 

- [b] Using square lattice , draw
- ΔABC
- , where :

A (-2 , 4) , B (5 , 0) , C (3 , -3)

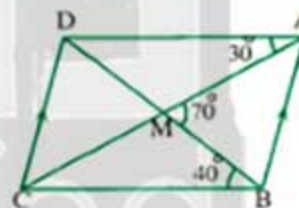
, then draw the reflected image of ΔABC in the origin point.

- 5 [a] In the opposite figure :

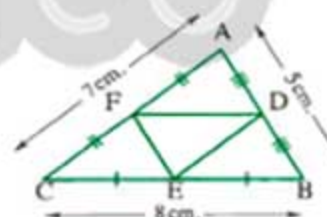
$\overline{AB} \parallel \overline{DC}$, $\overline{AC} \cap \overline{BD} = \{M\}$

 $m(\angle DAC) = 30^\circ$, $m(\angle DBC) = 40^\circ$ and $m(\angle AMB) = 70^\circ$

Prove that : ABCD is a parallelogram



- [b] In the opposite figure :

 $AB = 5$ cm. , $BC = 8$ cm. , $AC = 7$ cm. D , E and Fare the midpoints of \overline{AB} , \overline{BC} and \overline{CA} respectively.Calculate : The perimeter of ΔDEF 

7

Alexandria Governorate

Middle Educational Zone
Math's Supervision

Answer the following questions :

- 1 Complete each of the following :

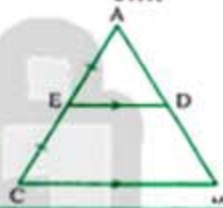
- The measure of the straight angle equals
- The image of the point (4 , -2) by reflection in X-axis is

Geometry and Measurement

- 3 The ray drawn from the midpoint of a side parallel to another side in a triangle
- 4 The image of the point $(-2, 1)$ by rotation with an angle of measure 180° about origin point is
- 5 The length of line segment joining the midpoints of two sides of a triangle equals
- 6 A rhombus is a with two adjacent equal sides in length.

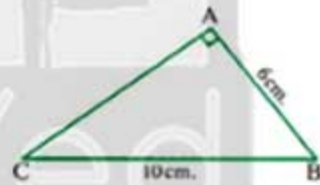
2 Choose the correct answer :

- 1 The perimeter of a square with side length 1 cm. equals cm.
(a) 5 (b) 1 (c) 4 (d) 2
- 2 The number of diagonals in a pentagon is
(a) 0 (b) 3 (c) 4 (d) 5
- 3 The edge length of a cube whose volume is 27 cm^3 is cm.
(a) 9 (b) 3 (c) 27 (d) 6
- 4 In $\triangle ABC$, if $m(\angle B) = 90^\circ$, $AB = 3 \text{ cm}$, $BC = 4 \text{ cm}$, then $AC = \dots\dots\dots \text{ cm}$.
(a) 7 (b) 12 (c) 1 (d) 5
- 5 In the opposite figure : $CB : ED = \dots\dots\dots$
(a) 1 : 1 (b) 1 : 2 (c) 2 : 1 (d) 1 : 4



3 [a] In the opposite figure :

ABC is a right-angled triangle at A
 $BC = 10 \text{ cm}$, $AB = 6 \text{ cm}$.
 Find : The length of \overline{AC}

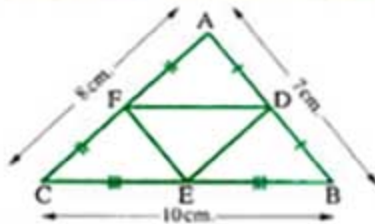


- [b] Draw the image of the rectangle XYZL where $X(-5, 1)$, $Y(-5, 4)$, $Z(-1, 4)$, $L(-1, 1)$ by reflection in the X-axis.

4 [a] In the opposite figure :

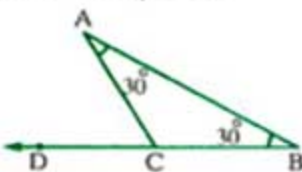
$BC = 10 \text{ cm}$, $AB = 7 \text{ cm}$, $AC = 8 \text{ cm}$.
 Calculate : The perimeter of the $\triangle FDE$

- [b] The ratio between the measures of the angles of a quadrilateral is $2 : 2 : 3 : 5$
 Calculate : The measure of the biggest angle.

5 [a] Find the image of the point A $(5, -5)$ by translation $(X, y) \rightarrow (X - 2, y - 3)$

[b] In the opposite figure :

$m(\angle A) = m(\angle B) = 30^\circ$
 Find showing steps : $m(\angle ACD)$



8

El-Kalyoubia Governorate

Directorate of Education
Central Maths Supervision

Answer the following questions :

1 Choose the correct answer :

1 If the perimeter of a square is 20 cm. , then the length of its side is cm.

- (a) 3 (b) 5 (c) 7 (d) 9

2 The number of diagonals of a pentagon is

- (a) 3 (b) 5 (c) 7 (d) 9

3 If ABCD is a parallelogram , $m(\angle A) + m(\angle C) = 140^\circ$, then $m(\angle D) = \dots\dots\dots$

- (a)
- 40°
- (b)
- 70°
- (c)
- 180°
- (d)
- 110°

4 The image of the point $(-3, 5)$ by rotation about the origin point by an angle of measure 90° is

- (a)
- $(-3, 5)$
- (b)
- $(5, -3)$
- (c)
- $(-5, -3)$
- (d)
- $(3, -5)$

5 The measure of the exterior angle of the equilateral triangle is

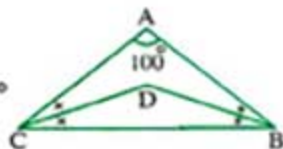
- (a)
- 30°
- (b)
- 45°
- (c)
- 60°
- (d)
- 120°

6 If ABC is a right-angled triangle at B , $AB = 6$ cm. and $BC = 8$ cm. , then $AC = \dots\dots\dots$

- (a) 5 cm. (b) 10 cm. (c) 15 cm. (d) 20 cm.

2 Complete :

1 The number of axis of symmetry of a rectangle equals

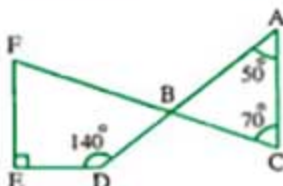
2 The volume of a cube of edge length 0.2 m. equals cm^3 3 The image of $(3, -2)$ by reflection in the y-axis is4 In the opposite figure : $m(\angle BDC) = \dots\dots\dots^\circ$ 5 The measure of each interior angle of a regular hexagon is $^\circ$ 

3 [a] In the opposite figure :

$$\overline{AD} \cap \overline{FC} = \{B\}$$

$$, m(\angle A) = 50^\circ , m(\angle C) = 70^\circ$$

$$, m(\angle D) = 140^\circ , \overline{EF} \perp \overline{ED}$$

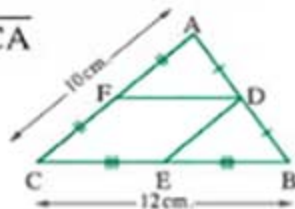
Find : $m(\angle F)$ 

Geometry and Measurement

[b] In the opposite figure :

ABC is a triangle , D , E , F are the midpoints of \overline{AB} , \overline{BC} , \overline{CA} respectively, $BC = 12$ cm. , $AC = 10$ cm.

Find : The perimeter of the quadrilateral DECF

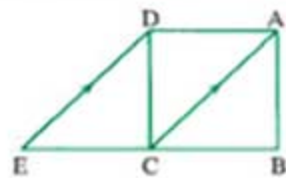


4 [a] In the opposite figure :

ABCD is a square , $E \in \overline{BC}$ and $\overline{AC} \parallel \overline{DE}$

1 Prove that : ACED is a parallelogram.

2 Find : $m(\angle ACE)$



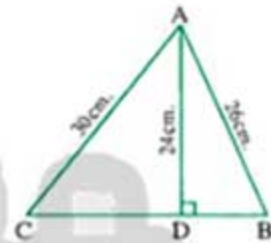
[b] In the opposite figure :

$m(\angle ADB) = 90^\circ$, $AD = 24$ cm.

, $AB = 26$ cm. , $AC = 30$ cm.

Find : 1 The length of \overline{BC}

2 The area of $\triangle ABC$



5 [a] Using square lattice , draw \overline{AB} where $A(4, 3)$, $B(-1, 1)$, then find the image of \overline{AB} by translation $(X, y) \rightarrow (X+2, y-1)$

[b] Draw the image of the triangle ABC where $A(1, 1)$, $B(3, 4)$, $C(5, 2)$ by reflection in X-axis.

9

El-Gharbia Governorate

Official Language Schools
The Central Maths Supervision



Answer the following questions :

1 Choose the correct answer :

1 The measure of the exterior angle of the equilateral triangle equals°

- (a) 30 (b) 45 (c) 60 (d) 120

2 If the image of the point $(5, -3)$ by rotation around the origin point is itself , then the measure of the rotation angle equals°

- (a) 90 (b) 270 (c) 180 (d) 360

3 The image of a square by rotation around the origin point with an angle of measure 90° is a

- (a) rectangle (b) square (c) rhombus (d) trapezium

- 4 Any triangle has at least acute angle.
 (a) 0 (b) 1 (c) 2 (d) 3
- 5 The measure of the interior angle of the regular hexagon equals°
 (a) 60 (b) 108 (c) 120 (d) 135
- 6 The image of the point $(-5, 0)$ by reflection on X-axis is
 (a) $(5, 0)$ (b) $(0, 5)$ (c) $(-5, 0)$ (d) $(0, -5)$

2 Complete :

- 1 The line segment joining the midpoints of two sides of a triangle is
- 2 If ABCD is a parallelogram in which $m(\angle A) = 60^\circ$, then $m(\angle B) = \dots\dots\dots^\circ$
- 3 The image of the point $(3, 2)$ by reflection in the origin point is
- 4 Each two opposite angles in a parallelogram are
- 5 The rectangle is a parallelogram in which one of its angles is

3 [a] In the opposite figure :

$$\overline{AC} \cap \overline{DE} = \{B\}, m(\angle ABD) = 40^\circ$$

and \overline{BE} bisects $\angle CBF$

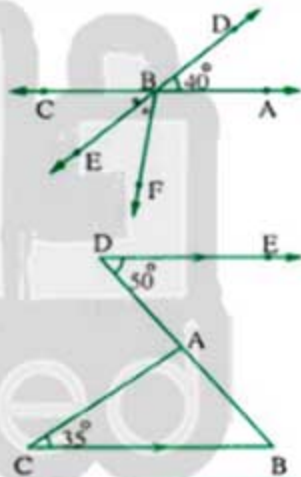
Find with proof : $m(\angle ABF)$

[b] In the opposite figure :

$$\overline{DE} \parallel \overline{CB}, m(\angle D) = 50^\circ, m(\angle C) = 35^\circ$$

Find with proof :

$$m(\angle B), m(\angle BAC)$$



4 [a] In the opposite figure :

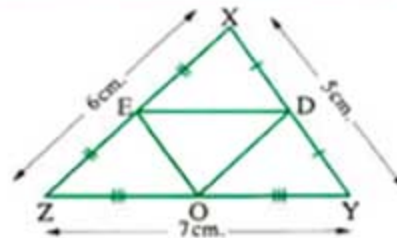
XYZ is a triangle in which $XY = 5$ cm.

, $XZ = 6$ cm. , $YZ = 7$ cm.

Find with proof : The perimeter of $\triangle DOE$

[b] On the square lattice , draw the triangle whose

vertices are $A(4, 4)$, $B(4, 2)$, $C(1, 2)$, then find its image by the translation $(-4, -2)$

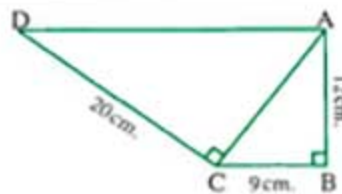


5 [a] In the opposite figure :

$$m(\angle B) = m(\angle ACD) = 90^\circ$$

$$AB = 12 \text{ cm.}, BC = 9 \text{ cm.}, CD = 20 \text{ cm.}$$

Find : The length of \overline{AD}

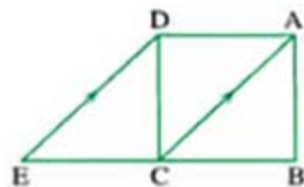


Geometry and Measurement

[b] In the opposite figure :

ABCD is a square , $E \in \overline{BC}$, $\overline{AC} \parallel \overline{DE}$

Prove that : ACED is a parallelogram.



10

El-Dakahlia Governorate

Directorate of Education
Mathe Supervision

Answer the following questions :

1 Choose the correct answer :

- 1 The sum of the measures of an exterior angles of a triangle equals
(a) 90° (b) 180° (c) 270° (d) 360°
- 2 The side length of a rhombus whose perimeter 36 cm. equals
(a) 144 cm. (b) 6 cm. (c) 9 cm. (d) 18 cm.
- 3 The measure of each angle of regular octagon equals
(a) 60° (b) 108° (c) 120° (d) 135°
- 4 The parallelogram whose diagonals are not perpendicular but equal in length is called
(a) rhombus (b) square (c) rectangle (d) trapezium
- 5 The image of the point $(-3, 5)$ by rotation about the origin point with an angle of measure -270° is
(a) $(5, 3)$ (b) $(-5, 3)$ (c) $(3, 5)$ (d) $(-5, -3)$
- 6 The number of the acute angles in any triangle equals at least
(a) zero (b) 1 (c) 2 (d) 3

2 Complete each of the following :

- 1 The measure of any of the exterior angles of an equilateral triangle equals
- 2 If $\triangle ABC$ is right-angled triangle at B , $m(\angle C) = 55^\circ$, then $m(\angle A) = \dots^\circ$
- 3 The parallelogram whose perimeter 32 cm. and the length of one of its sides is 7 cm. , then the length of its adjacent side equals
- 4 If the image of the point $(-5, 4)$ by a translation is $(1, 4)$, then the image of the point $(3, -6)$ by the same translation is
- 5 The rectangle is a parallelogram in which one of its angles is

3 [a] In the opposite figure :

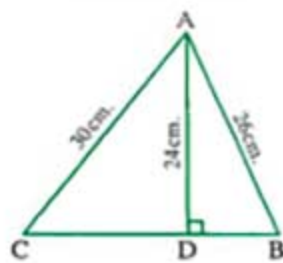
ABC is a triangle in which $D \in \overline{BC}$

, $m(\angle ADB) = 90^\circ$, $AB = 26$ cm.

, $AD = 24$ cm., $AC = 30$ cm.

Find : 1 The length of \overline{BC}

2 The area of the triangle ABC



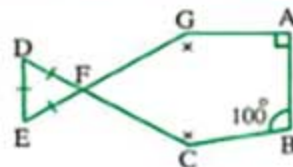
- [b] Draw the image of triangle ABC where $A(2, 2)$, $B(5, 2)$, $C(3, 5)$ by reflection in y-axis.

4 [a] In the opposite figure :

DFE is an equilateral triangle

, $m(\angle A) = 90^\circ$, $m(\angle B) = 100^\circ$, $m(\angle C) = m(\angle G)$

Find : $m(\angle C)$



[b] In the opposite figure :

ABC is a triangle in which D, E are the midpoints of \overline{AB}

, \overline{AC} respectively

, $CB = 12$ cm. and $DX = XF$

Find : The length of \overline{XY}



5 [a] In the opposite figure :

ABCD is a square, $E \in \overline{BC}$, $\overline{AC} \parallel \overline{DE}$

Prove that : ACED is a parallelogram, then find : $m(\angle ACE)$

- [b] Draw $\triangle OBC$ on a square lattice where

$O(0, 0)$, $B(4, 0)$, $C(0, 3)$, then find its image by rotation about the origin point with an angle of measure 180°



11

Suez Governorate

Directorate of Education
Math Supervision

Answer the following questions :

1 Choose the correct answer :

- 1 The two diagonals are equal in length and not perpendicular in a
 (a) parallelogram (b) rectangle (c) square (d) rhombus
- 2 The image of $(1, 3)$ by translation $(4, 2)$ is
 (a) $(3, 1)$ (b) $(5, 5)$ (c) $(5, 1)$ (d) $(5, -5)$

Geometry and Measurement

- 3 The measure of an exterior angle in an equilateral triangle is
 (a) 30° (b) 45° (c) 60° (d) 120°
- 4 In a parallelogram if the two adjacent sides are equal in length, then the shape is a
 (a) square (b) rhombus (c) rectangle (d) trapezium
- 5 The number of axes of symmetry of the equilateral triangle is
 (a) 0 (b) 1 (c) 2 (d) 3
- 6 The sum of measures of the interior angles in a triangle is
 (a) 90 (b) 360 (c) 180 (d) 540

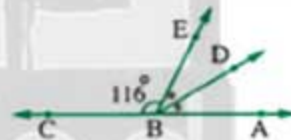
2 Complete :

- 1 In the opposite figure : $m(\angle ACD) = \dots\dots\dots^\circ$
- 2 The ray drawn from the midpoint of one side of a triangle parallel to another side
- 3 The image of the point $(1, -2)$ by reflection in X-axis is
- 4 The sum of measures of the interior angles of the pentagon is $^\circ$
- 5 If ABCD is a rhombus, then \perp



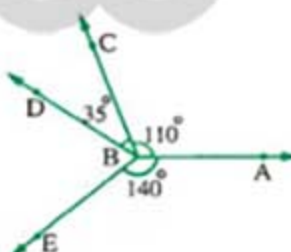
3 [a] In the opposite figure :

$B \in \overline{AC}$, $m(\angle CBE) = 116^\circ$
 \overline{BD} bisects $\angle ABE$
 Find : $m(\angle ABD)$



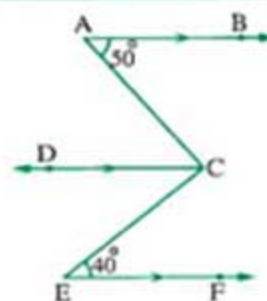
[b] In the opposite figure :

$m(\angle ABC) = 110^\circ$, $m(\angle CBD) = 35^\circ$
 $m(\angle ABE) = 140^\circ$
 Find : $m(\angle DBE)$



4 [a] In the opposite figure :

$\overline{AB} \parallel \overline{CD} \parallel \overline{EF}$
 $m(\angle A) = 50^\circ$, $m(\angle E) = 40^\circ$
 Find by proof : $m(\angle ACE)$

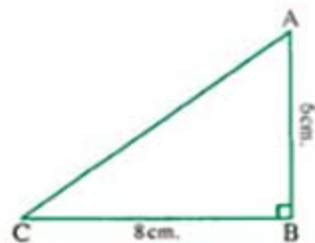


[b] In the opposite figure :

ΔABC is right-angled at B

, $AB = 6$ cm. , $BC = 8$ cm.

Find : The length of \overline{AC}



5 [a] Complete :

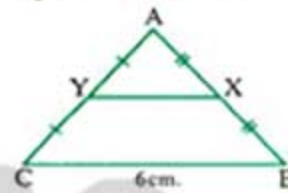
1 The image of (3 , 2) by rotation about the origin point with an angle of measure 90° is

2 The image of (3 , 2) by reflection in the origin point is

3 The image of (3 , 2) by rotation about the origin point with an angle of measure 180° is

4 In the opposite figure :

$XY =$ cm.



[b] In the opposite figure :

\overline{AB} , \overline{DE} are perpendicular to \overline{BD}

, $\overline{BD} \cap \overline{AF} = \{C\}$, $m(\angle A) = 60^\circ$, $m(\angle CFE) = 120^\circ$

Find with proof : $m(\angle E)$



12

Port Said Governorate

East Educational Zone
Math's Supervision

Answer the following questions :

1 Choose the correct answer :

- The image of the point (2 , -5) by reflection in X-axis is
(a) (2 , -5) (b) (2 , 5) (c) (-2 , -5) (d) (5 , 2)
- The measure of each interior angle of a regular hexagon equals
(a) 60° (b) 108° (c) 120° (d) 135°
- The two diagonals are equal in length and not perpendicular in the
(a) parallelogram. (b) rectangle. (c) rhombus. (d) square.
- The sum of the measures of the interior angles of a triangle equals
(a) 90° (b) 180° (c) 270° (d) 360°
- The image of the point (3 , -2) by reflection in the y-axis is the point
(a) (3 , 2) (b) (-3 , -2) (c) (-3 , 2) (d) (-2 , 3)
- The measure of the exterior angle of the equilateral triangle is
(a) 30° (b) 45° (c) 60° (d) 120°

Geometry and Measurement

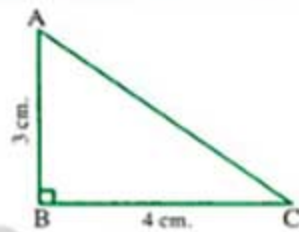
2 Complete each of the following :

- The length of the line segment that joins two midpoints of two sides of a triangle equals the length of the third side.
- The image of the point A $(-3, 2)$ by reflection in the origin point is the point
- The sum of the measures of the angles of a quadrilateral equals°
- If ABCD is a parallelogram in which $m(\angle A) = 60^\circ$, then $m(\angle B) = \dots\dots\dots^\circ$
- The length of the side of a rhombus whose perimeter is 24 cm. equals cm.

3 [a] In the opposite figure :

ABC is a right-angled triangle at B
 $AB = 3$ cm. , $BC = 4$ cm.

Find : The length of \overline{AC}



- [b] On the lattice , find the image of the triangle LMN where L $(-4, -1)$, M $(-1, -3)$, N $(0, -1)$ by reflection in the X-axis.

4 [a] Using the square lattice , draw \overline{AB} where A $(4, 3)$, B $(-1, 1)$, then find the image of \overline{AB} by reflection in the origin point.

[b] In the opposite figure :

$\overline{DC} \parallel \overline{EO}$, $m(\angle D) = 90^\circ$
 $m(\angle O) = 120^\circ$

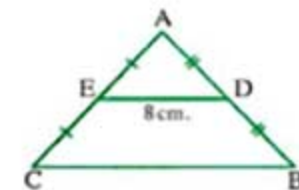
Find : $m(\angle C)$



5 [a] In the opposite figure :

ABC is a triangle in which $ED = 8$ cm.

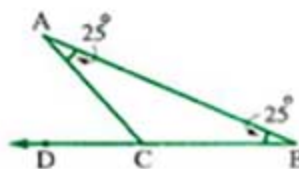
Find : The length of \overline{CB}



[b] In the opposite figure :

$m(\angle A) = m(\angle B) = 25^\circ$

Find : $m(\angle ACD)$



13

Kafr El-Sheikh Governorate

General Math Supervision



Answer the following questions :

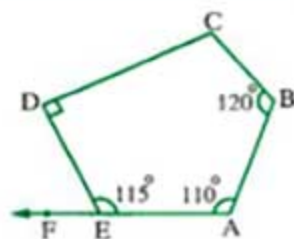
1 Choose the correct answer :

- 1 The sum of measures of the interior angles of a hexagon equals°
(a) 180 (b) 540 (c) 720 (d) 360
- 2 The two diagonals are equal in length and perpendicular in the
(a) trapezium. (b) square. (c) rectangle. (d) parallelogram.
- 3 In $\triangle XYZ$, if $m(\angle X) > m(\angle Y) + m(\angle Z)$, then $\angle X$ is angle.
(a) an acute (b) an obtuse (c) a right (d) a straight
- 4 The image of $(3, -5)$ by rotation $R(O, 90^\circ)$ is
(a) $(-3, 5)$ (b) $(-3, -5)$ (c) $(5, 3)$ (d) $(5, -3)$
- 5 The sum of the measures of the exterior angles of a triangle equals°
(a) 60 (b) 120 (c) 270 (d) 360
- 6 The measure of the exterior angle of the equilateral triangle is°
(a) 90 (b) 120 (c) 360 (d) 60

2 Complete :

- 1 The image of $A(-2, 3)$ by translation $(x+3, y-2)$ is
- 2 The rhombus with a right angle is
- 3 The image of $(-1, 2)$ by reflection in the origin point is
- 4 The length of the line segment joining two midpoints of two sides of a triangle is equal to the length of the third side.
- 5 If ABCD is a parallelogram in which $BC = 8$ cm. and $CD = 6$ cm. , then its perimeter = cm.

3 [a] In the opposite figure :

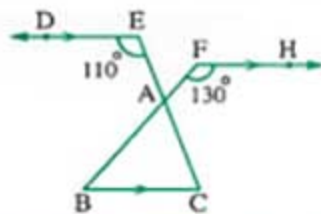
ABCDE is a pentagon in which $F \in \overline{AE}$ $m(\angle A) = 110^\circ$, $m(\angle B) = 120^\circ$, $m(\angle DEA) = 115^\circ$ $m(\angle D) = 90^\circ$ Find with proof : $m(\angle C)$ 

Geometry and Measurement

[b] In the opposite figure :

$$\overline{ED} \parallel \overline{BC} \parallel \overline{FH}$$

$$, m(\angle E) = 110^\circ , m(\angle F) = 130^\circ$$

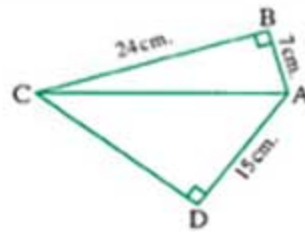
Find with proof : $m(\angle BAC)$ 

4 [a] In the opposite figure :

ABCD is a quadrilateral in which

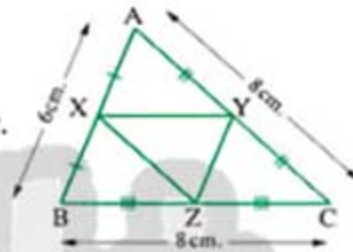
$$m(\angle B) = m(\angle D) = 90^\circ$$

$$, AB = 7 \text{ cm.} , BC = 24 \text{ cm. and } AD = 15 \text{ cm.}$$

Find : The length of each of \overline{AC} and \overline{DC} 

[b] In the opposite figure :

$$AB = 6 \text{ cm.} , BC = 8 \text{ cm.} , AC = 8 \text{ cm.}$$

 X, Y, Z are the midpoints of $\overline{AB}, \overline{AC}$ and \overline{BC} respectively.Find with proof : The perimeter of $\triangle XYZ$ 

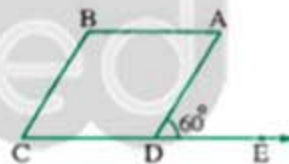
5 [a] On a square lattice , draw $\triangle ABC$, where $A(2, 4)$, $B(2, 1)$ and $C(6, 1)$, then draw its image by :

- 1 reflection in the y-axis. 2 rotation $(O, 180^\circ)$

[b] In the opposite figure :

ABCD is a parallelogram , $E \in \overline{CD}$

$$, m(\angle ADE) = 60^\circ$$

Find with proof : $m(\angle B)$ 

14 Beni Suef Governorate

Directorate of official Language Schools
Education Administration

Answer the following questions :

1 Choose the correct answer :

1 The measure of the interior angle of a regular polygon of n sides equals

- (a) $\frac{(n-2) \times 90^\circ}{n}$ (b) $\frac{(n-2) \times 180^\circ}{2}$ (c) $\frac{(n-2) \times 180^\circ}{n}$ (d) $180^\circ \times (n-1)$

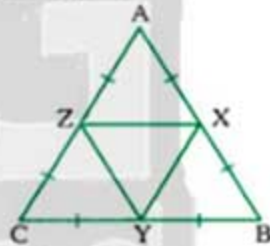
2 In $\triangle XYZ$, if $m(\angle X) = 50^\circ$, $m(\angle Y) = 100^\circ$, then $m(\angle Z) = \dots\dots\dots$

- (a) 30° (b) 50° (c) 80° (d) 100°

- 3 The measure of the exterior angle of the equilateral triangle at any one of its vertices equals
- (a) 30° (b) 60° (c) 120° (d) 150°
- 4 If the point $\hat{A}(-4, 5)$ is the image of the point A by translation $(-2, 3)$, then the point A is
- (a) $(-6, 8)$ (b) $(-2, 8)$ (c) $(-2, 2)$ (d) $(-6, 2)$
- 5 The angle whose measure is 179° , its type is
- (a) acute (b) right (c) obtuse (d) straight
- 6 If $\triangle ABC \cong \triangle XYZ$, then
- (a) $AB = YZ$ (b) $BC = XZ$ (c) $YX = CA$ (d) $ZY = CB$

2 Complete :

- 1 The parallelogram whose two diagonals are is called a rectangle.
- 2 The ray drawn from the midpoint of a side of a triangle parallel to another side
- 3 In the right-angled triangle, the area of the square drawn on the hypotenuse equals
- 4 In the opposite figure :
- $\triangle ABC$ is an equilateral triangle in which X, Y and Z are the midpoints of \overline{AB} , \overline{BC} and \overline{AC} respectively, then the image of $\triangle XBY$ by a translation of magnitude XZ in the direction of \overline{XZ} is
- 5 If a straight line intersects two parallel straight lines, then every two corresponding angles are

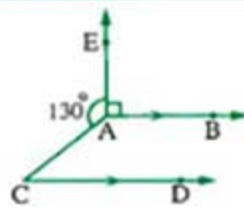


3 [a] In the opposite figure :

$$\overline{AB} \parallel \overline{CD}, m(\angle EAC) = 130^\circ$$

$$\text{and } m(\angle EAB) = 90^\circ$$

Find each of : $m(\angle BAC)$ and $m(\angle C)$

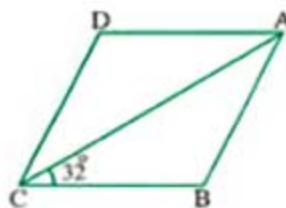


[b] In the opposite figure :

ABCD is a rhombus

\overline{AC} is a diagonal in it, $m(\angle ACB) = 32^\circ$

Find : $m(\angle D)$

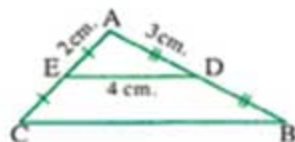


Geometry and Measurement

4 [a] In the opposite figure :

D and E are the midpoints of \overline{AB} and \overline{AC} respectively
 $AD = 3$ cm. , $AE = 2$ cm. and $DE = 4$ cm.

Find : The perimeter of the figure DBCE

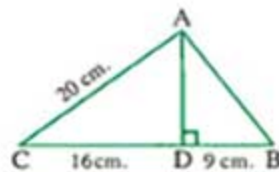


[b] In the opposite figure :

$\overline{AD} \perp \overline{BC}$, $BD = 9$ cm.

$DC = 16$ cm. and $AC = 20$ cm.

Find : The length of each of \overline{AD} and \overline{AB}

5 On a square lattice , draw $\triangle ABC$ where

A $(-6, -1)$, B $(-2, -1)$ and C $(-5, -6)$, then draw :

1 The image of $\triangle ABC$ by reflection in the X-axis.

2 The image of $\triangle ABC$ by rotation about the origin point with an angle of measure (-180°)

15

Souhag Governorate

Math Supervision



Answer the following questions :

1 Choose the correct answer from those given :

1 The sum of the measures of the interior angles of a pentagon equals°

- (a) 108 (b) 180 (c) 540 (d) 720

2 In the the two diagonals are perpendicular and not equal in length.

- (a) square (b) rectangle (c) rhombus (d) parallelogram

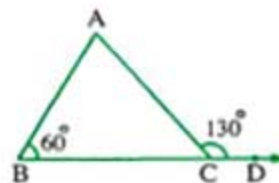
3 The image of the point $(-2, 3)$ by reflection in the y-axis is the point

- (a) $(3, 2)$ (b) $(-3, 2)$ (c) $(2, 3)$ (d) $(-3, -2)$

4 In the opposite figure :

$m(\angle A) = \dots\dots\dots$

- (a) 40° (b) 50°
 (c) 60° (d) 70°



5 The image of the point $(-1, 3)$ by translation $(4, -2)$ is

- (a) $(3, 1)$ (b) $(3, -1)$ (c) $(5, 1)$ (d) $(5, -5)$

6 In the triangle ABC , if $m(\angle A) = 50^\circ$, $m(\angle B) = 100^\circ$, then $m(\angle C) = \dots\dots\dots$

- (a) 30° (b) 180° (c) 32° (d) 23°

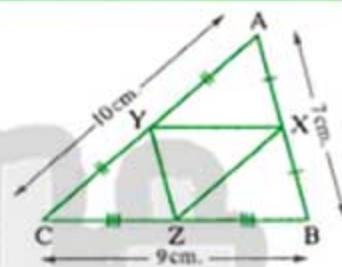
2 Complete each of the following :

- The length of the line segment joining the midpoints of two sides of a triangle is and
- If $\triangle XYZ$ is a right-angled triangle at X , $XY = 12$ cm. and $XZ = 9$ cm., then $YZ =$ cm.
- The image of the point $(-1, 2)$ by rotation about the origin point with an angle of measure 90° is
- If $\triangle ABC \cong \triangle XYZ$, then $m(\angle B) = m(\angle \dots\dots\dots)$
- The ray drawn from the midpoint of a side of a triangle parallel to another side

3 [a] In the opposite figure :

X, Y, Z are the midpoints of $\overline{AB}, \overline{AC}, \overline{BC}$ respectively, $AB = 7$ cm.,
 $BC = 9$ cm., $AC = 10$ cm.

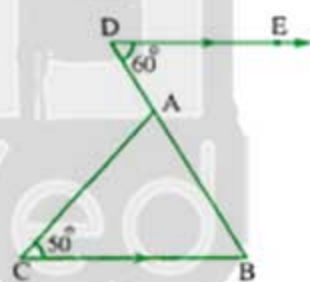
Find : The perimeter of $\triangle XYZ$



[b] In the opposite figure :

$\overline{DE} \parallel \overline{CB}$, $m(\angle D) = 60^\circ$, $m(\angle C) = 50^\circ$

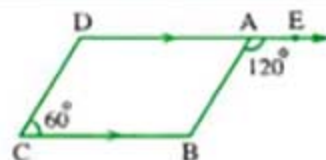
Find : $m(\angle DAC)$



4 [a] In the opposite figure :

$\overline{DA} \parallel \overline{BC}$, $m(\angle DCB) = 60^\circ$
 $m(\angle EAB) = 120^\circ$

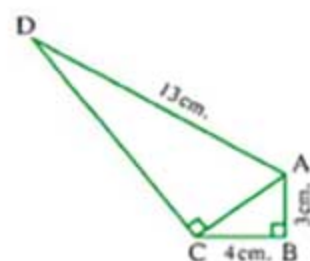
Prove that : ABCD is a parallelogram.



[b] In the opposite figure :

$m(\angle B) = m(\angle ACD) = 90^\circ$
 $AB = 3$ cm., $BC = 4$ cm.
 and $AD = 13$ cm.

Find : The length of each of \overline{AC} , \overline{CD}



Geometry and Measurement

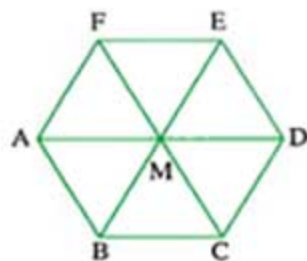
- 5 [a] On the square lattice draw $\triangle ABC$, where $A(1, 2)$, $B(4, 2)$, $C(4, -1)$, then find its image by rotation about the origin point with an angle of measure 180°

- [b] In the opposite figure :

ABCDEF is a regular hexagon

Find the image of $\triangle ABM$ by :

- 1 reflection in \overleftrightarrow{EB}
- 2 translation FE in direction of \overrightarrow{FE}
- 3 rotation $(M, 120^\circ)$
- 4 reflection in M



Final Examinations

on Geometry and Measurement



هذا العمل خاص بموقع ذاكرولي التعليمي ولا يسمح بتداوله على مواقع أخرى

Model Examinations of the School Book

on Geometry and
Measurement

Model 1

Answer the following questions :

1 Choose the correct answer from those given :

- 1 Circumference of a circle of radius 7 cm. = cm.

$(\pi = \frac{22}{7})$

- (a) 11 (b) 22 (c) 44 (d) 88

- 2 The image of the point
- $(-1, 3)$
- by translation
- $(4, -2)$
- is

- (a)
- $(3, 1)$
- (b)
- $(3, -1)$
- (c)
- $(5, 1)$
- (d)
- $(5, -5)$

- 3 The measure of the exterior angle of the equilateral triangle is

- (a)
- 30°
- (b)
- 45°
- (c)
- 60°
- (d)
- 120°

- 4 In a parallelogram if the adjacent sides are equal in the length, then the shape is

- (a) square. (b) rhombus. (c) rectangle. (d) trapezium.

- 5 The number of the diagonals of a pentagon is

- (a) 3 (b) 5 (c) 7 (d) 9

- 6 The number of axes of symmetry of an isosceles triangle =

- (a) zero (b) 1 (c) 2 (d) 3

2 Complete the following :

- 1 The image of the point
- $(2, 1)$
- by reflection in X-axis is

- 2 In the opposite figure :

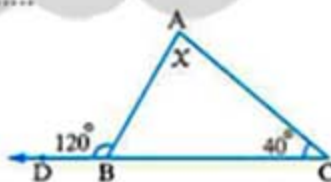
$X = \dots\dots\dots^\circ$

- 3 XYZ is a triangle in which
- $m(\angle Y) = 90^\circ$
- ,
- $XY = 3$
- cm.

, $XZ = 5$ cm. , then $YZ = \dots\dots\dots$ cm.

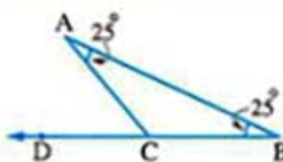
- 4 ABCD is a parallelogram in which
- $m(\angle A) = 100^\circ$
- , then
- $m(\angle B) + m(\angle D) = \dots\dots\dots^\circ$

- 5 The sum of the measures of the interior angles of a triangle =



3 [a] In the opposite figure :

$m(\angle A) = m(\angle B) = 25^\circ$

Find : $m(\angle ACD)$ 

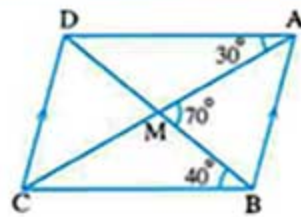
Geometry and Measurement

- [b] Draw a triangle ABC in which $AB = 5$ cm. , $AC = 3$ cm. and $m(\angle A) = 40^\circ$
 , then draw \hat{C} is the image of C under rotation $R(A, 40^\circ)$, \hat{B} is the image
 of B under rotation $R(A, -40^\circ)$

4 [a] In the opposite figure :

$\overline{AB} \parallel \overline{DC}$, $\overline{AC} \cap \overline{BD} = \{M\}$,
 $m(\angle DAC) = 30^\circ$, $m(\angle DBC) = 40^\circ$
 and $m(\angle AMB) = 70^\circ$

Prove that : ABCD is a parallelogram.



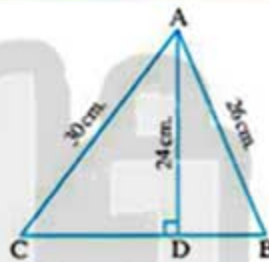
- [b] Use the translation : $(X, y) \longrightarrow (X + 2, y + 3)$
 to find the point whose image is $(2, 3)$

5 [a] In the opposite figure :

$\overline{AD} \perp \overline{BC}$, if $AD = 24$ cm. , $AB = 26$ cm. , $AC = 30$ cm.

1 Find : The length of \overline{BC}

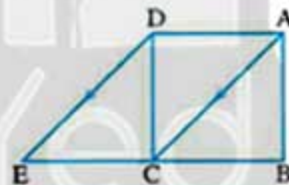
2 Find : The area of $\triangle ABC$



[b] In the opposite figure :

ABCD is a square , $E \in \overline{BC}$, $\overline{AC} \parallel \overline{DE}$

Prove that : ACED is a parallelogram.



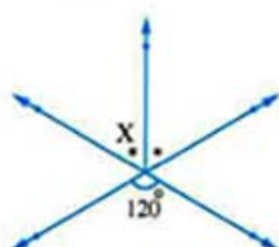
Model 2

Answer the following questions :

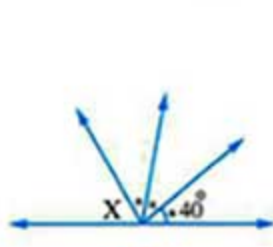
1 Choose the correct answer from those given :

- 1 ABC is a right-angled triangle at B , $AB = 6$ cm. , $BC = 8$ cm. , then $AC = \dots\dots\dots$ cm.
 (a) 10 (b) 28 (c) 100 (d) 160
- 2 The measure of each angle of regular hexagon equals
 (a) 60° (b) 108° (c) 120° (d) 135°
- 3 The two diagonals are equal in length and not perpendicular in
 (a) parallelogram. (b) rectangle. (c) rhombus. (d) square.

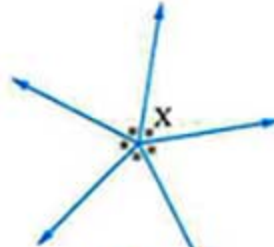
- 4 In all the following shapes $m(\angle X) = 60^\circ$ except the shape



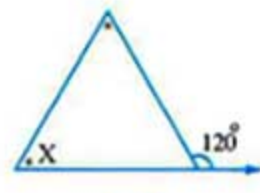
(a)



(b)



(c)



(d)

- 5 In the opposite figure :

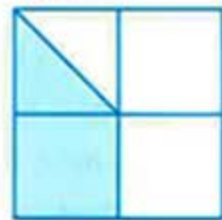
The area of the shaded part from the area of all shape equals

(a) $\frac{1}{8}$

(b) $\frac{1}{4}$

(c) $\frac{3}{8}$

(d) $\frac{3}{4}$



- 6 In the opposite figure :

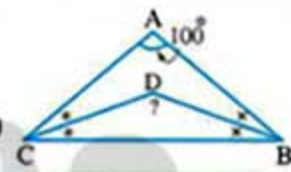
$m(\angle BDC) = \dots\dots\dots^\circ$

(a) 60

(b) 80

(c) 100

(d) 140



- 2 Complete the following :

- 1 In the opposite figure :

Semicircle of diameter 14 cm. and two semicircles the diameter of each is 7 cm.

, then the perimeter of the figure equals cm. ($\pi = \frac{22}{7}$)



- 2 The image of the point (2, 3) by translation MN, in direction \overrightarrow{MN} , where M (2, -1), N (5, 1) is

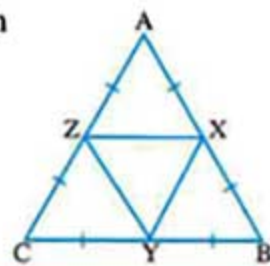
- 3 The volume of a cube of side length 1.2 m. = cm^3 .

- 4 The ray drawn parallel to one side of a triangle and passing through the midpoint of another side

- 5 In the opposite figure :

The image of the triangle XBY

by translation XZ in direction \overrightarrow{XZ} is



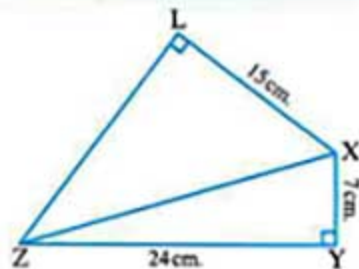
- 3 [a] In the opposite figure :

XYZL is a quadrilateral in which

$m(\angle Y) = m(\angle L) = 90^\circ$, $XY = 7 \text{ cm}$,

$YZ = 24 \text{ cm}$, $XL = 15 \text{ cm}$.

Find : The length of each of \overline{XZ} and \overline{LZ}



Geometry and Measurement

- [b] Using the square lattice, draw \overline{AB} where $A(4, 3)$, $B(-1, 1)$
then find the image of \overline{AB} by translation $(x, y) \rightarrow (x+2, y-1)$

- 4 [a] Draw the image of triangle ABC where $A(1, 1)$, $B(3, 4)$, $C(5, 2)$
by reflection in X-axis.

- [b] In the opposite figure :

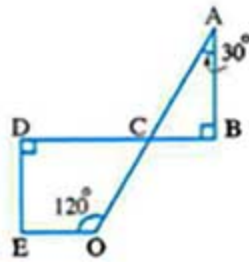
\overline{AB} and \overline{ED} are perpendicular to \overline{BD}

$$\overline{BD} \cap \overline{AO} = \{C\},$$

$$m(\angle A) = 30^\circ$$

$$m(\angle EOC) = 120^\circ,$$

Find : $m(\angle E)$

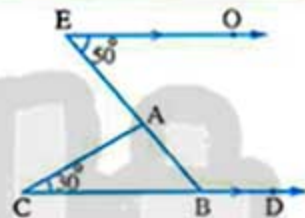


- 5 [a] In the opposite figure :

$$\overline{EO} \parallel \overline{CD}, m(\angle E) = 50^\circ$$

$$m(\angle C) = 30^\circ,$$

Find the measures of angles of $\triangle ABC$, $m(\angle ABD)$



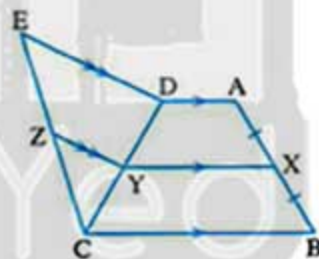
- [b] In the opposite figure :

X is the midpoint of \overline{AB}

$$Y \in \overline{CD}, Z \in \overline{CE}$$

$$\overline{AD} \parallel \overline{XY} \parallel \overline{BC}, \overline{YZ} \parallel \overline{DE}$$

Is $CZ = ZE$? giving reason

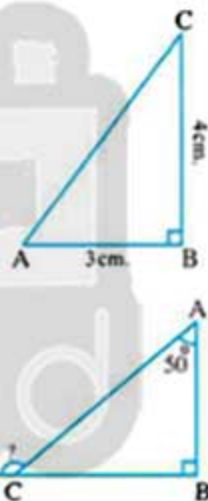


Model examination for the merge students

Answer the following questions :

1 Choose the correct answer :

- 1 The sum of the measures of the interior angles of a triangle =°
 (a) 90 (b) 360 (c) 180 (d) 540
- 2 The image of the point (3, -2) by reflection in the y-axis is the point
 (a) (3, 2) (b) (-3, -2) (c) (-3, 2) (d) (-2, 3)
- 3 The diagonals are equal and perpendicular in
 (a) rhombus. (b) square. (c) rectangle. (d) parallelogram.
- 4 In the opposite figure :
 AC = cm.
 (a) 5 (b) 7
 (c) 25 (d) 625
- 5 In the opposite figure :
 $m(\angle ACD) = \dots\dots\dots^\circ$
 (a) 40 (b) 140
 (c) 90 (d) 50



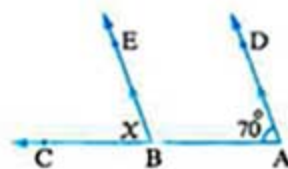
2 Complete each of the following :

- 1 The length of the line segment that joins two midpoints of two sides of a triangle equals the length of the third side.
- 2 The rectangle is a parallelogram in which one of its angles is
- 3 The length of the side of a rhombus whose perimeter is 24 cm. equals cm.
- 4 The image of the point A (-3, 2) by reflection in the origin point is the point \hat{A} (..... ,)

Geometry and Measurement

5 In the opposite figure :

$x = \dots\dots\dots^\circ$



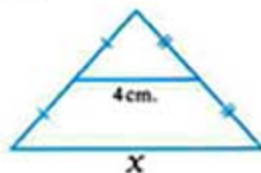
3 Put (✓) or (X) :

- 1 The image of the point (4, 3) by reflection in the X-axis is the point (3, -4) ()
- 2 If ABC is a right-angled triangle at B, then $(AB)^2 = (BC)^2 + (AC)^2$ ()
- 3 The pentagon has 5 diagonals. ()
- 4 ABCD is a parallelogram, in which $m(\angle A) = 70^\circ$, then $m(\angle C) = 110^\circ$ ()
- 5 Any triangle contains at least two acute angles. ()

4 Join from the column (A) to the suitable in the column (B) :

Column (A)	Column (B)
1 The sum of the measures of the interior angles of a quadrilateral =	• 120°
2 The measure of each angle of a regular hexagon =	• 360°
3 The image of the point (3, 2) by translation (1, -2) is the point	• (-1, -3)
4 The image of the point (1, 3) by rotation about the origin point, of angle of measure 180° is the point (.....,)	• 45
5 The diagonal of the square divides the angle of the vertex into two angles, the measure of each =°	• (4, 0)

5 Find the value of x :



$x = \dots\dots\dots \text{ cm.}$

Fig. (1)



$x = \dots\dots\dots^\circ$

Fig. (2)

Schools Examinations

on Geometry and
Measurement

1

Cairo Governorate

Hedagok El Koba Educational Zone



Answer the following questions : (Calculators are Permitted)

1 Choose the correct answer :

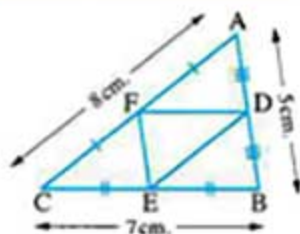
- 1 The measure of the interior angle of the regular octagon equals
 - (a) 1080°
 - (b) 180°
 - (c) 135°
 - (d) 108°
- 2 If ABCD is a parallelogram in which $m(\angle A) + m(\angle C) = 140^\circ$, then $m(\angle B) = \dots\dots\dots$
 - (a) 40°
 - (b) 110°
 - (c) 70°
 - (d) 60°
- 3 In $\triangle ABC$, if $m(\angle B) = 90^\circ$, $AB = 20$ cm., $AC = 25$ cm., then $BC = \dots\dots\dots$ cm.
 - (a) 625
 - (b) 12
 - (c) 15
 - (d) 225
- 4 If the perimeter of a square is 20 cm., then its area equals cm^2
 - (a) 25
 - (b) 100
 - (c) 5
 - (d) 16
- 5 The image of the point $(-3, 5)$ by rotation about the origin point with an angle of measure 90° is
 - (a) $(-5, 3)$
 - (b) $(-5, -3)$
 - (c) $(5, 3)$
 - (d) $(3, -5)$
- 6 The image of the point $(-1, 3)$ by translation $(4, -2)$ is
 - (a) $(3, 1)$
 - (b) $(3, -1)$
 - (c) $(5, 1)$
 - (d) $(5, -5)$

2 Complete the following :

- 1 The line segment joining the midpoints of two sides of a triangle is parallel to
- 2 The image of the point $(2, -4)$ by reflection in y-axis is
- 3 The number of axes of symmetry of a rectangle is
- 4 The measure of the exterior angle of an equilateral triangle equals $^\circ$
- 5 The volume of a cube of edge length 6 cm. is cm^3

3 [a] In the opposite figure :

ABC is a triangle, D, E and F are the midpoints of \overline{AB} , \overline{BC} , \overline{CA} respectively where $AB = 5$ cm., $BC = 7$ cm. and $CA = 8$ cm.
Calculate : The perimeter of $\triangle DEF$



Geometry and Measurement

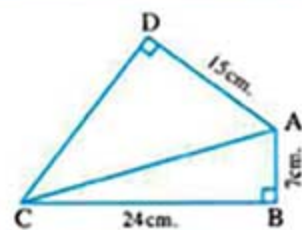
- [b] On square lattice, draw the square ABCD where A (1, 2), B (-2, 2), C (-2, 5) and D (1, 5), then draw its image by reflection in X-axis.

4 [a] In the opposite figure :

$$m(\angle B) = m(\angle D) = 90^\circ$$

$$AD = 15 \text{ cm.}, AB = 7 \text{ cm. and } BC = 24 \text{ cm.}$$

Find : The length of each of \overline{AC} , \overline{DC}



- [b] Draw $\triangle ABC$ where A (1, 5), B (3, 1) and C (5, 3), then draw its image by rotation about the origin point with an angle of measure 180°

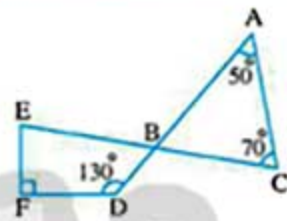
5 [a] In the opposite figure :

$$\overline{CE} \cap \overline{AD} = \{B\}$$

$$m(\angle A) = 50^\circ, m(\angle C) = 70^\circ$$

$$m(\angle D) = 130^\circ \text{ and } m(\angle F) = 90^\circ$$

Find : $m(\angle E)$



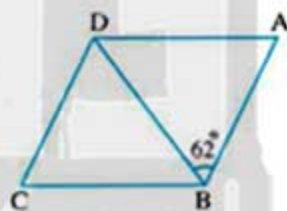
[b] In the opposite figure :

ABCD is a rhombus

\overline{BD} is a diagonal in it

$$m(\angle ABD) = 62^\circ$$

Find with proof : $m(\angle A)$



2

Cairo Governorate

East Naser City Zone
Manaret Heliopolis School

Answer the following questions :

1 Complete :

- The sum of measures of the exterior angles of the heptagon is
- If two lines intersect, then each two vertically opposite angles are
- In $\triangle ABC$, if $m(\angle A) + m(\angle C) = m(\angle B)$, then $m(\angle B) = \dots\dots\dots$
- The image of (2, 3) by translation $(X, y) \longrightarrow (X + 4, y - 2)$ is
- The length of the line segment joining two midpoints of two sides of a triangle equals the length of the third side.

2 Choose the correct answer :

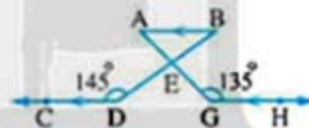
- 1 ABCD is a parallelogram in which $m(\angle A) = 80^\circ$, then $m(\angle C) = \dots\dots\dots$
 (a) 80° (b) 100° (c) 120° (d) 60°
- 2 If the image of the point $(5, -3)$ by rotation about the origin point is itself, then the measure of the rotation angle is $\dots\dots\dots^\circ$
 (a) 90 (b) 180 (c) 270 (d) 360
- 3 The line segment joining two midpoints of two sides of a triangle is $\dots\dots\dots$ the third side.
 (a) intersecting (b) parallel to (c) perpendicular to (d) congruent to
- 4 The sum of measures of the accumulative angles at a point is $\dots\dots\dots^\circ$
 (a) 90 (b) 180 (c) 270 (d) 360
- 5 If ABC is a right-angled triangle at B and $AB = 4$ cm, $BC = 3$ cm, then $AC = \dots\dots\dots$ cm.
 (a) 16 (b) 25 (c) 9 (d) 5
- 6 The sum of measures of the interior angles of a hexagon is $\dots\dots\dots^\circ$
 (a) 360 (b) 540 (c) 720 (d) 120

3 [a] In the opposite figure :

ABE is a triangle, $\overline{AB} \parallel \overline{GH} \parallel \overline{CD}$, $m(\angle CDB) = 145^\circ$

, $m(\angle AGH) = 135^\circ$

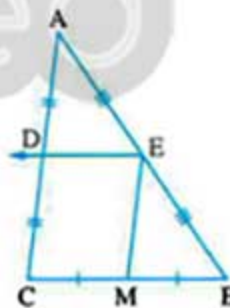
Calculate : $m(\angle DEG)$



[b] In the opposite figure :

ABC is a triangle in which E, M and D are the midpoints of \overline{AB} , \overline{BC} and \overline{CA} respectively

Prove that : DEMC is a parallelogram.



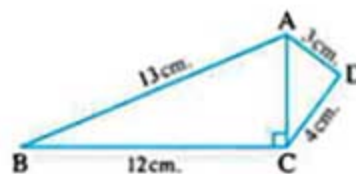
4 [a] In the opposite figure :

$m(\angle ACB) = 90^\circ$, $AB = 13$ cm, $AD = 3$ cm.

, $CD = 4$ cm, $BC = 12$ cm.

Find : 1 The length of \overline{AC}

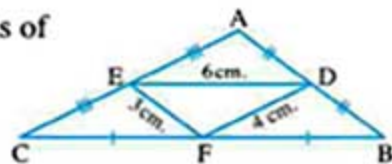
2 The perimeter of the figure ABCD



Geometry and Measurement

[b] In the opposite figure :

ABC is a triangle in which : D , F and E are the midpoints of \overline{AB} , \overline{BC} and \overline{CA} respectively such that : $DF = 4$ cm ,
 $FE = 3$ cm , $DE = 6$ cm .

Calculate : The perimeter of ΔABC 

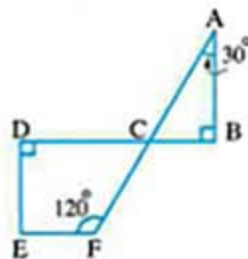
5 [a] Using the lattice , find the images of the points :

A (- 4 , 1) , B (0 , 4) and C (- 2 , 2) by reflection in X-axis.

[b] In the opposite figure :

$\overline{AB} \perp \overline{BC}$, $\overline{ED} \perp \overline{CD}$, $\overline{BD} \cap \overline{AF} = \{C\}$

$m(\angle A) = 30^\circ$, $m(\angle F) = 120^\circ$

Find with proof : 1 $m(\angle ACB)$ 2 $m(\angle E)$ 

3

Giza Governorate

El-haram Directorate
Fadl language School

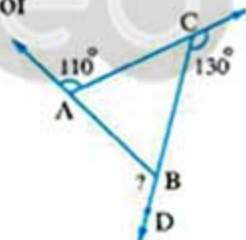
Answer the following questions :

1 Complete :

- The image of the point (2 , - 1) by reflection in X-axis is
- ABCD is a parallelogram in which $m(\angle A) = 60^\circ$, then $m(\angle B) = \dots\dots\dots^\circ$
- The measure of each angle of the regular hexagon equals
- The length of the line segment that joins two midpoints of two sides of a triangle equals the length of the third side.

5 In the opposite figure :

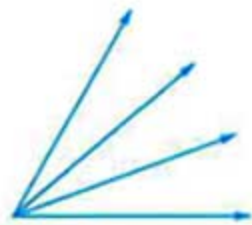
$m(\angle ABD) = \dots\dots\dots^\circ$



2 Choose the correct answer :

- The number of the diagonals of a pentagon is
 (a) 3 (b) 5 (c) 7 (d) 9
- The image of the point (2 , 5) by rotation about the origin point with an angle of measure 90° is
 (a) (- 5 , 2) (b) (5 , - 2) (c) (- 2 , - 5) (d) (- 2 , 5)

- 3 ABC is a right-angled triangle at A , then $(AC)^2 = (BC)^2 \dots\dots\dots (AB)^2$
 (a) + (b) \times (c) \div (d) -
- 4 The number of axes of symmetry of the rectangle is
 (a) 1 (b) 2 (c) 3 (d) 4
- 5 If the total surface area of a cuboid = 148 cm^2 and its lateral surface area = 118 cm^2
 , then its base area = cm^2
 (a) 30 (b) 15 (c) 45 (d) 266
- 6 Number of acute angles in the opposite figure is
 (a) 3 (b) 4 (c) 5 (d) 6



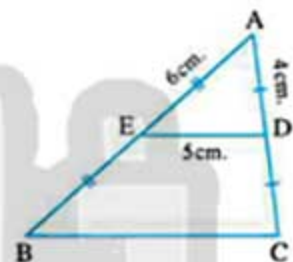
- 3 [a] In the opposite figure :

E and D are midpoints of \overline{AB} and \overline{AC}

, AE = 6 cm. , ED = 5 cm.

, AD = 4 cm.

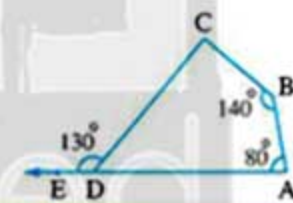
, Calculate the perimeter of ΔABC



- [b] In the opposite figure :

$D \in \overline{AE}$

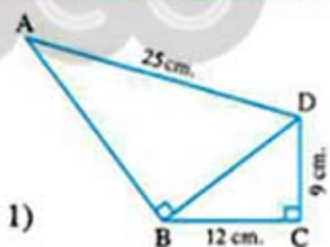
Find : $m(\angle C)$



- 4 [a] In the opposite figure :

$m(\angle C) = m(\angle ABD) = 90^\circ$

Find : The length of each of \overline{BD} and \overline{AB}

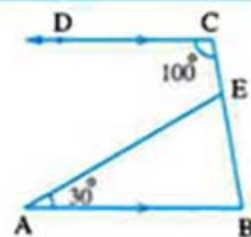


- [b] On the square lattice , draw ΔABC where A (0 , 5) , B (2 , 1)
 , C (4 , 7) , then draw the image of ΔABC by reflection in y-axis.

- 5 [a] In the opposite figure :

$\overline{BA} \parallel \overline{CD}$, $m(\angle C) = 100^\circ$, $m(\angle A) = 30^\circ$

Find : $m(\angle AEC)$



- [b] On the square lattice , draw \overline{AB} where A (4 , 3) , B (-1 , 1)
 , then draw the image of \overline{AB} by translation : $(X , y) \longrightarrow (X + 2 , y - 1)$

Geometry and Measurement

4

Giza Governorate

Experimental Schools
Math Inspector

Answer the following questions :

1 Complete the following :

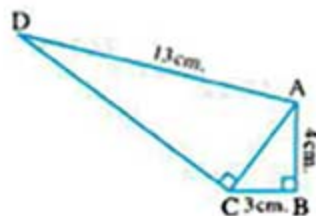
- The image of the point $(5, -3)$ under rotation of an angle of measure 90° about the origin point is
- The ray which is drawn from the midpoint of a side in a triangle parallel to another side the third side.
- In the rhombus the two diagonals are
- The sum of measures of the exterior angles of any convex polygon equals $^\circ$
- In $\triangle ABC$, if $m(\angle A) + m(\angle B) = m(\angle C)$, then $\triangle ABC$ is

2 Choose the correct answer :

- If the measure of an interior angle of a regular polygon is 135° , then the number of its sides is
(a) 6 (b) 4 (c) 7 (d) 8
- The image of the point $(-1, 4)$ by the translation $(x, y) \rightarrow (x+3, y-2)$ followed by reflection in the X-axis is
(a) $(2, 2)$ (b) $(-2, 2)$ (c) $(-2, -2)$ (d) $(2, -2)$
- ABCD is a parallelogram in which $m(\angle A) + m(\angle C) = 110^\circ$, then $m(\angle B) = \dots\dots\dots^\circ$
(a) 125 (b) 80 (c) 100 (d) 110
- The concave polygon should have angle.
(a) an acute (b) a right (c) an obtuse (d) a reflex
- The image of the point is itself by reflection in y-axis.
(a) $(0, 3)$ (b) $(3, 0)$ (c) $(3, 3)$ (d) $(-3, 3)$
- The identity rotation about the origin point with an angle of measure $^\circ$
(a) 90 (b) 180 (c) 360 (d) -90

3 [a] In the opposite figure :

ABCD is a quadrilateral in which
 $m(\angle B) = m(\angle ACD) = 90^\circ$
 $AB = 4$ cm, $BC = 3$ cm, and $AD = 13$ cm.
 Find : AC and DC

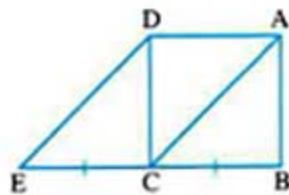


[b] In the opposite figure :

ABCD is a square , $E \in \overline{BC}$
such that $BC = CE$

1 Prove that : The figure ACED is a parallelogram.

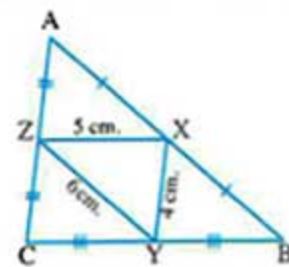
2 Find : $m(\angle E)$



4 [a] In the opposite figure :

ΔABC in which X , Y and Z are the midpoints of
 \overline{AB} , \overline{BC} , \overline{CA} respectively
 $XZ = 5$ cm. , $XY = 4$ cm. , $YZ = 6$ cm.

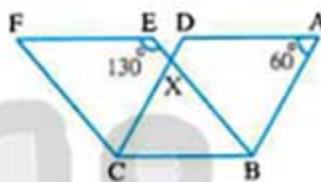
Find with proof : The perimeter of ΔABC



[b] In the opposite figure :

ABCD and EBCF are two parallelograms
 $m(\angle BAD) = 60^\circ$, $m(\angle BEF) = 130^\circ$

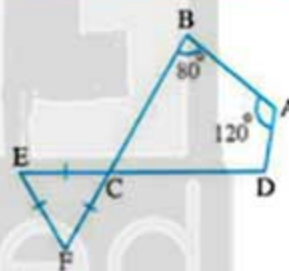
Find with proof : $m(\angle BXC)$



5 [a] In the opposite figure :

ABCD is a quadrilateral in which $m(\angle A) = 120^\circ$
 $m(\angle B) = 80^\circ$, ΔCEF is an equilateral triangle

Find : $m(\angle D)$



[b] Using the square lattice draw ΔABC where :

A (2 , 4) , B (4 , 2) and C (3 , 1) , then map its image by the translation
 $(x, y) \rightarrow (x + 2, y + 3)$

5

Alexandria Governorate

East Educational Zone
Mathematics Director

Answer the following questions :

1 Choose the correct answer :

1 The measure of the exterior angle of the equilateral triangle =

(a) 60° (b) 120° (c) 90° (d) 180°

2 The diagonals are equal in length and not perpendicular in

(a) parallelogram. (b) rectangle. (c) rhombus. (d) square.

Geometry and Measurement

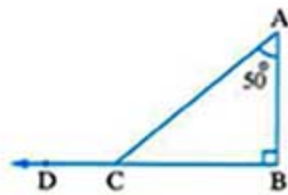
- 3 The image of the point $(-1, 3)$ by translation $(4, -2)$ is
- (a) $(3, 1)$ (b) $(3, -1)$ (c) $(5, 1)$ (d) $(5, -5)$

- 4 The measure of the interior angle of the regular hexagon is
- (a) 60° (b) 108° (c) 120° (d) 135°

- 5 In the opposite figure :

$m(\angle ACD) = \dots\dots\dots$

- (a) 40° (b) 140°
(c) 90° (d) 50°



- 6 If two adjacent sides in a parallelogram are equal in length, then it is a
- (a) square. (b) rhombus. (c) rectangle. (d) trapezium.

2 Complete :

- 1 The length of the line segment joining two midpoints of two sides of a triangle

- 2 The angle of measure 89° is angle.

- 3 In the opposite figure :

$m(\angle EBC) = \dots\dots\dots^\circ$

- 4 The image of $(-3, 2)$ by reflection in origin point is

- 5 A rhombus of perimeter 24 cm. its side length equals

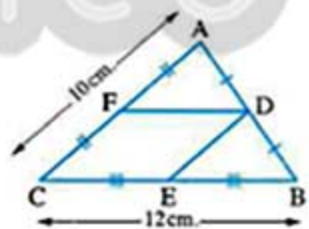


- 3 [a] Draw \overline{AB} such that $A(2, 1)$, $B(2, 4)$
then find its image by translation $(x, y) \rightarrow (x+5, y+2)$

- [b] In the opposite figure :

D, E, F are midpoints of \overline{AB} , \overline{BC} , \overline{CA}
 $BC = 12$ cm, $AC = 10$ cm.

Find : The perimeter of DECF

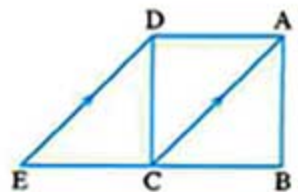


- 4 [a] Draw $\triangle LMN$ such that $L(-4, -1)$, $M(-1, -3)$, $N(0, -1)$
then find its image by reflection in X-axis.

- [b] In the opposite figure :

ABCD is a square, $E \in \overline{BC}$, $\overline{AC} \parallel \overline{DE}$

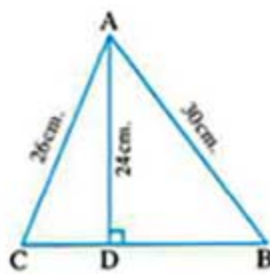
Prove that : ACED is a parallelogram.



- 5 [a] Find the number of sides of a regular polygon if the measure of its interior angle is 140°

[b] In the opposite figure :

Find the length of \overline{BC}
and the area of $\triangle ABC$



6 Alexandria Governorate

Middle Educational Zone
Math's Supervision



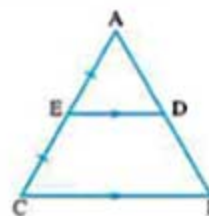
Answer the following questions :

- 1 Complete each of the following :

- 1 The measure of the straight angle equals°
- 2 The image of the point $(4, -2)$ by reflection in X-axis is
- 3 The ray drawn from the midpoint of a side parallel to another side in a triangle
- 4 The image of the point $(-2, 1)$ by rotation with an angle of measure 180° about origin point is
- 5 The length of line segment joining the midpoints of two sides of a triangle equals
- 6 A rhombus is a with two adjacent equal sides in length.

- 2 Choose the correct answer :

- 1 The perimeter of a square with side length 1 cm. equals cm.
(a) 5 (b) 1 (c) 4 (d) 2
- 2 The number of diagonals in a pentagon is
(a) 0 (b) 3 (c) 4 (d) 5
- 3 The edge length of a cube whose volume is 27 cm^3 is cm.
(a) 9 (b) 3 (c) 27 (d) 6
- 4 In $\triangle ABC$, if $m(\angle B) = 90^\circ$, $AB = 3 \text{ cm}$, $BC = 4 \text{ cm}$, then $AC = \dots\dots\dots \text{ cm}$.
(a) 7 (b) 12 (c) 1 (d) 5
- 5 In the opposite figure : $CB : ED = \dots\dots\dots$
(a) 1 : 1 (b) 1 : 2 (c) 2 : 1 (d) 1 : 4

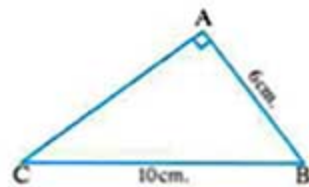


Geometry and Measurement

3 [a] In the opposite figure :

ABC is a right-angled triangle at A
 $BC = 10 \text{ cm}$, $AB = 6 \text{ cm}$.

Find : The length of \overline{AC}



- [b] Draw the image of the rectangle XYZL where $X(-5, 1)$, $Y(-5, 4)$, $Z(-1, 4)$, $L(-1, 1)$ by reflection in the X-axis.

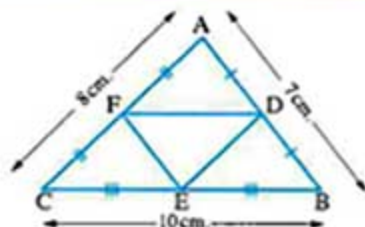
4 [a] In the opposite figure :

$BC = 10 \text{ cm}$, $AB = 7 \text{ cm}$, $AC = 8 \text{ cm}$.

Calculate : The perimeter of $\triangle FDE$

- [b] The ratio between the measures of the angles of a quadrilateral is $2 : 2 : 3 : 5$

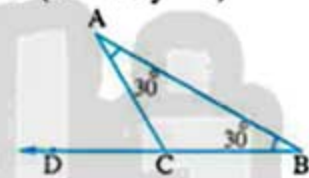
Calculate : The measure of the biggest angle.

5 [a] Find the image of the point A (5 , -5) by translation $(X, y) \rightarrow (X - 2, y - 3)$

[b] In the opposite figure :

$m(\angle A) = m(\angle B) = 30^\circ$

Find showing steps : $m(\angle ACD)$



7

El-Kalyoubia Governorate

Al-Obour Directorate of Education
 Memphis Language School



Answer the following questions :

1 Choose the correct answer from those given :

- The sum of the measures of the interior angles of a triangle equals
 (a) 90° (b) 180° (c) 270° (d) 360°
- The image of the point $(-1, 3)$ by translation $(4, -2)$ is
 (a) $(3, 1)$ (b) $(3, -1)$ (c) $(5, 1)$ (d) $(5, -5)$
- The measure of the exterior angle of the equilateral triangle is
 (a) 30° (b) 45° (c) 60° (d) 120°
- In a parallelogram if the adjacent sides are equal in length , then the shape is a
 (a) square. (b) rhombus. (c) rectangle. (d) trapezium.
- The number of the diagonals of a pentagon is
 (a) 3 (b) 5 (c) 7 (d) 9

2 Complete the following :

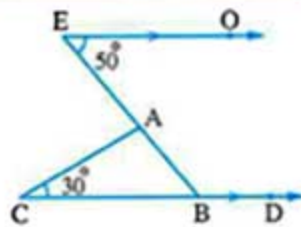
- The line segment joining the midpoints of two sides of a triangle is the third side.
- If $\triangle XYZ$ is a right-angled triangle at X , $XY = 12$ cm. and $XZ = 9$ cm.
then $YZ =$
- If $ABCD$ is a rhombus, then \perp
- The image of the point $(-1, 2)$ by rotation about the origin point with an angle of measure 90° is
- The sum of the measures of the accumulative angles about a point =

3 [a] In the opposite figure :

$$\overline{EO} \parallel \overline{CD}, m(\angle E) = 50^\circ$$

$$, m(\angle C) = 30^\circ$$

Find : The measures of the angles of $\triangle ABC$, $m(\angle ABD)$



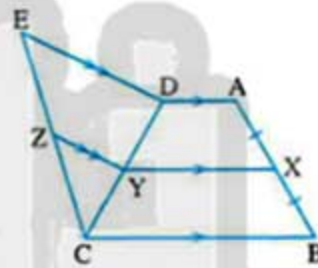
[b] In the opposite figure :

X is the midpoint of \overline{AB}

$Y \in \overline{CD}$, $Z \in \overline{CE}$

$\overline{AD} \parallel \overline{XY} \parallel \overline{BC}$, $\overline{YZ} \parallel \overline{DE}$

Is $CZ = ZE$? Giving reason.



- 4 [a] Using the square lattice, draw $\triangle ABC$, where $A(-2, 3)$, $B(2, 3)$, $C(2, 6)$, then find its image by translation $(X, y) \rightarrow (X + 2, y - 1)$

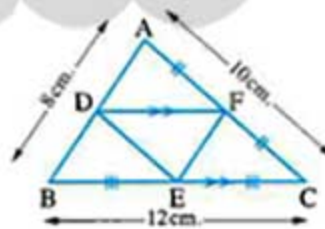
[b] In the opposite figure :

D, E, F are midpoints of

\overline{AB} , \overline{BC} , \overline{CA} respectively

$AB = 8$ cm., $BC = 12$ cm., $AC = 10$ cm.

Find : The perimeter of $\triangle DEF$

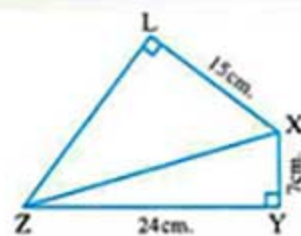


5 [a] In the opposite figure :

$XYZL$ is a quadrilateral in which $m(\angle Y) = m(\angle L) = 90^\circ$

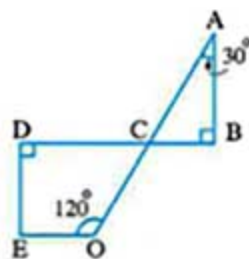
$XY = 7$ cm., $YZ = 24$ cm., $XL = 15$ cm.

Find : The length of each of \overline{XZ} and \overline{LZ}



Geometry and Measurement

[b] In the opposite figure :

 \overline{AB} and \overline{ED} are perpendicular to \overline{BD} $\overline{BD} \cap \overline{AO} = \{C\}$ $m(\angle A) = 30^\circ$, $m(\angle EOC) = 120^\circ$ Find : $m(\angle E)$ 

8

El-Gharbia Governorate

Official Language Schools
The Central Maths Supervision

Answer the following questions :

1 Choose the correct answer :

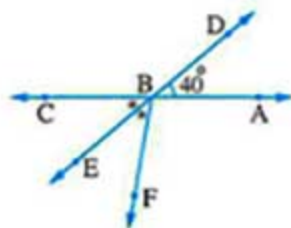
- 1 The measure of the exterior angle of the equilateral triangle equals°
(a) 30 (b) 45 (c) 60 (d) 120
- 2 If the image of the point (5 , - 3) by rotation around the origin point is itself , then the measure of the rotation angle equals°
(a) 90 (b) 270 (c) 180 (d) 360
- 3 The image of a square by rotation around the origin point with an angle of measure 90° is a
(a) rectangle. (b) square. (c) rhombus. (d) trapezium.
- 4 Any triangle has at least acute angles.
(a) 0 (b) 1 (c) 2 (d) 3
- 5 The measure of the interior angle of the regular hexagon equals°
(a) 60 (b) 108 (c) 120 (d) 135
- 6 The image of the point (- 5 , 0) by reflection in X-axis is
(a) (5 , 0) (b) (0 , 5) (c) (- 5 , 0) (d) (0 , - 5)

2 Complete :

- 1 The line segment joining the midpoints of two sides of a triangle is
- 2 If ABCD is a parallelogram in which $m(\angle A) = 60^\circ$, then $m(\angle B) = \dots\dots\dots^\circ$
- 3 The image of the point (3 , 2) by reflection in the origin point is
- 4 Each two opposite angles in a parallelogram are
- 5 The rectangle is a parallelogram in which one of its angles is

- 3 [a] In the opposite figure :

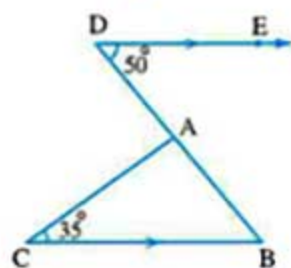
$$\overline{AC} \cap \overline{DE} = \{B\}, m(\angle ABD) = 40^\circ$$

and \overline{BE} bisects $\angle CBF$ Find with proof : $m(\angle ABF)$ 

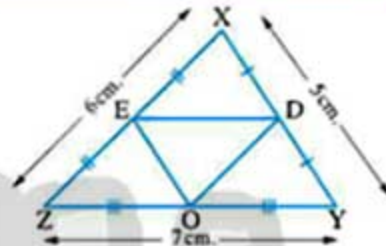
- [b] In the opposite figure :

$$\overline{DE} \parallel \overline{CB}, m(\angle D) = 50^\circ, m(\angle C) = 35^\circ$$

Find with proof :

 $m(\angle B), m(\angle BAC)$ 

- 4 [a] In the opposite figure :

XYZ is a triangle in which $XY = 5$ cm. $XZ = 6$ cm. , $YZ = 7$ cm.Find with proof : The perimeter of $\triangle DOE$ 

- [b] On the square lattice , draw the triangle whose

vertices are $A(4, 4), B(4, 2), C(1, 2)$, then find its image by the translation $(-4, -2)$

- 5 [a] In the opposite figure :

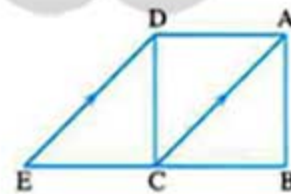
$$m(\angle B) = m(\angle ACD) = 90^\circ$$

 $AB = 12$ cm. , $BC = 9$ cm. , $CD = 20$ cm.Find : The length of \overline{AD} 

- [b] In the opposite figure :

ABCD is a square , $E \in \overline{BC}$, $\overline{AC} \parallel \overline{DE}$

Prove that : ACED is a parallelogram.



9

El-Dakahlia Governorate

Dakahlia Directorate of Education
Math's Supervision

Answer the following questions :

- 1 Choose the correct answer :

- 1 The sum of measures of the interior angles of the hexagon equals

(a) 270° (b) 180° (c) 720° (d) 360°

Geometry and Measurement

- 2 The side length of a rhombus whose perimeter 8 cm. =
 (a) 32 cm. (b) 2 cm. (c) 16 cm. (d) 12 cm.
- 3 The measure of each angle of a regular triangle equals
 (a) 60° (b) 108° (c) 120° (d) 135°
- 4 The parallelogram whose diagonals are perpendicular and equal in length is called
 (a) rhombus. (b) square. (c) rectangle. (d) trapezium.
- 5 The image of the point $(-3, 5)$ by rotation about the origin point with an angle of measure 270° is
 (a) $(5, 3)$ (b) $(-5, 3)$ (c) $(3, 5)$ (d) $(-5, -3)$
- 6 Any triangle has at least acute angles.
 (a) zero (b) 1 (c) 2 (d) 3

2 Complete each of the following :

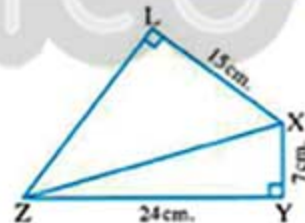
- 1 The measure of the exterior angle of an equilateral triangle equals
- 2 If $\triangle ABC$ is right-angled triangle at B , $m(\angle A) = 55^\circ$, then $m(\angle C) = \dots\dots\dots$
- 3 The parallelogram whose perimeter 28 cm. and the length of one of its sides is 10 cm. , then the length of its adjacent side equals
- 4 If the image of the point A (X, y) by a translation $(1, -4)$ is the point $(3, -2)$, then point A is $(\dots\dots\dots, \dots\dots\dots)$
- 5 The rectangle is a parallelogram in which one of its angles is

3 [a] In the opposite figure :

XYZL is quadrilateral in which $m(\angle Y) = m(\angle L) = 90^\circ$

, $XY = 7$ cm. , $YZ = 24$ cm. , $XL = 15$ cm.

Find : The length of each of \overline{XZ} , \overline{LZ}



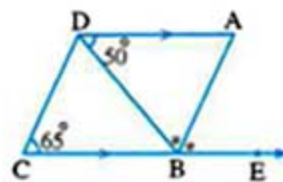
- [b] Draw on square lattice the image of triangle ABC where A $(0, 1)$, B $(3, 4)$, C $(5, 1)$ by reflection in y-axis.

4 [a] In the opposite figure :

$\overline{DA} \parallel \overline{CE}$, \overline{BA} bisects $\angle DBE$

, $m(\angle ADB) = 50^\circ$, $m(\angle C) = 65^\circ$

Prove that : ABCD is a parallelogram.



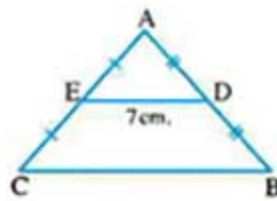
[b] In the opposite figure :

ABC is a triangle in which

D and E are the midpoints of \overline{AB} and \overline{AC} respectively

, $\overline{DE} = 7$ cm.

Find : The length of \overline{BC}



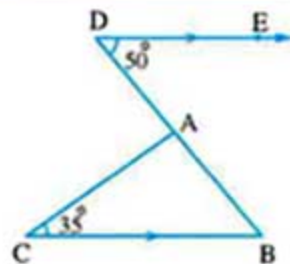
5 [a] In the opposite figure :

$\overline{DE} \parallel \overline{CB}$

, $m(\angle D) = 50^\circ$

, $m(\angle C) = 35^\circ$

Find : $m(\angle B)$ and $m(\angle BAC)$



- [b] Draw $\triangle OBC$ on a square lattice where $O(0, 0)$, $B(3, 0)$, $C(0, 4)$
 , then find its image by rotation about the origin point with an angle of measure (-180°)

10

Suez Governorate

Directorate of Education
Math Supervision

Answer the following questions :

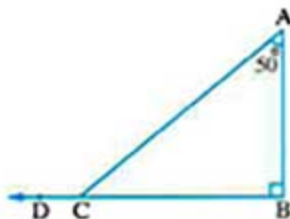
1 Choose the correct answer :

- The two diagonals are equal in length and not perpendicular in a
 (a) parallelogram. (b) rectangle. (c) square. (d) rhombus.
- The image of $(1, 3)$ by translation $(4, 2)$ is
 (a) $(3, 1)$ (b) $(5, 5)$ (c) $(5, 1)$ (d) $(5, -5)$
- The measure of an exterior angle in an equilateral triangle is $^\circ$
 (a) 30 (b) 45 (c) 60 (d) 120
- In a parallelogram if the two adjacent sides are equal in length , then the shape is a
 (a) square. (b) rhombus. (c) rectangle. (d) trapezium.
- The number of axes of symmetry of the equilateral triangle is
 (a) 0 (b) 1 (c) 2 (d) 3
- The sum of measures of the interior angles of a triangle is $^\circ$
 (a) 90 (b) 360 (c) 180 (d) 540

Geometry and Measurement

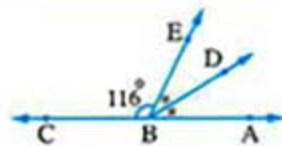
2 Complete :

- 1 In the opposite figure : $m(\angle ACD) = \dots\dots\dots^\circ$
- 2 The ray drawn from the midpoint of one side of a triangle parallel to another side
- 3 The image of the point $(1, -2)$ by reflection in X-axis is
- 4 The sum of measures of the interior angles of the pentagon is
- 5 If ABCD is a rhombus , then $\dots\dots\dots \perp \dots\dots\dots$



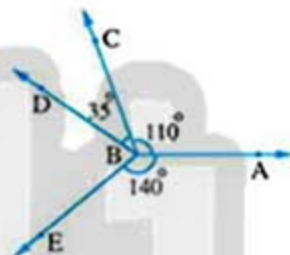
3 [a] In the opposite figure :

$B \in \overline{AC}$, $m(\angle CBE) = 116^\circ$
 \overline{BD} bisects $\angle ABE$
 Find : $m(\angle ABD)$



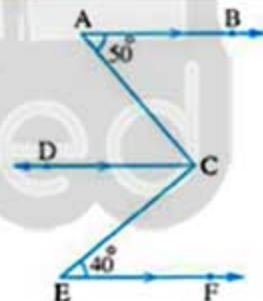
[b] In the opposite figure :

$m(\angle ABC) = 110^\circ$, $m(\angle CBD) = 35^\circ$
 $m(\angle ABE) = 140^\circ$
 Find : $m(\angle DBE)$



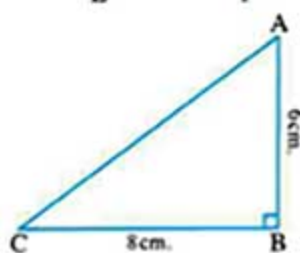
4 [a] In the opposite figure :

$\overline{AB} \parallel \overline{CD} \parallel \overline{EF}$
 $m(\angle A) = 50^\circ$, $m(\angle E) = 40^\circ$
 Find with proof : $m(\angle ACE)$



[b] In the opposite figure :

$\triangle ABC$ is right-angled at B
 $AB = 6 \text{ cm}$, $BC = 8 \text{ cm}$
 Find : The length of \overline{AC}



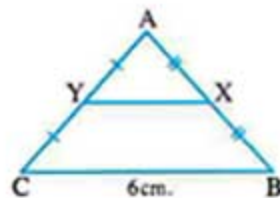
5 [a] Complete :

- 1 The image of $(3, 2)$ by rotation about the origin point with an angle of measure 90° is
- 2 The image of $(3, 2)$ by reflection in the origin point is

- 3 The image of (3, 2) by rotation about the origin point with an angle of measure 180° is

- 4 In the opposite figure :

$XY = \dots\dots\dots$ cm.

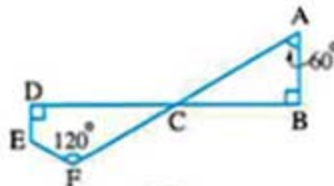


- [b] In the opposite figure :

\overline{AB} , \overline{DE} are perpendicular to \overline{BD}

, $\overline{BD} \cap \overline{AF} = \{C\}$, $m(\angle A) = 60^\circ$, $m(\angle CFE) = 120^\circ$

Find with proof : $m(\angle E)$



11

Damietta Governorate

Damietta Inspection of Mathematic
official language schools

Answer the following questions :

- 1 Choose the correct answer :

- 1 The measure of each angle of the regular pentagon equals°

(a) 60 (b) 108 (c) 120 (d) 135

- 2 The image of the point (2, -7) by reflection in the origin point is

(a) (2, 7) (b) (-2, 7) (c) (-2, -7) (d) (2, -7)

- 3 Any triangle has at least two angles.

(a) reflex (b) obtuse (c) acute (d) right

- 4 ABCD is parallelogram in which : $m(\angle A) + m(\angle C) = 100$, then $m(\angle B) = \dots\dots\dots^\circ$

(a) 50 (b) 150 (c) 130 (d) 80

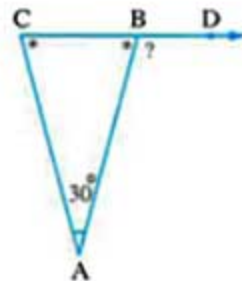
- 5 The ratio between the perimeter of an equilateral triangle and its side length =

(a) 3 : 1 (b) 3 : 2 (c) 1 : 3 (d) 2 : 3

- 6 In the opposite figure :


$m(\angle ABD) = \dots\dots\dots^\circ$

(a) 150 (b) 95
(c) 105 (d) 115



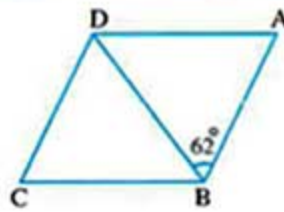
Geometry and Measurement

2 Complete each of the following :

- The ray drawn from the midpoint of a side of a triangle parallel to another side
- The image of the point $(3, -2)$ by rotation with an angle of measure 90° about the origin is
- If $m(\angle B) = 90^\circ$, then $m(\text{reflex } \angle B) = \dots\dots\dots^\circ$
- If ABC is right-angled triangle at B, $AB = 3$ cm. and $BC = 4$ cm., then $AC = \dots\dots\dots$ cm.
- This figure  has line (s) of symmetry.

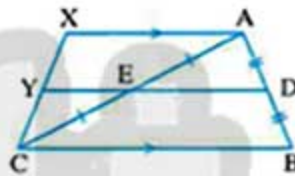
3 [a] In the opposite figure :

ABCD is a rhombus in which
 \overline{BD} is a diagonal and $m(\angle ABD) = 62^\circ$
 Find with proof : $m(\angle A)$



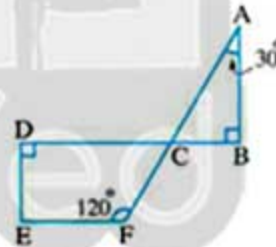
[b] In the opposite figure :

$AD = BD$, $AE = EC$, $\overline{AX} \parallel \overline{BC}$
 $\overline{DE} \cap \overline{XC} = \{Y\}$
 Prove that : Y is the midpoint of \overline{XC}



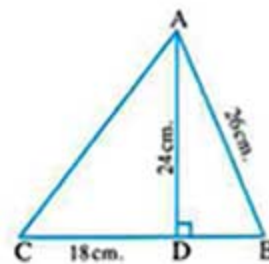
4 [a] In the opposite figure :

\overline{AB} and \overline{ED} are perpendicular to \overline{BD}
 $\overline{BD} \cap \overline{AF} = \{C\}$
 $m(\angle A) = 30^\circ$
 $m(\angle EFC) = 120^\circ$
 Find : $m(\angle E)$



[b] In the opposite figure :

ABC is a triangle and $\overline{AD} \perp \overline{BC}$
 If $AD = 24$ cm., $AB = 26$ cm.
 and $CD = 18$ cm.
 Find : The length of each of \overline{AC} , \overline{DB}



5 [a] On the square lattice find the image of the triangle LMN where :

$L(-4, -1)$, $M(-1, -3)$, $N(0, -1)$ by reflection in the X-axis.

- [b] Using the square lattice, draw \overline{AB} where $A(4, 3)$, $B(-1, 1)$
 then find the image of \overline{AB} by translation $(x, y) \rightarrow (x+2, y-1)$

12

Kafr El-Sheikh Governorate

General Maths Supervision



Answer the following questions :

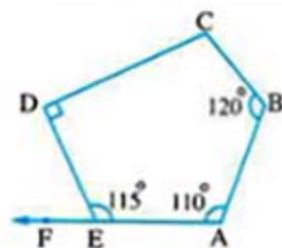
1 Choose the correct answer :

- 1 The sum of measures of the interior angles of a hexagon equals°
(a) 180 (b) 540 (c) 720 (d) 360
- 2 The two diagonals are equal in length and perpendicular in the
(a) trapezium. (b) square. (c) rectangle. (d) parallelogram.
- 3 In ΔXYZ , if $m(\angle X) > m(\angle Y) + m(\angle Z)$, then $\angle X$ is angle.
(a) an acute (b) an obtuse (c) a right (d) a straight
- 4 The image of $(3, -5)$ by rotation $R(O, 90^\circ)$ is
(a) $(-3, 5)$ (b) $(-3, -5)$ (c) $(5, 3)$ (d) $(5, -3)$
- 5 The sum of the measures of the exterior angles of a triangle equals°
(a) 60 (b) 120 (c) 270 (d) 360
- 6 The measure of the exterior angle of the equilateral triangle is°
(a) 90 (b) 120 (c) 360 (d) 60

2 Complete :

- 1 The image of $A(-2, 3)$ by translation $(X+3, Y-2)$ is
- 2 The rhombus with a right angle is
- 3 The image of $(-1, 2)$ by reflection in the origin point is
- 4 The length of the line segment joining two midpoints of two sides of a triangle is equal to the length of the third side.
- 5 If ABCD is a parallelogram in which $BC = 8$ cm. and $CD = 6$ cm. , then its perimeter = cm.

3 [a] In the opposite figure :

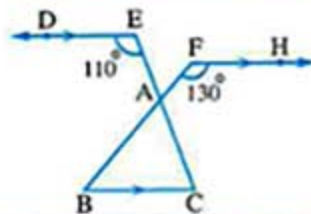
ABCDE is a pentagon in which $F \in \overline{AE}$ $m(\angle A) = 110^\circ$, $m(\angle B) = 120^\circ$, $m(\angle DEA) = 115^\circ$ $m(\angle D) = 90^\circ$ Find with proof : $m(\angle C)$ 

Geometry and Measurement

[b] In the opposite figure :

$$\overline{ED} \parallel \overline{BC} \parallel \overline{FH}$$

$$m(\angle E) = 110^\circ, m(\angle F) = 130^\circ$$

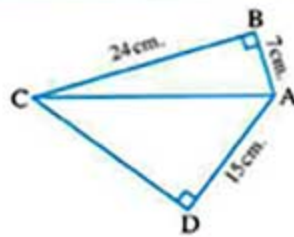
Find with proof : $m(\angle BAC)$ 

4 [a] In the opposite figure :

ABCD is a quadrilateral in which

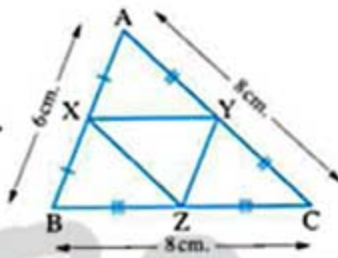
$$m(\angle B) = m(\angle D) = 90^\circ$$

$$AB = 7 \text{ cm}, BC = 24 \text{ cm}, \text{ and } AD = 15 \text{ cm}.$$

Find : The length of each of \overline{AC} and \overline{DC} 

[b] In the opposite figure :

$$AB = 6 \text{ cm}, BC = 8 \text{ cm}, AC = 8 \text{ cm}.$$

 X, Y, Z are the midpoints of $\overline{AB}, \overline{AC}$ and \overline{BC} respectively.Find with proof : The perimeter of $\triangle XYZ$ 5 [a] On a square lattice, draw $\triangle ABC$, where $A(2, 4)$, $B(2, 1)$ and $C(6, 1)$

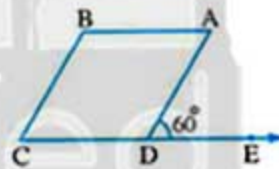
, then draw its image by :

- 1 reflection in the y-axis. 2 rotation $(O, 180^\circ)$

[b] In the opposite figure :

ABCD is a parallelogram, $E \in \overline{CD}$

$$m(\angle ADE) = 60^\circ$$

Find with proof : $m(\angle B)$ 

13

El-Beheira Governorate

Delengat Educational Directorate
Bani El-Delengat G.L.C

Answer the following questions :

1 Complete :

- In the right-angled triangle, area of the square drawn on the hypotenuse equals
- The reflection in a line reserves,
- The measure of the exterior angle of the triangle is equal to the sum of
- $(-3, 2)$ is the image of the point $(3, 2)$ by reflection in axis.
- The line segment joining the midpoints of two sides of the triangle is the third side.

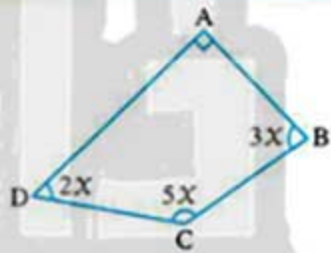
2 Choose the correct answer :

- 1 The image of the point $(-1, 3)$ by translation $(4, -2)$ is
 (a) $(3, 1)$ (b) $(3, -1)$ (c) $(5, 1)$ (d) $(5, -5)$
- 2 The measure of the exterior angle of the equilateral triangle equals
 (a) 60° (b) 100° (c) 120° (d) 150°
- 3 The image of the point $(-3, 5)$ by rotation about the origin point by an angle of measure 90° is
 (a) $(5, 3)$ (b) $(5, -3)$ (c) $(-5, -3)$ (d) $(-5, 3)$
- 4 The sum of measures of the exterior angles of any polygon =
 (a) 180° (b) 360° (c) 120° (d) 540°
- 5 The number of lines of symmetry of the square =
 (a) 1 (b) 2 (c) 3 (d) 4
- 6 The parallelogram whose diagonals are is a rectangle.
 (a) parallel (b) perpendicular (c) equal in length (d) bisect each other

3 [a] In the opposite figure :

$$m(\angle A) = 90^\circ$$

Find the value of : x

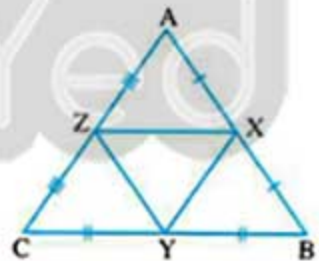


[b] In the opposite figure :

$$AC = AB = 7 \text{ cm.}$$

$$BC = 8 \text{ cm.}$$

Find : The perimeter of $\triangle XYZ$

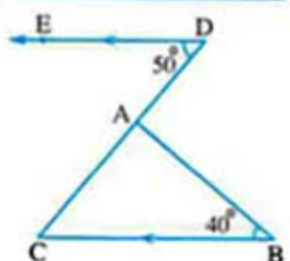


4 [a] In the opposite figure :

$$\overline{DE} \parallel \overline{BC}, m(\angle D) = 50^\circ$$

$$, m(\angle B) = 40^\circ$$

Find : $m(\angle BAC)$

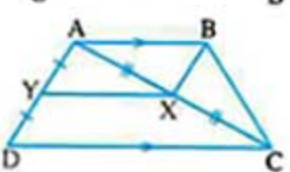


[b] In the opposite figure :

$$\overline{AB} \parallel \overline{DC}, AB = \frac{1}{2} DC$$

, X is the midpoint of \overline{AC} , Y is the midpoint of \overline{AD}

Prove that : $ABXY$ is a parallelogram.



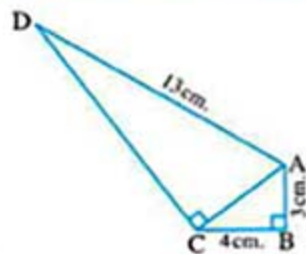
Geometry and Measurement

5 [a] In the opposite figure :

$$m(\angle B) = m(\angle ACD) = 90^\circ$$

$$AB = 3 \text{ cm.}, BC = 4 \text{ cm.}, AD = 13 \text{ cm.}$$

Find : The length of each of \overline{AC} and \overline{DC}



- [b] On the square lattice, draw $\triangle ABC$ where $A(1, 1)$, $B(4, 1)$, $C(4, 4)$, then find the image of $\triangle ABC$ by reflection in X-axis.

14

Souhag Governorate

Math Supervision



Answer the following questions :

1 Choose the correct answer from those given :

- 1 The sum of the measures of the interior angles of a pentagon equals°

(a) 108 (b) 180 (c) 540 (d) 720

- 2 In the the two diagonals are perpendicular and not equal in length.

(a) square (b) rectangle (c) rhombus (d) parallelogram

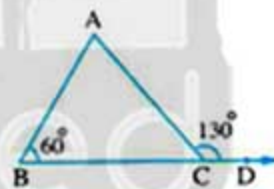
- 3 The image of the point $(-2, 3)$ by reflection in the y-axis is the point

(a) $(3, 2)$ (b) $(-3, 2)$ (c) $(2, 3)$ (d) $(-3, -2)$

- 4 In the opposite figure :

$$m(\angle A) = \dots\dots\dots$$

(a) 40° (b) 50°
(c) 60° (d) 70°



- 5 The image of the point $(-1, 3)$ by translation $(4, -2)$ is

(a) $(3, 1)$ (b) $(3, -1)$ (c) $(5, 1)$ (d) $(5, -5)$

- 6 In the triangle ABC, if $m(\angle A) = 50^\circ$, $m(\angle B) = 100^\circ$, then $m(\angle C) = \dots\dots\dots$

(a) 30° (b) 180° (c) 32° (d) 23°

2 Complete each of the following :

- 1 The length of the line segment joining the midpoints of two sides of a triangle is
- 2 If $\triangle XYZ$ is a right-angled triangle at X, $XY = 12 \text{ cm.}$ and $XZ = 9 \text{ cm.}$, then $YZ = \dots\dots\dots \text{ cm.}$
- 3 The image of the point $(-1, 2)$ by rotation about the origin point with an angle of measure 90° is

4 If $\triangle ABC \cong \triangle XYZ$, then $m(\angle B) = m(\angle \dots)$

5 The ray drawn from the midpoint of a side of a triangle parallel to another side

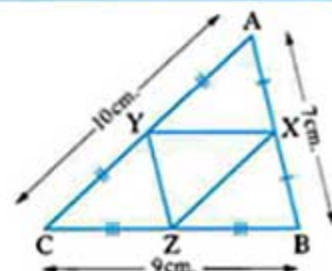
3 [a] In the opposite figure :

X, Y, Z are the midpoints of \overline{AB} , \overline{AC} , \overline{BC}

respectively, $AB = 7$ cm.

, $BC = 9$ cm., $AC = 10$ cm.

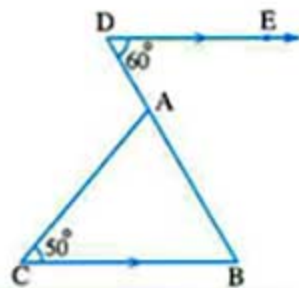
Find : The perimeter of $\triangle XYZ$



[b] In the opposite figure :

$\overline{DE} \parallel \overline{CB}$, $m(\angle D) = 60^\circ$, $m(\angle C) = 50^\circ$

Find : $m(\angle DAC)$



4 [a] In the opposite figure :

$\overline{DA} \parallel \overline{BC}$, $m(\angle DCB) = 60^\circ$

, $m(\angle EAB) = 120^\circ$

Prove that : ABCD is a parallelogram.



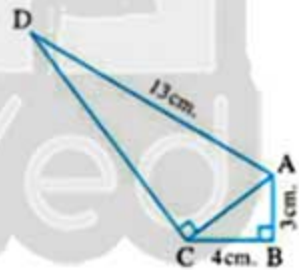
[b] In the opposite figure :

$m(\angle B) = m(\angle ACD) = 90^\circ$

, $AB = 3$ cm., $BC = 4$ cm.

and $AD = 13$ cm.

Find : The length of each of \overline{AC} , \overline{CD}



5 [a] On the square lattice draw $\triangle ABC$, where $A(1, 2)$, $B(4, 2)$, $C(4, -1)$, then find its image by rotation about the origin point with an angle of measure 180°

[b] In the opposite figure :

ABCDEF is a regular hexagon

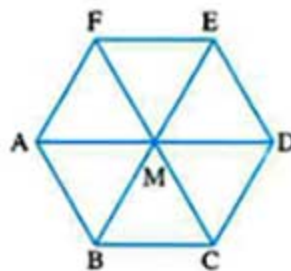
Find the image of $\triangle ABM$ by :

1 reflection in \overline{EB}

2 translation FE in direction of \overline{FE}

3 rotation (M, 120°)

4 reflection in M



Geometry and Measurement

15

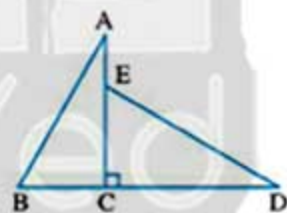
Qena Governorate

Qena Directorate of Education
Math's supervision

Answer the following questions :

1 Choose the correct answer :

- 1 The image of the point $(-3, 4)$ by reflection in y-axis is
- (a) $(2, -4)$ (b) $(-3, -5)$ (c) $(-3, -4)$ (d) $(3, 4)$
- 2 ABCD is a parallelogram, $m(\angle A) = 60^\circ$, then $m(\angle B) = \dots\dots\dots^\circ$
- (a) 120 (b) 60 (c) 90 (d) 100
- 3 ABCD is a parallelogram $m(\angle A) = m(\angle B)$, then ABCD is a
- (a) rectangle. (b) square. (c) rhombus. (d) trapezium.
- 4 Measure of each angle in the regular pentagon =
- (a) 108° (b) 100° (c) 90° (d) 60°
- 5 The image of the point $(-1, -2)$ by translation $(3, 1)$ is
- (a) $(1, 2)$ (b) $(2, -1)$ (c) $(0, 2)$ (d) $(3, -2)$
- 6 In the opposite figure :
- ΔABC is the image of ΔDEC
which is right-angled at C by rotation
about C with an angle of measure
- (a) 90° (b) -90°
(c) 180° (d) 360°



2 Complete :

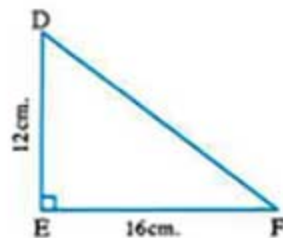
- 1 The ray drawn parallel to one side of a triangle and passing through the midpoint of another side
- 2 $(-5, 1)$ is the image of the point $(5, 1)$ by reflection in axis.
- 3 If two adjacent sides are equal in length in a parallelogram, then it becomes
- 4 Sum of measures of the exterior angles of any convex polygon =
- 5 In ΔLMN if $m(\angle M) = 90^\circ$, then $(LM)^2 = \dots\dots\dots$

- 3 [a] In the opposite figure :

EDF is a right-angled triangle at E , $DE = 12$ cm.

, $EF = 16$ cm.

Find : DF

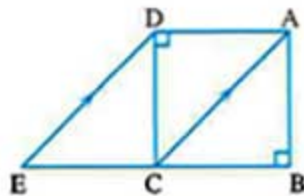


- [b] In the opposite figure :

ABCD is a square , $E \in \overline{BC}$

, $\overline{AC} \parallel \overline{DE}$

Prove that : ACED is a parallelogram.



- 4 [a] Using the square lattice , draw $\triangle ABC$ where $A(-4, 2)$, $B(0, 1)$ and $C(-1, -2)$, then find the image of $\triangle ABC$ by rotation $R(O, 180^\circ)$

- [b] Find the number of sides of the regular polygon if the measure of its angle = 144°

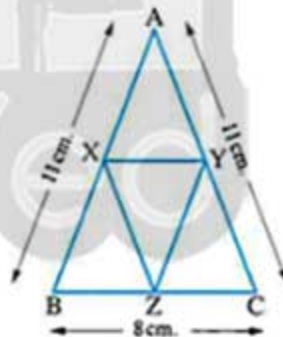
- 5 [a] Using the square lattice , draw $\triangle ABC$ where $A(-1, 3)$, $B(2, 1)$ and $C(4, 5)$, then find the image of $\triangle ABC$ by reflection in X-axis.

- [b] In the opposite figure :

$AB = 11$ cm. , $BC = 8$ cm. , $CA = 11$ cm.

X , Z , Y are midpoints of \overline{AB} , \overline{BC} , \overline{CA}

Find perimeter of : $\triangle XYZ$



Answers of school book models on Geometry and Measurement

Model 1

1 (c) 2 (a) 3 (d) 4 (b) 5 (b) 6 (b)

2

1 (2, -1) 2 80° 3 4

4 160° 5 180°

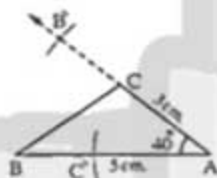
3

[a] $\angle ACD$ is an exterior angle of $\triangle ABC$

$$\therefore m(\angle ACD) = m(\angle A) + m(\angle B) = 25^\circ + 25^\circ = 50^\circ$$

(The req.)

[b]



4

[a] $M \in \overline{AC}$

$$\therefore m(\angle BMC) = 180^\circ - 70^\circ = 110^\circ$$

In $\triangle BMC$:

$$m(\angle MCB) = 180^\circ - (110^\circ + 40^\circ) = 30^\circ$$

$$\therefore m(\angle MCB) = m(\angle MAD)$$

and they are alternate angles

$$\therefore \overline{AD} \parallel \overline{BC} \quad , \quad \therefore \overline{AB} \parallel \overline{DC}$$

$\therefore ABCD$ is a parallelogram (Q.E.D.)

[b] The point (0, 0)

5

[a] In $\triangle ABD$: $\therefore m(\angle ADB) = 90^\circ$

$$\therefore (BD)^2 = (AB)^2 - (AD)^2 = 676 - 576 = 100$$

$$\therefore BD = \sqrt{100} = 10 \text{ cm.}$$

In $\triangle ADC$: $\therefore m(\angle ADC) = 90^\circ$

$$\therefore (CD)^2 = (AC)^2 - (AD)^2 = 900 - 576 = 324$$

$$\therefore CD = \sqrt{324} = 18 \text{ cm.}$$

$$\therefore BC = 10 + 18 = 28 \text{ cm.} \quad (\text{First req.})$$

$$\therefore \text{The area of } \triangle ABC = \frac{1}{2} BC \times AD \\ = \frac{1}{2} \times 28 \times 24 = 336 \text{ cm}^2$$

(Second req.)

[b] $\therefore ABCD$ is a square

$$\therefore \overline{AD} \parallel \overline{BC} \quad , \quad \therefore E \in \overline{BC}$$

$$\therefore \overline{AD} \parallel \overline{EC} \quad , \quad \therefore \overline{AC} \parallel \overline{DE}$$

$\therefore ACED$ is a parallelogram (Q.E.D.)

Model 2

1

1 (a) 2 (c) 3 (b) 4 (c) 5 (c) 6 (d)

2

1 44 2 (5, 5) 3 1728000

4 bisects the third side. 5 ZYC

3

[a] In $\triangle XYZ$: $\therefore m(\angle Y) = 90^\circ$

$$\therefore (XZ)^2 = (XY)^2 + (YZ)^2 = 49 + 576 = 625$$

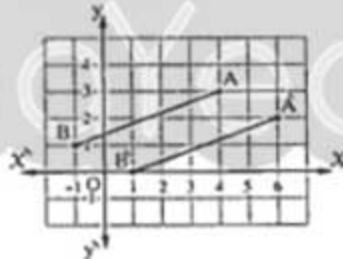
$$\therefore XZ = \sqrt{625} = 25 \text{ cm.}$$

In $\triangle LXZ$: $\therefore m(\angle L) = 90^\circ$

$$\therefore (LZ)^2 = (XZ)^2 - (LX)^2 = 625 - 225 = 400$$

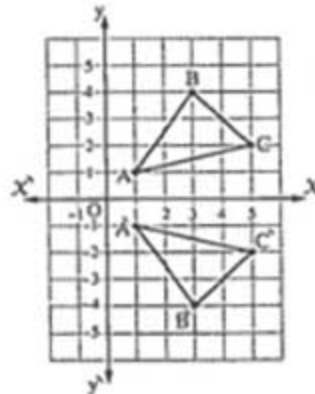
$$\therefore LZ = \sqrt{400} = 20 \text{ cm.} \quad (\text{The req.})$$

[b]



4

[a]



Geometry and Measurement

[b] In $\triangle ABC$: $m(\angle ACB) = 180^\circ - (90^\circ + 30^\circ) = 60^\circ$
 $\therefore \overline{BD} \cap \overline{AO} = \{C\}$

$\therefore m(\angle ACB) = m(\angle OCD) = 60^\circ$ (V.O.A)

$\therefore m(\angle E) = 360^\circ - (60^\circ + 120^\circ + 90^\circ) = 90^\circ$

(The req.)

5

[a] $\therefore \overline{EO} \parallel \overline{CD}$, \overline{EB} is a transversal

$\therefore m(\angle CBA) = m(\angle E) = 50^\circ$ (alternate angles)

From $\triangle ABC$:

$m(\angle BAC) = 180^\circ - (50^\circ + 30^\circ) = 100^\circ$

$\therefore \angle ABD$ is an exterior angle of $\triangle ABC$

$\therefore m(\angle ABD) = 30^\circ + 100^\circ = 130^\circ$ (The req.)

[b] $\therefore \overline{AD} \parallel \overline{XY} \parallel \overline{BC}$, $\therefore AX = XB$

$\therefore DY = YC$

$\therefore Y$ is the midpoint of \overline{CD}

In $\triangle CDE$: $\therefore \overline{ZY} \parallel \overline{DE}$

$\therefore Y$ is the midpoint of \overline{CD}

$\therefore Z$ is the midpoint of \overline{CE}

$\therefore CZ = ZE$

(Q.E.D.)

Model examination for the merge students

- | | | | |
|---|---|---------|----------|
| 1 | 1 c | 2 b | 3 b |
| | 4 a | 5 b | |
| 2 | 1 half | 2 right | 3 6 |
| | 4 (3, -2) | 5 70° | |
| 3 | 1 x | 2 x | 3 ✓ |
| | 4 x | 5 ✓ | |
| 4 | 1 360° | 2 120° | 3 (4, 0) |
| | 4 (-1, -3) | 5 45° | |
| 5 | Fig (1): $X = 8$
Fig (2): $X = 90^\circ$ | | |

Answers of schools examinations on Geometry and Measurement

1 Cairo

1

- 1 360° 2 equal in measure 3 90°
4 $(6, 1)$ 5 half

2

- 1 a 2 d 3 b 4 d 5 d 6 c

3

[a] $\because \overline{GH} \parallel \overline{AB}$, \overline{AG} is a transversal to them

$$\therefore m(\angle A) + m(\angle G) = 180^\circ$$

(two interior angles in the same side of the transversal)

$$\therefore m(\angle A) = 180^\circ - 135^\circ = 45^\circ$$

$\because \overline{DC} \parallel \overline{AB}$, \overline{BD} is a transversal to them

$$\therefore m(\angle B) + m(\angle D) = 180^\circ$$

(two interior angles in the same side of the transversal)

$$\therefore m(\angle B) = 180^\circ - 145^\circ = 35^\circ$$

\therefore In $\triangle ABE$:

$$m(\angle BEA) = 180^\circ - (45^\circ + 35^\circ) = 100^\circ$$

$$\because \overline{AG} \cap \overline{BD} = \{E\}$$

$$\therefore m(\angle DEG) = m(\angle BEA) = 100^\circ \quad (\text{The req.})$$

[b] In $\triangle ABC$:

$\because E$ is the midpoint of \overline{AB}

$\therefore D$ is the midpoint of \overline{AC}

$$\therefore DE = \frac{1}{2} BC$$

$$\text{similarly: } ME = \frac{1}{2} AC$$

$$\therefore DE = MC$$

$$\therefore ME = CD$$

$$\therefore DEMC \text{ is a parallelogram} \quad (\text{Q.E.D.})$$

4

[a] In $\triangle ABC$:

$$\because m(\angle ACB) = 90^\circ$$

$$\therefore (AC)^2 = (AB)^2 - (BC)^2 = (13)^2 - (12)^2 = 25$$

$$\therefore AC = \sqrt{25} = 5 \text{ cm.} \quad (\text{First req.})$$

\therefore the perimeter of the figure ABCD

$$= 13 + 12 + 4 + 3 = 32 \text{ cm.} \quad (\text{Second req.})$$

[b] In $\triangle ABC$:

$\because D$ is the midpoint of \overline{AB}

$\therefore F$ is the midpoint of \overline{BC}

$$\therefore AC = 2 DF = 2 \times 4 = 8 \text{ cm.}$$

$\because D$ is the midpoint of \overline{AB}

$\therefore E$ is the midpoint of \overline{AC}

$$\therefore BC = 2 DE = 2 \times 6 = 12 \text{ cm.}$$

$\because F$ is the midpoint of \overline{BC}

$\therefore E$ is the midpoint of \overline{AC}

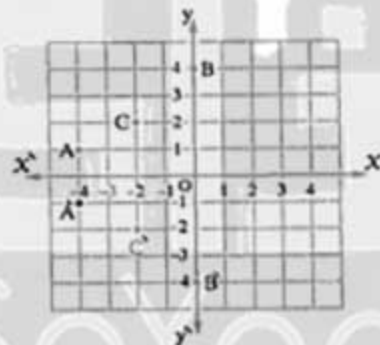
$$\therefore AB = 2 FE = 2 \times 3 = 6 \text{ cm.}$$

$$\therefore \text{The perimeter of } \triangle ABC = 8 + 12 + 6 = 26 \text{ cm.}$$

(The req.)

5

[a]



[b] In $\triangle ABC$:

$$m(\angle ACB) = 180^\circ - (30^\circ + 90^\circ) = 60^\circ$$

$$\therefore m(\angle DCF) = m(\angle ACB) = 60^\circ \quad (\text{V.O.A.})$$

\therefore From the quadrilateral CDEF:

$$m(\angle E) = 360^\circ - (120^\circ + 60^\circ + 90^\circ) = 90^\circ$$

(The req.)

2 Cairo

1

- 1 b 2 d 3 a 4 a 5 d 6 c

2

1 a trapezium.

2 135°

3 $(-3, 1)$

4 9

5 130°

Geometry and Measurement

3

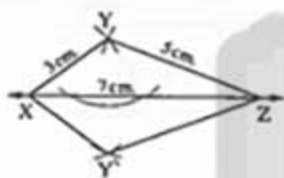
[a] In $\triangle ABC$: $\therefore D$ is the midpoint of \overline{AB} $\therefore E$ is the midpoint of \overline{AC} $\therefore \overline{DE} \parallel \overline{BC}$, $\therefore F \in \overline{CB}$ $\therefore \overline{DE} \parallel \overline{BF}$ $\therefore DE = \frac{1}{2} BC$, $\therefore BF = \frac{1}{2} BC$ $\therefore DE = BF$

From (1) and (2):

 $\therefore DFBE$ is a parallelogram.

(Q.E.D.)

[b]



4

[a] In $\triangle ABC$: $\therefore m(\angle B) = 90^\circ$ $\therefore (AC)^2 = (AB)^2 + (BC)^2$

$$= (9)^2 + (12)^2 = 81 + 144 = 225$$

 $\therefore AC = \sqrt{225} = 15 \text{ cm.}$

(First req.)

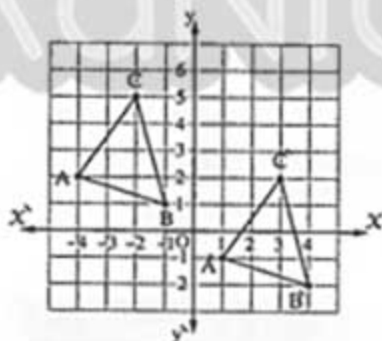
 \therefore In $\triangle ACD$ $\therefore m(\angle ACD) = 90^\circ$ $\therefore (AD)^2 = (AC)^2 + (CD)^2$

$$= (15)^2 + (20)^2 = 225 + 400 = 625$$

 $\therefore AD = \sqrt{625} = 25 \text{ cm.}$

(Second req.)

[b]



5

[a] In $\triangle COE$: $m(\angle COE) = 180^\circ - (50^\circ + 35^\circ) = 95^\circ$ $\therefore m(\angle BOD) = m(\angle COE) = 95^\circ$ (V.O.A.)

from the quadrilateral ABOD

 $\therefore m(\angle B) = 360^\circ - (85^\circ + 100^\circ + 95^\circ) = 80^\circ$

(The req.)

[b] $\therefore \overline{AC} \cap \overline{DE} = \{B\}$ $\therefore m(\angle CBE) = m(\angle ABD) = 40^\circ$ (V.O.A.) $\therefore \overline{BE}$ bisects $\angle CBF$ $\therefore m(\angle EBF) = m(\angle CBE) = 40^\circ$ $\therefore m(\angle ABF) = 180^\circ - (40^\circ + 40^\circ) = 100^\circ$

(The req.)

3

Cairo

1

1 c

2 b

3 c

4 a

5 b

6 a

2

1 the third side

2 $(-2, -4)$

3 2

4 120°

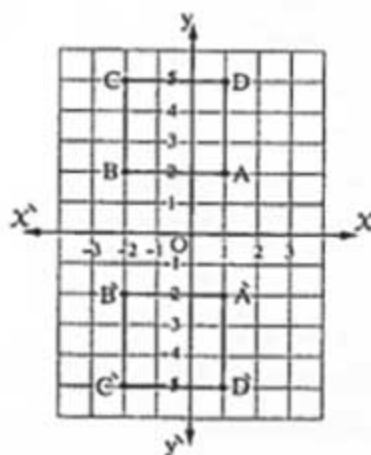
5 216

3

[a] In $\triangle ABC$: $\therefore D$ is the midpoint of \overline{AB} $\therefore E$ is the midpoint of \overline{BC} $\therefore DE = \frac{1}{2} AC$ $\therefore DE = 4 \text{ cm.}$ $\therefore D$ is the midpoint of \overline{AB} $\therefore F$ is the midpoint of \overline{AC} $\therefore DF = \frac{1}{2} BC$ $\therefore DF = 3.5 \text{ cm.}$ $\therefore F$ is the midpoint of \overline{AC} $\therefore E$ is the midpoint of \overline{BC} $\therefore FE = \frac{1}{2} AB$ $\therefore FE = 2.5 \text{ cm.}$ \therefore The perimeter of $\triangle DEF = 4 + 3.5 + 2.5 = 10 \text{ cm.}$

(The req.)

[b]



4

[a] In $\triangle ABC$:

$$\therefore m(\angle B) = 90^\circ$$

$$\therefore (AC)^2 = (AB)^2 + (BC)^2 = (7)^2 + (24)^2 = 625$$

$$\therefore AC = \sqrt{625} = 25 \text{ cm.} \quad (\text{First req.})$$

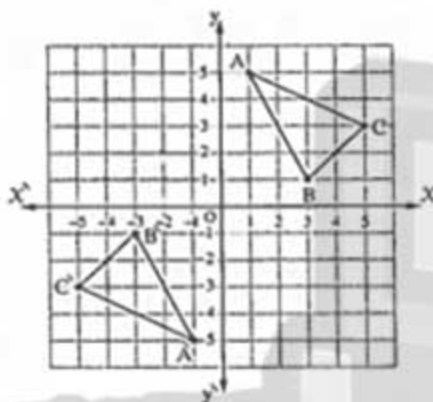
In $\triangle ADC$:

$$\therefore m(\angle D) = 90^\circ$$

$$\therefore (DC)^2 = (AC)^2 - (AD)^2 = (25)^2 - (15)^2 = 400$$

$$\therefore DC = \sqrt{400} = 20 \text{ cm.} \quad (\text{Second req.})$$

[b]



5

[a] In $\triangle ABC$:

$$\therefore m(\angle ABC) = 180^\circ - (50^\circ + 70^\circ) = 60^\circ$$

$$\therefore m(\angle DBE) = m(\angle ABC) = 60^\circ \quad (\text{V.O.A.})$$

from the quadrilateral BDFE:

$$\therefore m(\angle E) = 360^\circ - (60^\circ + 130^\circ + 90^\circ) = 80^\circ \quad (\text{The req.})$$

[b] \because ABCD is a rhombus \therefore BD is a diagonal

$$\therefore m(\angle B) = 2 \times 62^\circ = 124^\circ$$

$$\therefore m(\angle A) = 180^\circ - 124^\circ = 56^\circ \quad (\text{The req.})$$

4 Giza

1

1 c 2 c 3 a 4 b 5 a 6 b

2

1 180° 2 equal in measure.
3 half 4 $(3, -5)$ 5 $(3, 0)$

3

[a] The perimeter of a regular hexagon

$$= 6 \times 15 = 90 \text{ cm.} \quad (\text{First req.})$$

$$\begin{aligned} \text{the measure of each angle} &= \frac{(6-2) \times 180^\circ}{6} \\ &= 120^\circ \end{aligned}$$

(Second req.)

[b] \because ABCD is a parallelogram $\therefore m(\angle B) = 120^\circ$

$$\therefore m(\angle C) = 180^\circ - 120^\circ = 60^\circ$$

$$\therefore m(\angle D) = m(\angle B) = 120^\circ$$

$$\therefore AD = BC = 7 \text{ cm.}$$

$$\therefore DC = AB = 5 \text{ cm.} \quad (\text{The req.})$$

4

[a] $\because \overline{DE} \parallel \overline{BC}$, \overline{BD} is a transversal

$$\therefore m(\angle B) = m(\angle D) = 50^\circ \quad (\text{alternate angles})$$

In $\triangle ABC$:

$$\therefore m(\angle BAC) = 180^\circ - (50^\circ + 30^\circ) = 100^\circ$$

(The req.)

[b] \because X is the midpoint of \overline{AB} \therefore Y is the midpoint of \overline{BC}

$$\therefore XY = \frac{1}{2} AC \quad \therefore XY = 3 \text{ cm.}$$

 \therefore X is the midpoint of \overline{AB} \therefore Z is the midpoint of \overline{AC}

$$\therefore XZ = \frac{1}{2} BC \quad \therefore XZ = 5 \text{ cm.}$$

 \therefore Y is the midpoint of \overline{BC} \therefore Z is the midpoint of \overline{AC}

$$\therefore YZ = \frac{1}{2} AB \quad \therefore YZ = 4 \text{ cm.}$$

$$\therefore \text{The perimeter of } \triangle XYZ = 3 + 5 + 4 = 12 \text{ cm.}$$

(The req.)

5

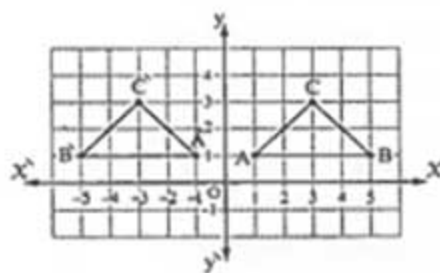
[a] In $\triangle ABC$:

$$\therefore m(\angle B) = 90^\circ$$

$$\therefore (AC)^2 = (AB)^2 + (BC)^2 = (7)^2 + (24)^2 = 625$$

$$\therefore AC = \sqrt{625} = 25 \text{ cm.} \quad (\text{The req.})$$

[b]



Geometry and Measurement

5 Giza

1

- 1 (3, 5) 2 bisects
3 perpendicular and bisect each other
4 360° 5 a right-angled triangle

2

- 1 d 2 d 3 a 4 d 5 a 6 c

3

[a] In $\triangle ABC$:

$$\therefore m(\angle B) = 90^\circ$$

$$\therefore (AC)^2 = (AB)^2 + (BC)^2 = (4)^2 + (3)^2 = 25$$

$$AC = \sqrt{25} = 5 \text{ cm.} \quad (\text{First req.})$$

In $\triangle ACD$:

$$\therefore m(\angle C) = 90^\circ$$

$$\therefore (CD)^2 = (AD)^2 - (AC)^2 = (13)^2 - (5)^2 = 144$$

$$\therefore CD = \sqrt{144} = 12 \text{ cm.} \quad (\text{Second req.})$$

[b] $\therefore ABCD$ is a square

$$\therefore BC = AD$$

$$\therefore BC = CE \quad \therefore AD = CE \quad (1)$$

$$\therefore \overline{BC} \parallel \overline{AD}, E \in \overline{BC}$$

$$\therefore \overline{CE} \parallel \overline{AD} \quad (2)$$

From (1) and (2):

$$\therefore AD = CE \text{ and } \overline{AD} \parallel \overline{CE}$$

$$\therefore ACED \text{ is a parallelogram} \quad (\text{First req.})$$

$$\therefore \overline{AC} \text{ is a diagonal in square } ABCD$$

$$\therefore m(\angle ACB) = 45^\circ$$

$$\therefore m(\angle E) = m(\angle ACB) = 45^\circ$$

$$(\text{corresponding angles}) \quad (\text{Second req.})$$

4

[a] In $\triangle ABC$:

$$\therefore X \text{ is the midpoint of } \overline{AB}$$

$$\therefore Y \text{ is the midpoint of } \overline{BC}$$

$$\therefore AC = 2XY = 2 \times 4 = 8 \text{ cm.}$$

$$\therefore X \text{ is the midpoint of } \overline{AB}$$

$$\therefore Z \text{ is the midpoint of } \overline{CA}$$

$$\therefore BC = 2XZ = 2 \times 5 = 10 \text{ cm.}$$

$$\therefore Z \text{ is the midpoint of } \overline{CA}$$

$$\therefore Y \text{ is the midpoint of } \overline{BC}$$

$$\therefore AB = 2YZ = 2 \times 6 = 12 \text{ cm.}$$

$$\therefore \text{The perimeter of } \triangle ABC = 8 + 10 + 12 = 30 \text{ cm.}$$

(The req.)

[b] In parallelogram $ABCD$

$$m(\angle BCD) = m(\angle A) = 60^\circ \quad (1)$$

, in parallelogram $EBCF$

$$m(\angle EBC) = 180^\circ - 130^\circ = 50^\circ \quad (2)$$

In $\triangle XBC$:

From (1) , (2) :

$$m(\angle BXC) = 180^\circ - (60^\circ + 50^\circ) = 70^\circ \quad (\text{The req.})$$

5

[a] In $\triangle CEF$:

$$m(\angle ECF) = m(\angle E) = m(\angle F) = 60^\circ$$

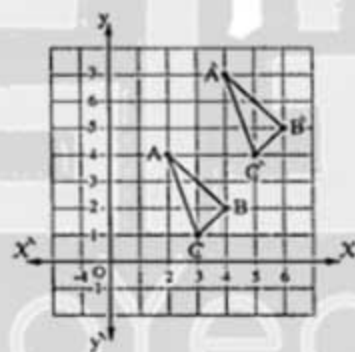
$$\therefore m(\angle BCD) = m(\angle ECF) = 60^\circ \quad (\text{V.O.A.})$$

from the quadrilateral $ABCD$

$$\therefore m(\angle D) = 360^\circ - (80^\circ + 120^\circ + 60^\circ) = 100^\circ$$

(The req.)

[b]



6 Alexandria

1

- 1 a cute
2 half the length of the third side.
3 125 4 (2, -1) 5 120°

2

- 1 d 2 b 3 a 4 c 5 a 6 d

3

[a] $\therefore \overline{AB} \parallel \overline{CD}$, \overline{AC} is a transversal

$$\therefore m(\angle ACD) = m(\angle A) = 50^\circ \quad (\text{alternate angles})$$

$$\therefore \angle ACE \text{ is a right angle}$$

$$\therefore m(\angle ECD) = 90^\circ - 50^\circ = 40^\circ$$

$$\therefore m(\angle E) = m(\angle ECD) = 40^\circ$$

and they are alternate angles

$$\therefore \overline{CD} \parallel \overline{EF}$$

$$\therefore \overline{AB} \parallel \overline{CD} \quad \therefore \overline{AB} \parallel \overline{EF} \quad (\text{Q.E.D.})$$

[b] (0, 0)

4

[a] In $\triangle ABC$:

$$\therefore m(\angle B) = 90^\circ$$

$$\therefore (AB)^2 = (AC)^2 - (BC)^2 = 400 - 144 = 256$$

$$\therefore AB = \sqrt{256} = 16 \text{ cm.}$$

$$\therefore BD = 9 \text{ cm.}$$

$$\therefore AD = 16 - 9 = 7 \text{ cm.}$$

(First req.)

$$\therefore AE = 2 BC = 2 \times 12 = 24 \text{ cm.}$$

$$\therefore \overline{AE} \parallel \overline{BC}, \overline{AB} \text{ is a transversal}$$

$$\therefore m(\angle EAB) = m(\angle B) = 90^\circ \text{ (alternate angles)}$$

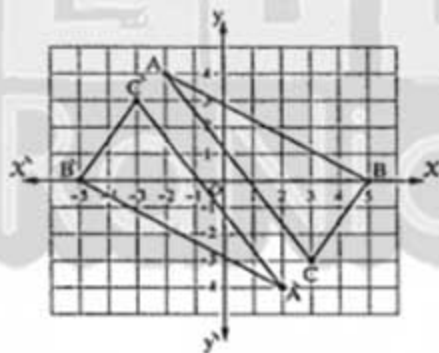
$$\therefore \text{In } \triangle EAD:$$

$$\therefore m(\angle EAD) = 90^\circ$$

$$\therefore (ED)^2 = (AE)^2 + (AD)^2 = (24)^2 + (7)^2 = 625$$

$$\therefore ED = \sqrt{625} = 25 \text{ cm.} \quad (\text{Second req.})$$

[b]



5

[a] $\therefore M \in \overline{AC}$

$$\therefore m(\angle BMC) = 180^\circ - 70^\circ = 110^\circ$$

$$\therefore \text{In } \triangle BMC:$$

$$m(\angle MCB) = 180^\circ - (110^\circ + 40^\circ) = 30^\circ$$

$$\therefore m(\angle MCB) = m(\angle MAD)$$

and they are alternate angles.

$$\therefore \overline{AD} \parallel \overline{BC}$$

$$\therefore \overline{AB} \parallel \overline{DC}$$

$$\therefore ABCD \text{ is a parallelogram.} \quad (\text{Q.E.D.})$$

[b] In $\triangle ABC$:

$$\therefore D \text{ is the midpoint of } \overline{AB}$$

$$\therefore E \text{ is the midpoint of } \overline{BC}$$

$$\therefore DE = \frac{1}{2} AC \quad \therefore DE = 3.5 \text{ cm.}$$

$$\therefore D \text{ is the midpoint of } \overline{AB}$$

$$\therefore F \text{ is the midpoint of } \overline{AC}$$

$$\therefore DF = \frac{1}{2} BC \quad \therefore DF = 4 \text{ cm.}$$

$$\therefore E \text{ is the midpoint of } \overline{BC}$$

$$\therefore F \text{ is the midpoint of } \overline{AC}$$

$$\therefore EF = \frac{1}{2} AB \quad \therefore EF = 2.5 \text{ cm.}$$

$$\therefore \text{The perimeter of } \triangle DEF = 3.5 + 4 + 2.5 = 10 \text{ cm.} \quad (\text{The req.})$$

7

Alexandria

1

$$1) 180^\circ$$

$$2) (4, 2)$$

$$3) \text{ bisects the third side.}$$

$$4) (2, -1)$$

$$5) \text{ half the length of the third side.}$$

$$6) \text{ parallelogram}$$

2

$$1) c$$

$$2) d$$

$$3) b$$

$$4) d$$

$$5) c$$

3

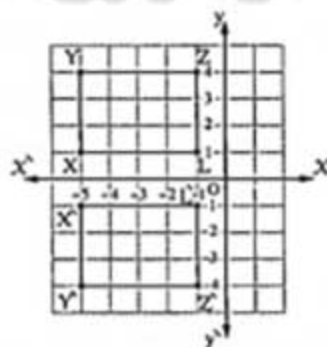
[a] In $\triangle ABC$:

$$\therefore m(\angle A) = 90^\circ$$

$$\therefore (AC)^2 = (CB)^2 - (AB)^2 = 100 - 36 = 64$$

$$\therefore AC = \sqrt{64} = 8 \text{ cm.} \quad (\text{The req.})$$

[b]



4

[a] In $\triangle ABC$:

$$\therefore D \text{ is the midpoint of } \overline{AB}$$

$$\therefore E \text{ is the midpoint of } \overline{BC}$$

Geometry and Measurement

$$\therefore DE = \frac{1}{2} AC \quad \therefore DE = 4$$

$\therefore D$ is the midpoint of \overline{AB}

$\therefore F$ is the midpoint of \overline{AC}

$$\therefore DF = \frac{1}{2} BC \quad \therefore DF = 5$$

$\therefore E$ is the midpoint of \overline{BC}

$\therefore F$ is the midpoint of \overline{AC}

$$\therefore EF = \frac{1}{2} AB \quad \therefore EF = 3.5 \text{ cm.}$$

$$\therefore \text{The perimeter of } \triangle FDE = 4 + 5 + 3.5 = 12.5 \text{ cm.} \quad (\text{The req.})$$

[b] Let the measures of the interior angles of the quadrilateral be $2x, 2x, 3x, 5x$

\therefore the sum of the measures of the interior angles of the quadrilateral $= 360^\circ$

$$\therefore 2x + 2x + 3x + 5x = 360^\circ$$

$$\therefore 12x = 360^\circ \quad \therefore x = \frac{360^\circ}{12} = 30^\circ$$

$$\therefore \text{The measure of the biggest angle} = 5 \times 30^\circ = 150^\circ \quad (\text{The req.})$$

5

[a] (3, -8)

[b] In $\triangle ABC$:

$\therefore \angle ACD$ is an exterior angle of $\triangle ABC$

$$\therefore m(\angle ACD) = m(\angle A) + m(\angle B) = 30^\circ + 30^\circ = 60^\circ \quad (\text{The req.})$$

8 El-Kalyoubia

1

1 b 2 b 3 d 4 c 5 d 6 b

2

1 2 2 8000 3 (-3, -2)
4 140° 5 120

3

[a] In $\triangle ABC$:

$$m(\angle ABC) = 180^\circ - (70^\circ + 50^\circ) = 60^\circ$$

$$\therefore m(\angle DBF) = m(\angle ABC) = 60^\circ \quad (\text{V.O.A.})$$

from the quadrilateral BDEF

$$\therefore m(\angle F) = 360^\circ - (60^\circ + 140^\circ + 90^\circ) = 70^\circ \quad (\text{The req.})$$

[b] $\therefore D$ is the midpoint of \overline{AB}

$\therefore F$ is the midpoint of \overline{AC}

$$\therefore DF = \frac{1}{2} BC = 6 \text{ cm.}$$

$\therefore D$ is the midpoint of \overline{AB}

$\therefore E$ is the midpoint of \overline{BC}

$$\therefore DE = \frac{1}{2} AC = 5 \text{ cm.}$$

$$\therefore CE = \frac{1}{2} BC = 6 \text{ cm.} \quad \therefore CF = \frac{1}{2} AC = 5 \text{ cm.}$$

$$\therefore \text{The perimeter of } \triangle DEC = 6 + 5 + 6 + 5 = 22 \text{ cm.} \quad (\text{The req.})$$

4

[a] $\therefore ABCD$ is a square $\therefore \overline{AD} \parallel \overline{BC}$

$\therefore E \in \overline{BC} \quad \therefore \overline{AD} \parallel \overline{CE}$

$\therefore \overline{AC} \parallel \overline{ED}$

$\therefore ACED$ is a parallelogram. (First req.)

$\therefore \overline{AC}$ is a diagonal in square $ABCD$

$$\therefore m(\angle ACB) = 45^\circ$$

$$\therefore m(\angle ACE) = 180^\circ - 45^\circ = 135^\circ \quad (\text{Second req.})$$

[b] In $\triangle ADC$:

$$\therefore m(\angle ADC) = 90^\circ$$

$$\therefore (CD)^2 = (AC)^2 - (AD)^2 = (30)^2 - (24)^2 = 324$$

$$\therefore CD = \sqrt{324} = 18 \text{ cm.}$$

In $\triangle ADB$:

$$m(\angle ADB) = 90^\circ$$

$$\therefore (BD)^2 = (AB)^2 - (AD)^2 = (26)^2 - (24)^2 = 100$$

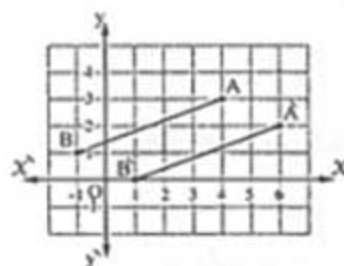
$$\therefore BD = \sqrt{100} = 10 \text{ cm.}$$

$$\therefore BC = 18 + 10 = 28 \text{ cm.} \quad (\text{First req.})$$

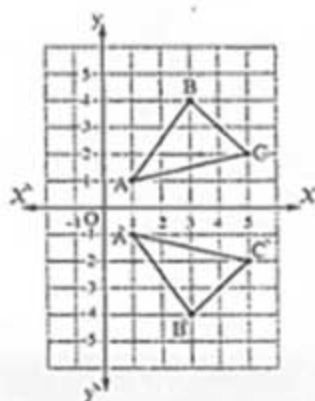
$$\therefore \text{The area of } \triangle ABC = \frac{1}{2} \times 28 \times 24 = 336 \text{ cm}^2. \quad (\text{Second req.})$$

5

[a]



[b]



9 El-Gharbia

[1]

- 1 d 2 d 3 b 4 c 5 c 6 c

[2]

- 1 parallel to the third side.
2 120 3 $(-3, -2)$
4 equal in measure. 5 a right angle.

[3]

- [a] $\overline{AC} \cap \overline{DE} = \{B\}$
 $\therefore m(\angle CBE) = m(\angle ABD) = 40^\circ$ (V.O.A.)
 $\therefore \overline{BE}$ bisects $\angle CBF$
 $\therefore m(\angle FBE) + m(\angle EBC) = 80^\circ$
 $\therefore m(\angle FBC) = 80^\circ$
 $\therefore B \in \overline{AC}$
 $\therefore m(\angle ABF) = 180^\circ - 80^\circ = 100^\circ$ (The req.)

- [b] $\therefore \overline{DE} \parallel \overline{CB}$, \overline{BD} is a transversal
 $\therefore m(\angle B) = m(\angle D) = 50^\circ$ (alternate angles)
 In $\triangle ABC$:
 $m(\angle BAC) = 180^\circ - (35^\circ + 50^\circ) = 95^\circ$ (The req.)

[4]

- [a] In $\triangle XYZ$:
 $\therefore D$ is the midpoint of \overline{XY}
 $\therefore O$ is the midpoint of \overline{YZ}
 $\therefore DO = \frac{1}{2} XZ = 3$ cm.
 $\therefore D$ is the midpoint of \overline{XY}
 $\therefore E$ is the midpoint of \overline{XZ}
 $\therefore DE = \frac{1}{2} YZ = 3.5$ cm.
 $\therefore O$ is the midpoint of \overline{YZ}

$\therefore E$ is the midpoint of \overline{XZ}

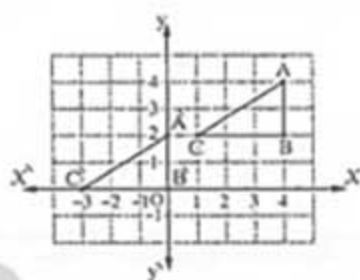
$$\therefore OE = \frac{1}{2} XY = 2.5 \text{ cm.}$$

\therefore The perimeter of $\triangle DOE$

$$= 3 + 3.5 + 2.5 = 9 \text{ cm.}$$

(The req.)

[b]



[a]

In $\triangle ABC$:

$$\therefore m(\angle B) = 90^\circ$$

$$\therefore (AC)^2 = (AB)^2 + (BC)^2 = (12)^2 + (9)^2 = 225$$

$$\therefore AC = \sqrt{225} = 15 \text{ cm.}$$

In $\triangle ACD$:

$$\therefore m(\angle ACD) = 90^\circ$$

$$\therefore (AD)^2 = (AC)^2 + (CD)^2 = (15)^2 + (20)^2 = 625$$

$$\therefore AD = \sqrt{625} = 25 \text{ cm.}$$

(The req.)

[b] $\therefore ABCD$ is a square

$$\therefore \overline{AD} \parallel \overline{BC}$$

$$\therefore E \in \overline{BC}$$

$$\therefore \overline{AD} \parallel \overline{CE}$$

$$\therefore \overline{AC} \parallel \overline{DE}$$

$\therefore ACED$ is a parallelogram.

(Q.E.D.)

10 El-Dakahlia

[1]

- 1 d 2 c 3 d 4 c 5 a 6 c

[2]

- 1 120° 2 35° 3 9 cm.
4 $(9, -6)$ 5 a right angle.

[3]

[a] In $\triangle ADC$:

$$\therefore m(\angle ADC) = 90^\circ$$

$$\therefore (CD)^2 = (AC)^2 - (AD)^2 = (30)^2 - (24)^2 = 324$$

$$\therefore CD = \sqrt{324} = 18 \text{ cm.}$$

In $\triangle ADB$:

$$\therefore m(\angle ADB) = 90^\circ$$

Geometry and Measurement

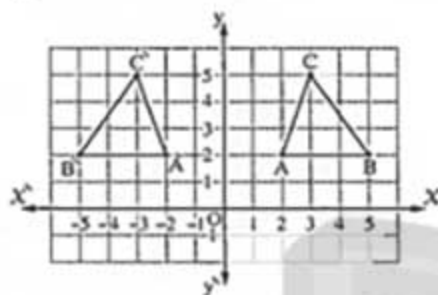
$$\therefore (BD)^2 = (AB)^2 - (AD)^2 = (26)^2 - (24)^2 = 100$$

$$\therefore BD = \sqrt{100} = 10 \text{ cm.}$$

$$\therefore BC = 18 + 10 = 28 \text{ cm.} \quad (\text{First req.})$$

$$\therefore \text{The area of } \triangle ABC = \frac{1}{2} \times 28 \times 24 = 336 \text{ cm}^2. \quad (\text{Second req.})$$

[b]



4

[a] In $\triangle DEF$:

$$\therefore m(\angle DFE) = 60^\circ$$

$$\therefore m(\angle CFG) = m(\angle DFE) = 60^\circ \quad (\text{V.O.A.})$$

\therefore the sum of measures of interior angles of the pentagon $= (5 - 2) \times 180^\circ = 540^\circ$

$$\therefore m(\angle C) + m(\angle G) = 540^\circ - (100^\circ + 90^\circ + 60^\circ) = 290^\circ$$

$$\therefore m(\angle C) = m(\angle G)$$

$$\therefore m(\angle C) = \frac{290^\circ}{2} = 145^\circ \quad (\text{The req.})$$

[b] In $\triangle ABC$:

\therefore D is the midpoint of \overline{AB}

\therefore E is the midpoint of \overline{AC}

$$\therefore \overline{DE} \parallel \overline{BC}, DE = \frac{1}{2} BC = 6 \text{ cm.}$$

\therefore In $\triangle FDE$:

\therefore X is the midpoint of \overline{DF}

$\therefore \overline{XY} \parallel \overline{DE}$

\therefore Y is the midpoint of \overline{EF}

$$\therefore XY = \frac{1}{2} DE = 3 \text{ cm.} \quad (\text{The req.})$$

5

[a] \therefore ABCD is a square

$$\therefore \overline{AD} \parallel \overline{BC}$$

$$\therefore E \in \overline{BC} \therefore \overline{AD} \parallel \overline{CE}$$

$$\therefore \overline{AC} \parallel \overline{ED}$$

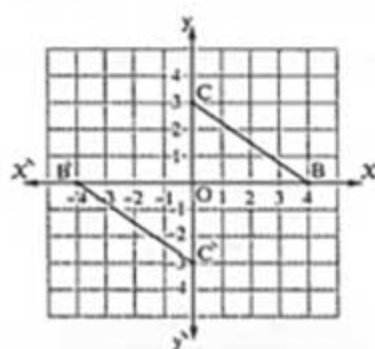
$$\therefore ACED \text{ is a parallelogram.} \quad (\text{First req.})$$

$\therefore \overline{AC}$ is a diagonal in square ABCD

$$\therefore m(\angle ACB) = 45^\circ$$

$$\therefore m(\angle ACE) = 180^\circ - 45^\circ = 135^\circ \quad (\text{Second req.})$$

[b]



11 Suez

1

- 1 b 2 b 3 d 4 b 5 d 6 c

2

- 1 140° 2 bisects the third side.
3 $(1, 2)$ 4 540° 5 $\overline{AC} \perp \overline{BD}$

3

$$[a] m(\angle ABE) = 180^\circ - 116^\circ = 64^\circ$$

$\therefore \overline{BD}$ bisects $\angle ABE$

$$\therefore m(\angle ABD) = \frac{1}{2} m(\angle ABE) = 32^\circ \quad (\text{The req.})$$

$$[b] m(\angle DBE) = 360^\circ - (110^\circ + 35^\circ + 140^\circ) = 75^\circ \quad (\text{The req.})$$

4

[a] $\therefore \overline{AB} \parallel \overline{CD}, \overline{AC}$ is a transversal

$$\therefore m(\angle ACD) = m(\angle A) = 50^\circ \quad (1) \quad (\text{alternate angles})$$

$\therefore \overline{CD} \parallel \overline{EF}, \overline{CE}$ is a transversal

$$\therefore m(\angle ECD) = m(\angle E) = 40^\circ \quad (2) \quad (\text{alternate angles})$$

From (1) & (2):

$$\therefore m(\angle ACE) = m(\angle ACD) + m(\angle ECD) = 50^\circ + 40^\circ = 90^\circ \quad (\text{The req.})$$

[b] In $\triangle ABC$:

$$\therefore m(\angle B) = 90^\circ$$

$$\therefore (AC)^2 = (AB)^2 + (BC)^2 = (6)^2 + (8)^2 = 36 + 64 = 100$$

$$\therefore AC = \sqrt{100} = 10 \text{ cm.} \quad (\text{The req.})$$

5

- [a] 1 $(-2, 3)$ 2 $(-3, -2)$
3 $(-3, -2)$ 4 3

[b] In $\triangle ABC$:

$$m(\angle ACB) = 180^\circ - (60^\circ + 90^\circ) = 30^\circ$$

$$\therefore m(\angle DCF) = m(\angle ACB) = 30^\circ \quad (\text{V.O.A.})$$

 \therefore in the polygon CDEF:

$$m(\angle E) = 360^\circ - (30^\circ + 120^\circ + 90^\circ) = 120^\circ$$

(The req.)

12 Port Said

1

- 1 b 2 c 3 b 4 b 5 b 6 d

2

- 1 $\frac{1}{2}$ 2 (3, -2) 3 360°
4 120° 5 6

3

[a] In $\triangle ABC$:

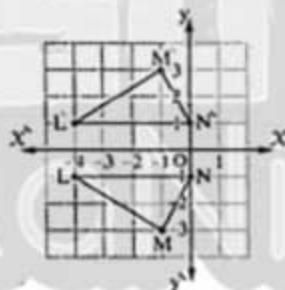
$$\therefore m(\angle B) = 90^\circ$$

$$\therefore (AC)^2 = (AB)^2 + (BC)^2$$

$$= (3)^2 + (4)^2 = 9 + 16 = 25$$

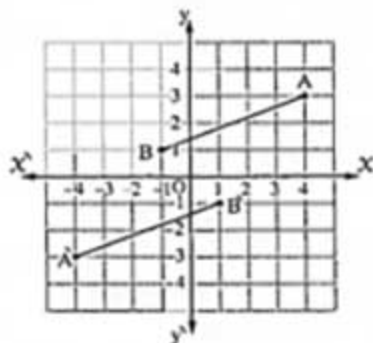
$$\therefore AC = \sqrt{25} = 5 \text{ cm.} \quad (\text{The req.})$$

[b]



4

[a]

[b] $\therefore \overline{DC} \parallel \overline{EO}$, \overline{DE} is a transversal

$$\therefore m(\angle E) + m(\angle D) = 180^\circ$$

(interior angles on the same side of the transversal)

$$\therefore m(\angle E) = 180^\circ - 90^\circ = 90^\circ$$

$$\therefore m(\angle C) = 360^\circ - (120^\circ + 90^\circ + 90^\circ) = 60^\circ$$

(The req.)

5

[a] In $\triangle ABC$: \therefore D is the midpoint of \overline{AB} \therefore E is the midpoint of \overline{AC}

$$\therefore CB = 2 ED = 16 \text{ cm.} \quad (\text{The req.})$$

[b] $\therefore \angle ACD$ is an exterior angle of $\triangle ABC$

$$\therefore m(\angle ACD) = 25^\circ + 25^\circ = 50^\circ \quad (\text{The req.})$$

13 Kafr El-Sheikh

1

- 1 c 2 b 3 b 4 c 5 d 6 b

2

- 1 (1, 1) 2 a square 3 (1, -2)
4 half 5 28

3

[a] From the pentagon ABCDE

$$m(\angle A) + m(\angle B) + m(\angle C) + m(\angle D) + m(\angle DEA) = 540^\circ$$

$$\therefore m(\angle C) = 540^\circ - (110^\circ + 120^\circ + 90^\circ + 115^\circ) = 105^\circ$$

(The req.)

[b] $\therefore \overline{ED} \parallel \overline{BC}$, \overline{EC} is a transversal

$$\therefore m(\angle C) + m(\angle E) = 180^\circ$$

(interior angles on the same side of the transversal)

$$\therefore m(\angle C) = 180^\circ - 110^\circ = 70^\circ$$

 $\therefore \overline{FH} \parallel \overline{BC}$, \overline{FB} is a transversal

$$\therefore m(\angle B) + m(\angle F) = 180^\circ$$

(interior angles on the same side of the transversal)

$$\therefore m(\angle B) = 180^\circ - 130^\circ = 50^\circ$$

 \therefore In $\triangle ABC$:

$$m(\angle BAC) = 180^\circ - (70^\circ + 50^\circ) = 60^\circ \quad (\text{The req.})$$

4

[a] In $\triangle ABC$:

$$\therefore m(\angle B) = 90^\circ$$

$$\therefore (AC)^2 = (AB)^2 + (BC)^2 = (7)^2 + (24)^2 = 625$$

Geometry and Measurement

$$\therefore AC = \sqrt{625} = 25 \text{ cm.}$$

(First req.)

In $\triangle ACD$:

$$\therefore m(\angle D) = 90^\circ$$

$$\therefore (DC)^2 = (AC)^2 - (AD)^2 = (25)^2 - (15)^2 = 400$$

$$\therefore DC = \sqrt{400} = 20 \text{ cm.}$$

(Second req.)

[b] In $\triangle ABC$: $\therefore X$ is the midpoint of \overline{AB} $\therefore Y$ is the midpoint of \overline{AC}

$$\therefore XY = \frac{1}{2} BC = 4 \text{ cm.}$$

 $\therefore X$ is the midpoint of \overline{AB} $\therefore Z$ is the midpoint of \overline{BC}

$$\therefore XZ = \frac{1}{2} AC = 4 \text{ cm.}$$

 $\therefore Y$ is the midpoint of \overline{AC} $\therefore Z$ is the midpoint of \overline{BC}

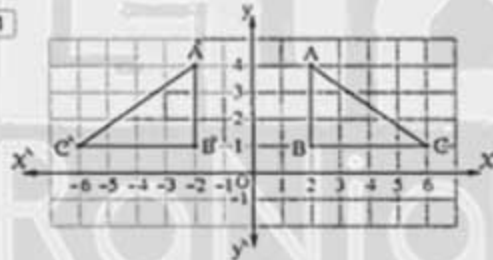
$$\therefore YZ = \frac{1}{2} AB = 3 \text{ cm.}$$

$$\therefore \text{The perimeter of } \triangle XYZ = 4 + 4 + 3 = 11 \text{ cm.}$$

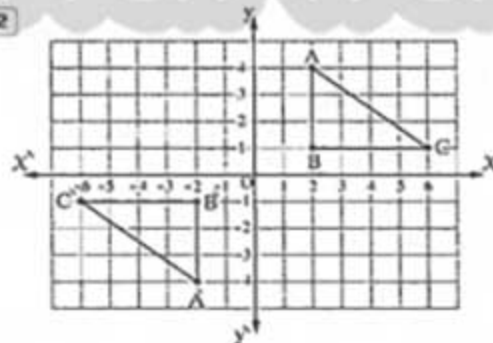
(The req.)

5

[a] 1



2

[b] $\therefore E \in \overline{CD}$

$$\therefore m(\angle ADC) = 180^\circ - 60^\circ = 120^\circ$$

 $\therefore ABCD$ is a parallelogram

$$\therefore m(\angle B) = m(\angle ADC) = 120^\circ$$

(The req.)

14 Beni Suef

1

1 c

2 a

3 c

4 c

5 c

6 d

2

1 equal in length. 2 bisects the third side.

3 the sum of areas of the squares on the sides of the right angle.

4 $\triangle ZYC$

5 equal in measure.

3

$$[a] \therefore m(\angle EAC) + m(\angle BAC) + m(\angle EAB) = 360^\circ$$

$$\therefore m(\angle BAC) = 360^\circ - (130^\circ + 90^\circ) = 140^\circ$$

(First req.)

 $\therefore \overline{AB} \parallel \overline{CD}$, \overline{AC} is a transversal to them.

$$\therefore m(\angle C) + m(\angle CAB) = 180^\circ$$

(Two interior angles in the same side of the transversal)

$$\therefore m(\angle C) = 180^\circ - 140^\circ = 40^\circ \quad (\text{Second req.})$$

[b] $\therefore ABCD$ is a rhombus, \overline{AC} is a diagonal

$$\therefore m(\angle BCD) = 2 \times 32^\circ = 64^\circ$$

$$\therefore m(\angle D) = 180^\circ - 64^\circ = 116^\circ \quad (\text{The req.})$$

4

[a] In $\triangle ABC$: $\therefore D$ is the midpoint of \overline{AB} $\therefore E$ is the midpoint of \overline{AC}

$$\therefore BC = 2 DE = 2 \times 4 = 8 \text{ cm.}$$

$$\therefore BD = AD = 3 \text{ cm.}$$

$$\therefore CE = AE = 2 \text{ cm.}$$

 \therefore The perimeter of $DBCE$

$$= 3 + 8 + 2 + 4 = 17 \text{ cm.}$$

(The req.)

[b] In $\triangle ADC$:

$$\therefore m(\angle ADC) = 90^\circ$$

$$\therefore (AD)^2 = (AC)^2 - (CD)^2 \\ = (20)^2 - (16)^2 = 144$$

$$\therefore AD = \sqrt{144} = 12 \text{ cm.}$$

(First req.)

In $\triangle ADB$: $\therefore m(\angle ADB) = 90^\circ$

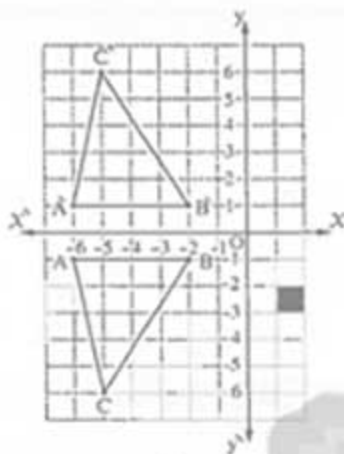
$$\therefore (AB)^2 = (AD)^2 + (BD)^2 \\ = (12)^2 + (9)^2 = 225$$

$$\therefore AB = \sqrt{225} = 15 \text{ cm.}$$

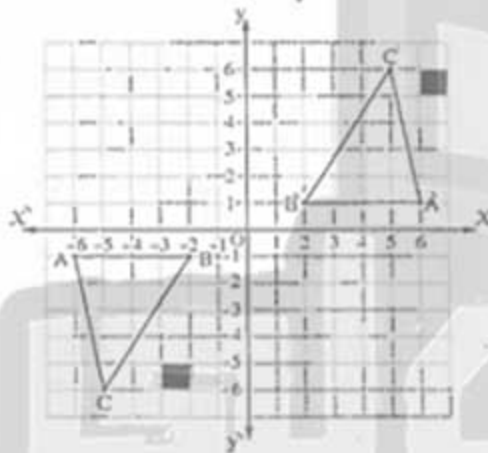
(Second req.)

5

1



2



15 Souhag

1

1 c 2 c 3 c 4 d 5 a 6 a

2

1 parallel to the third side, equal to half of its length.

2 15

3 (-2, -1)

4 Y

5 bisects the third side.

3

[a] In $\triangle ABC$: $\therefore X$ is the midpoint of \overline{AB} $\therefore Y$ is the midpoint of \overline{AC} $\therefore XY = \frac{1}{2} BC = 4.5$ cm. $\therefore X$ is the midpoint of \overline{AB} $\therefore Z$ is the midpoint of \overline{BC} $\therefore XZ = \frac{1}{2} AC = 5$ cm. $\therefore Y$ is the midpoint of \overline{AC} $\therefore Z$ is the midpoint of \overline{BC} $\therefore YZ = \frac{1}{2} AB = 3.5$ cm. \therefore The perimeter of $\triangle XYZ = 4.5 + 5 + 3.5 = 13$ cm. (The req.)[b] $\therefore \overline{DE} \parallel \overline{CB}$, \overline{BD} is a transversal $\therefore m(\angle B) = m(\angle D) = 60^\circ$ (alternate angles) $\therefore \angle DAC$ is an exterior angle of $\triangle ABC$ $\therefore m(\angle DAC) = 50^\circ + 60^\circ = 110^\circ$ (The req.)

4

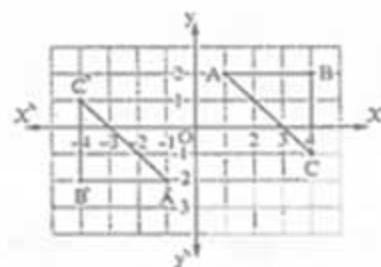
[a] $\therefore \overline{DA} \parallel \overline{CB}$, \overline{AB} is a transversal $\therefore m(\angle B) = m(\angle EAB) = 120^\circ$ (alternate angles) $\therefore m(\angle B) + m(\angle C) = 120^\circ + 60^\circ = 180^\circ$

and they are interior angles on the same side of the transversal

 $\therefore \overline{AB} \parallel \overline{CD}$ $\therefore \overline{AD} \parallel \overline{BC}$ $\therefore ABCD$ is a parallelogram (Q.E.D.)[b] In $\triangle ABC$: $\therefore m(\angle B) = 90^\circ$ $\therefore (AC)^2 = (AB)^2 + (BC)^2 = (3)^2 + (4)^2 = 25$ $\therefore AC = \sqrt{25} = 5$ cm. (First req.)In $\triangle ACD$: $\therefore m(\angle ACD) = 90^\circ$ $\therefore (CD)^2 = (AD)^2 - (AC)^2 = (13)^2 - (5)^2 = 144$ $\therefore CD = \sqrt{144} = 12$ cm. (Second req.)

5

[a]



[b] 1 CBM

2 MCD

3 CDM

4 DEM